

Automazione (Laboratorio)

Tecniche di Controllo

Reti Neurali e Modelli Fuzzy per L'Identificazione, Predizione E Controllo

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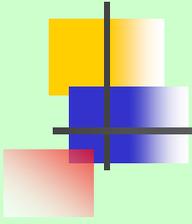
Lecture Notes on Neural Networks and Fuzzy Systems

Silvio Simani

References

Textbook (*suggested*):

- *Neural Networks for Identification, Prediction, and Control*, by Duc Truong Pham and Xing Liu. Springer Verlag; (December 1995). ISBN: 3540199594
- *Nonlinear Identification and Control: A Neural Network Approach*, by G. P. Liu. Springer Verlag; (October 2001). ISBN: 1852333421.
- *Fuzzy Modeling for Control*, by Robert Babuska. Springer; 1st edition (May 1, 1998) ISBN-10: 0792381548, ISBN-13: 978-0792381549.
- *Multi-Objective Optimization using Evolutionary Algorithms*, by Deb Kalyanmoy. John Wiley & Sons, Ltd, Chichester, England, 2001.

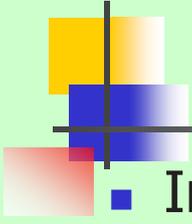


Course Overview

1. Introduction
 - i. Course introduction
 - ii. Introduction to neural network
 - iii. Issues in neural network
2. Simple neural network
 - i. Perceptron
 - ii. Adaline
3. Multilayer Perceptron
 - i. Basics
4. Genetic Algorithms: overview
5. Radial basis networks: overview
6. Fuzzy Systems: overview
7. Application examples

14/04/2009

3/148



Machine Learning

- Improve automatically with experience
- Imitating human learning
 - Human learning
 - Fast recognition and classification of complex classes of objects and concepts and fast adaptation
 - Example: neural networks
- Some techniques assume statistical source
 - Select a statistical model to model the source
- Other techniques are based on reasoning or inductive inference (e.G. Decision tree)

14/04/2009

4/148

Machine Learning Definition

A computer program is said to **learn** from *experience* **E** with respect to some class of *tasks* **T** and *performance measure* **P**, if its performance at tasks in **T**, as measured by **P**, improves with experience.

14/04/2009

5/148

Examples of Learning Problems

Example 1: handwriting recognition:

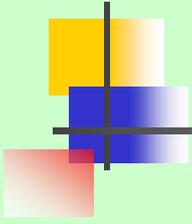
- T: recognizing and classifying handwritten words within images.
- P: percentage of words correctly classified.
- E: a database of handwritten words with given classification.

Example 2: learn to play checkers:

- T: play checkers.
- P: percentage of games won in a tournament.
- E: opportunity to play against itself (**war games...**).

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6/148

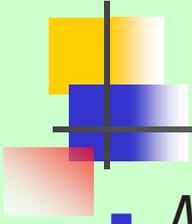


Issues in *Machine Learning*

- What algorithms can approximate functions well and when?
- How does the number of training examples influence accuracy?
- How does the complexity of hypothesis representation impact it?
- How does noisy data influence accuracy?
- *How do you reduce a learning problem to a set of function approximation ?*

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7/148

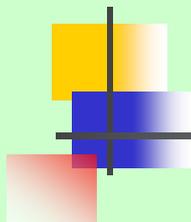


Summary

- *Machine learning* is useful for data mining, poorly understood domain (face recognition) and programs that must dynamically adapt.
- Draws from many diverse disciplines.
- Learning problem needs well-specified task, performance metric and training experience.
- Involve searching space of possible hypotheses. Different learning methods search different hypothesis space, such as numerical functions, *neural networks*, decision trees, symbolic rules.

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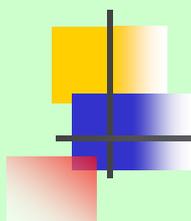
8/148



Introduction to Neural Networks

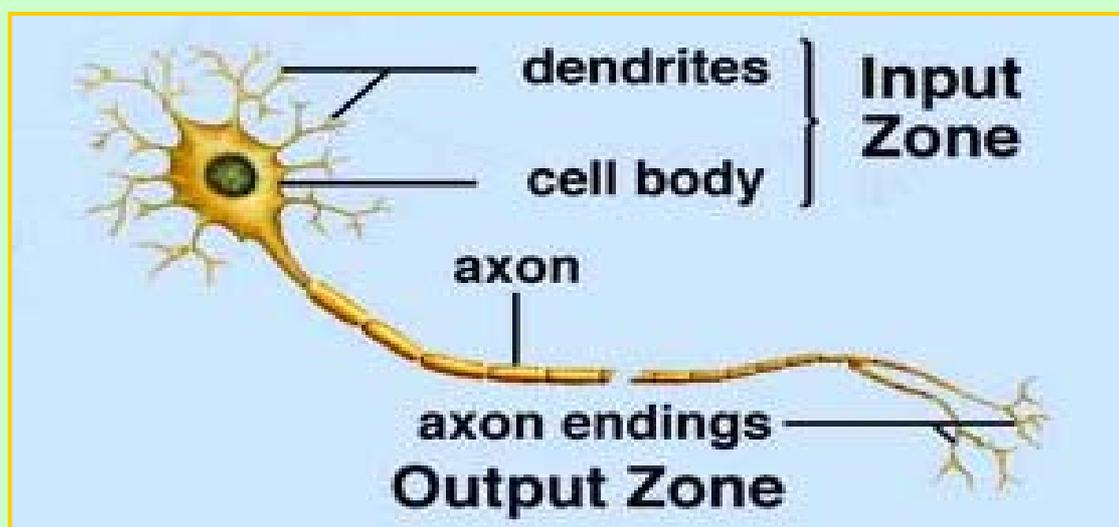
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9/148



Brain

- 10^{11} neurons (processors)
- On average 1000-10000 connections



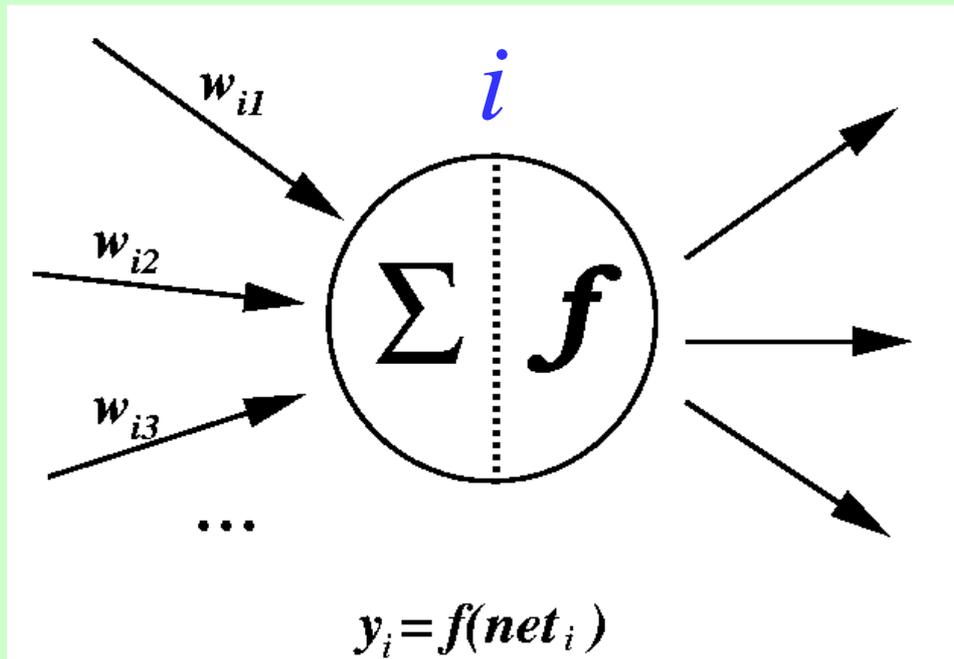
14/04/2009

10/148

Artificial Neuron

$$net_i = \sum_j w_{ij} y_j + b$$

bias



14/04/2009

11/148

Artificial Neuron

- Input/Output Signal may be.
 - Real value.
 - Unipolar $\{0, 1\}$.
 - Bipolar $\{-1, +1\}$.
- Weight : w_{ij} – strength of connection.

Note that w_{ij} refers to the weight from **unit j to unit i** (not the other way round).

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12/148

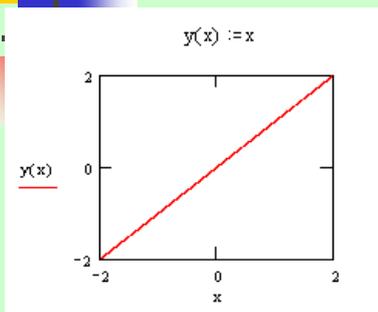
Artificial Neuron

- The bias b is a constant that can be written as $w_{i0}y_0$ with $y_0 = b$ and $w_{i0} = 1$ such that

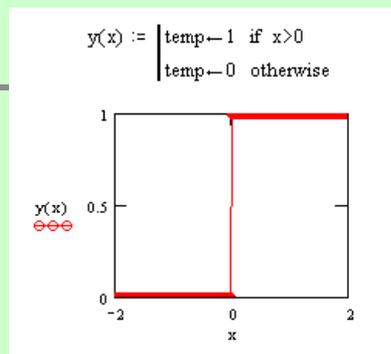
$$net_i = \sum_{j=0}^n w_{ij} y_j$$

- The function f is the unit's **activation function**. In the simplest case, f is the identity function, and the unit's output is just its net input. This is called a **linear unit**.
- Other activation functions are : **step function, sigmoid function and Gaussian function.**

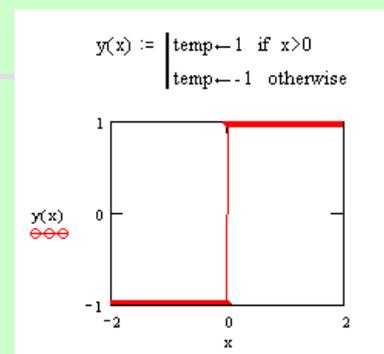
Activation Functions



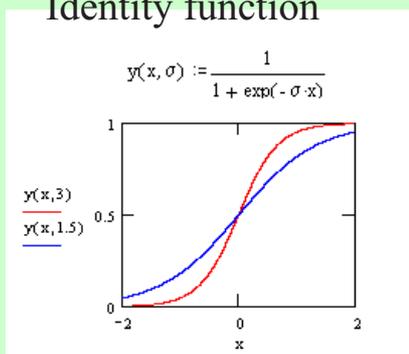
Identity function



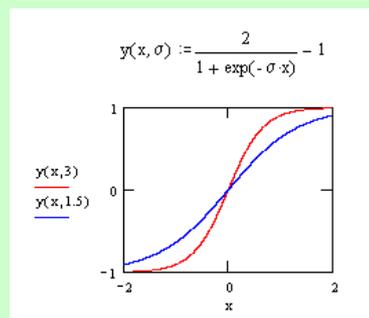
Binary Step function



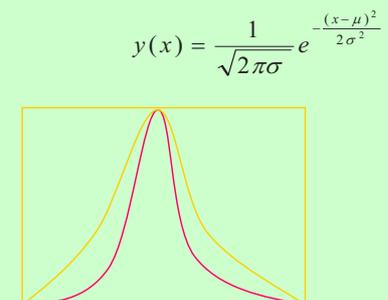
Bipolar Step function



Sigmoid function



Bipolar Sigmoid function



Gaussian function

When Should ANN Solution Be Considered ?

- The solution to the problem cannot be explicitly described by an algorithm, a set of equations, or a set of rules.
- There is some evidence that an input-output mapping exists between a set of input and output variables.
- There should be a large amount of data available to train the network.

14/04/2009

15/148

Problems That Can Lead to Poor Performance ?

- The network has to distinguish between very similar cases with a very high degree of accuracy.
- The train data does not represent the ranges of cases that the network will encounter in practice.
- The network has a several hundred inputs.
- The main discriminating factors are not present in the available data, *e.g.* trying to assess the loan application without having knowledge of the applicant's salaries.
- The network is required to implement a very complex function.

14/04/2009

16/148

Applications of Artificial Neural Networks

- Manufacturing : fault diagnosis, fraud detection.
- Retailing : fraud detection, forecasting, data mining.
- Finance : fraud detection, forecasting, data mining.
- Engineering : fault diagnosis, signal/image processing.
- Production : fault diagnosis, forecasting.
- Sales & marketing : forecasting, data mining.

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17/148

Data Pre-processing

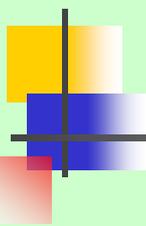
Neural networks very **rarely** operate on the raw data. An initial **pre-processing** stage is essential.

Some examples are as follows:

- Feature extraction of images: for example, the analysis of x-rays requires pre-processing to extract features which may be of interest within a specified region.
- Representing input variables with numbers. For example "+1" is the person is married, "0" if divorced, and "-1" if single. Another example is representing the pixels of an image: 255 = bright white, 0 = black. To ensure the generalization capability of a neural network, the data should be encoded in form which allows for interpolation.

14/04/2009

18/148



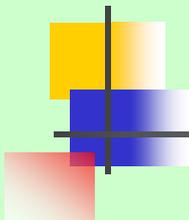
Data Pre-processing

■ CONTINUOUS VARIABLES

- A continuous variable can be directly applied to a neural network. However, if the dynamic range of input variables are not approximately the same, it is better to *normalize* all input variables of the neural network.

14/04/2009

19/148



Simple Neural Networks

Simple Perceptron

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20/148

Outlines

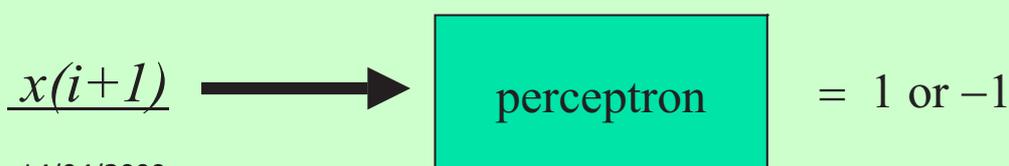
- The Perceptron
 - Linearly separable problem
 - Network structure
 - Perceptron learning rule
 - Convergence of Perceptron

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21/148

THE PERCEPTRON

- The perceptron was a simple model of ANN introduced by Rosenblatt of MIT in the 1960' with the idea of learning.
- Perceptron is designed to accomplish a **simple pattern recognition** task: after learning with real value training data $\{ \underline{x(i)}, d(i), i = 1, 2, \dots, p \}$ where $d(i) = 1$ or -1
- For a new signal (pattern) $\underline{x(i+1)}$, the perceptron is capable of telling you to which class the new signal belongs

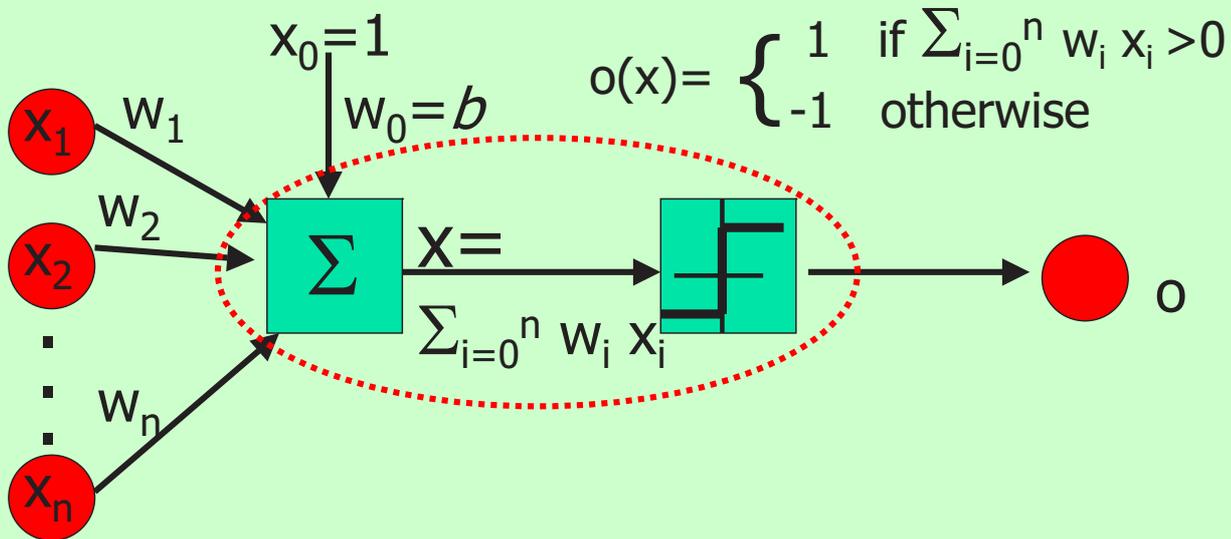


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22/148

Perceptron

Linear Threshold Unit (LTU)



14/04/2009

23/148

Mathematically the Perceptron is

$$y = f\left(\sum_{i=1}^m w_i x_i + b\right) = f\left(\sum_{i=0}^m w_i x_i\right)$$

We can always treat the bias b as another weight with inputs equal 1

where f is the hard limiter function i.e.

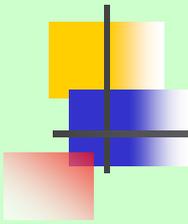
$$y = \begin{cases} 1 & \text{if } \sum_{i=1}^m w_i x_i + b > 0 \\ -1 & \text{if } \sum_{i=1}^m w_i x_i + b \leq 0 \end{cases}$$

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24/148

Why is the network

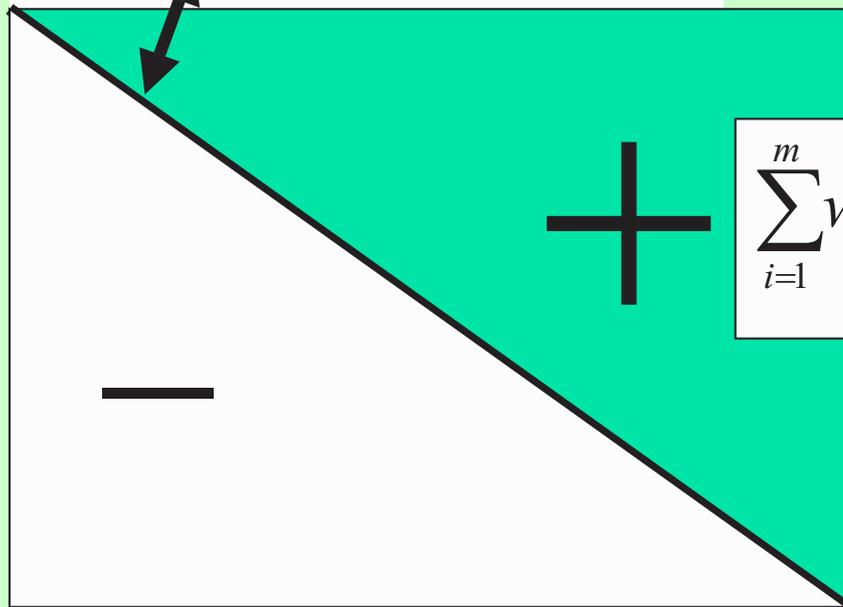
capable of solving **linearly separable problem** ?



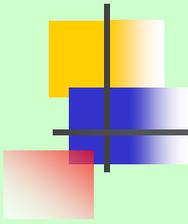
$$\sum_{i=1}^m w_i x_i + b = 0$$

$$\sum_{i=1}^m w_i x_i + b < 0$$

$$\sum_{i=1}^m w_i x_i + b > 0$$

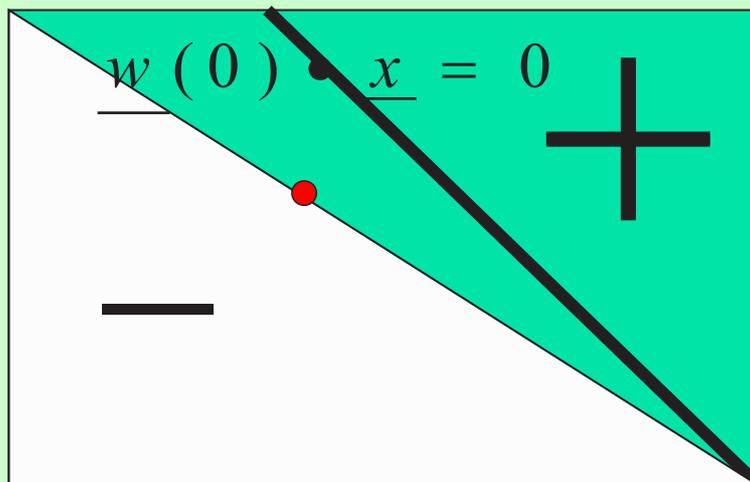


Learning rule



An algorithm to update the weights \underline{w} so that finally the input patterns lie on both sides of the line decided by the perceptron

Let t be the time, at $t = 0$, we have

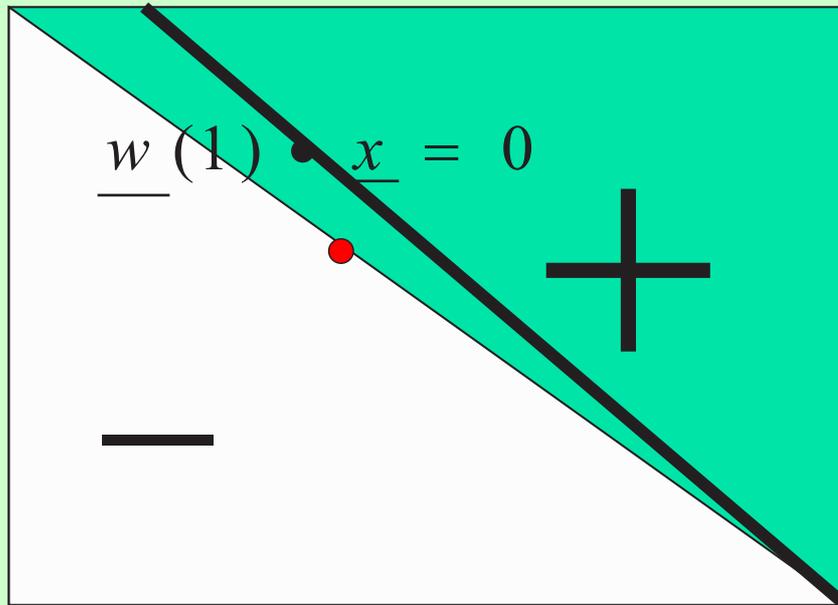


Learning rule



An algorithm to update the weights \underline{w} so that finally the input patterns lie on both sides of the line decided by the perceptron

Let t be the time, at $t = 1$

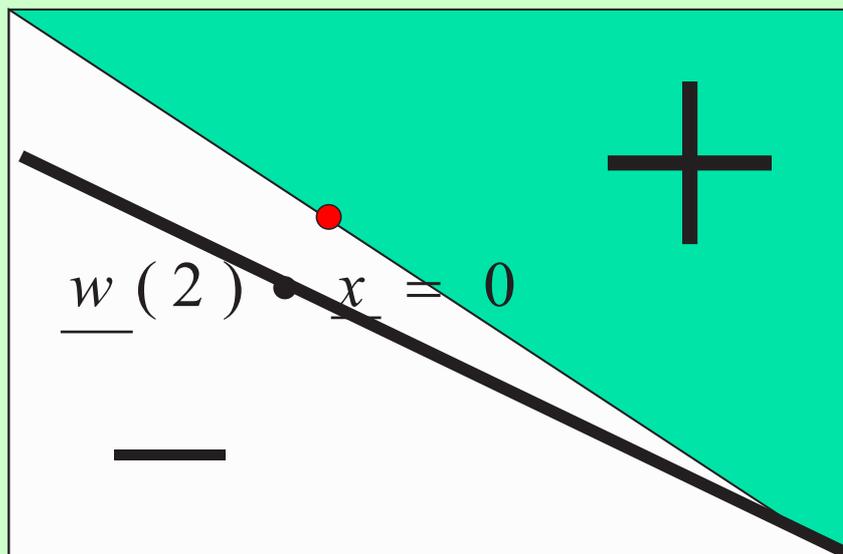


Learning rule



An algorithm to update the weights \underline{w} so that finally the input patterns lie on both sides of the line decided by the perceptron

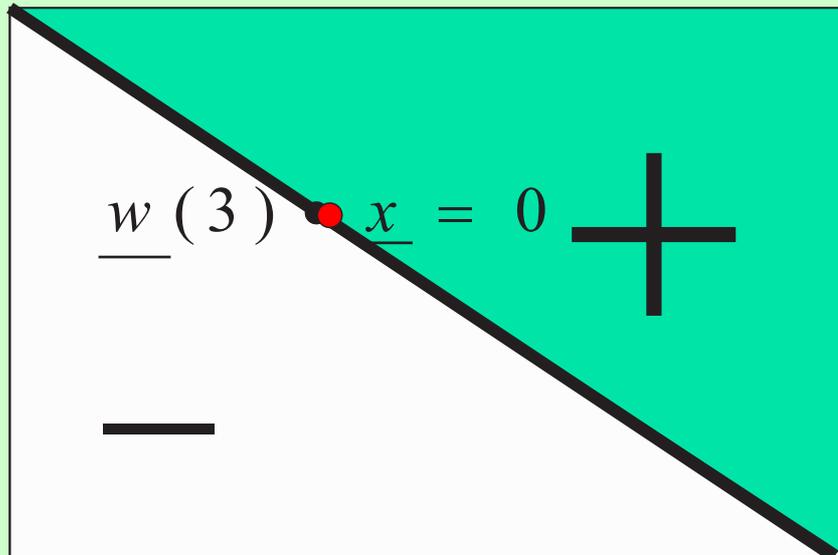
Let t be the time, at $t = 2$



Learning rule

An algorithm to update the weights \underline{w} so that finally the input patterns lie on both sides of the line decided by the perceptron

Let t be the time, at $t = 3$



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29/148

In Math

$$d(t) = \begin{cases} +1 & \text{if } x(t) \text{ in class } + \\ -1 & \text{if } x(t) \text{ in class } - \end{cases}$$

Perceptron learning rule

$$\underline{w}(t+1) = \underline{w}(t) + \eta(t) [d(t) - \text{sign}(\underline{w}(t) \cdot \underline{x}(t))] \underline{x}(t)$$

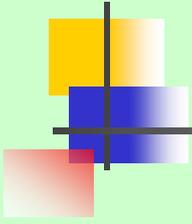
Where $\eta(t)$ is the learning rate >0 ,

$$\text{sign}(x) = \begin{cases} +1 & \text{if } x > 0 \\ -1 & \text{if } x \leq 0, \end{cases} \quad \text{hard limiter function}$$

NB : $d(t)$ is the same as $d(i)$ and $x(t)$ as $x(i)$

14/04/2009

30/148

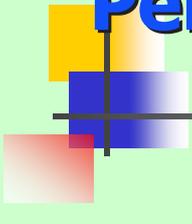


In words:

- If the classification is right, do not update the weights
- If the classification is not correct, update the weight towards the opposite direction so that the output move close to the right directions.

14/04/2009

31/148



Perceptron convergence theorem (Rosenblatt, 1962)

Let the subsets of training vectors be linearly separable. Then after finite steps of learning we have

$\lim \underline{w}(t) = \underline{w}$ which correctly separate the samples.

The idea of proof is that to consider $||\underline{w}(t+1) - \underline{w}|| - ||\underline{w}(t) - \underline{w}||$ which is a decrease function of t

14/04/2009

32/148

Summary of Perceptron learning ...

Variables and parameters

$$\underline{x}(t) = (m+1) \text{ dim. input vectors at time } t \\ = (b, x_1(t), x_2(t), \dots, x_m(t))$$

$$\underline{w}(t) = (m+1) \text{ dim. weight vectors} \\ = (1, w_1(t), \dots, w_m(t))$$

b = bias

$y(t)$ = actual response

$\eta(t)$ = learning rate parameter, a +ve constant < 1

$d(t)$ = desired response

14/04/2009

33/148

Summary of Perceptron learning ...

Data $\{ (\underline{x}(i), d(i)), i=1, \dots, p \}$

✓ Present the data to the network once a point

✓ could be cyclic :

$(\underline{x}(1), d(1)), (\underline{x}(2), d(2)), \dots, (\underline{x}(p), d(p)),$
 $(\underline{x}(p+1), d(p+1)), \dots$

✓ or randomly

(Hence we mix time t with i here)

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34/148

Summary of Perceptron learning (algorithm)

- 1. Initialisation** Set $\underline{w}(0)=0$. Then perform the following computation for time step $t=1,2,\dots$
- 2. Activation** At time step t , activate the perceptron by applying input vector $\underline{x}(t)$ and desired response $d(t)$
- 3. Computation of actual response** Compute the actual response of the perceptron

$$y(t) = \text{sign} (\underline{w}(t) \cdot \underline{x}(t))$$

where **sign** is the sign function

- 4. Adaptation of weight vector** Update the weight vector of the perceptron

$$\underline{w}(t+1) = \underline{w}(t) + \eta(t) [d(t) - y(t)] \underline{x}(t)$$

- 5. Continuation**

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35/148

Questions remain

Where or when to stop?

By minimizing the generalization error

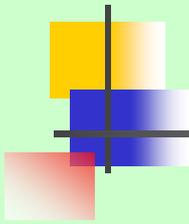
For training data $\{(\underline{x}(i), d(i)), i=1,\dots,p\}$

How to define training error after t steps of learning?

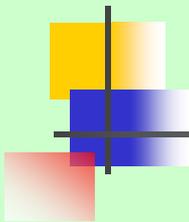
$$E(t) = \sum_{i=1}^p [d(i) - \text{sign}(\underline{w}(t) \cdot \underline{x}(i))]^2$$

14/04/2009

36/148

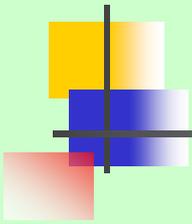


We next turn to **ADALINE learning**,
from which we can understand
the learning rule, and more general the
Back-Propagation (BP) learning



Simple Neural Network

ADALINE Learning



Outlines

- ADALINE
- Gradient descending learning
- Modes of training

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39/148



Unhappy Over Perceptron Training

- When a perceptron gives the right answer, no learning takes place
- Anything below the threshold is interpreted as **'no', even it is just below the threshold.**
- It might be better to train the neuron based on **how far below the threshold it is.**

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40/148

ADALINE

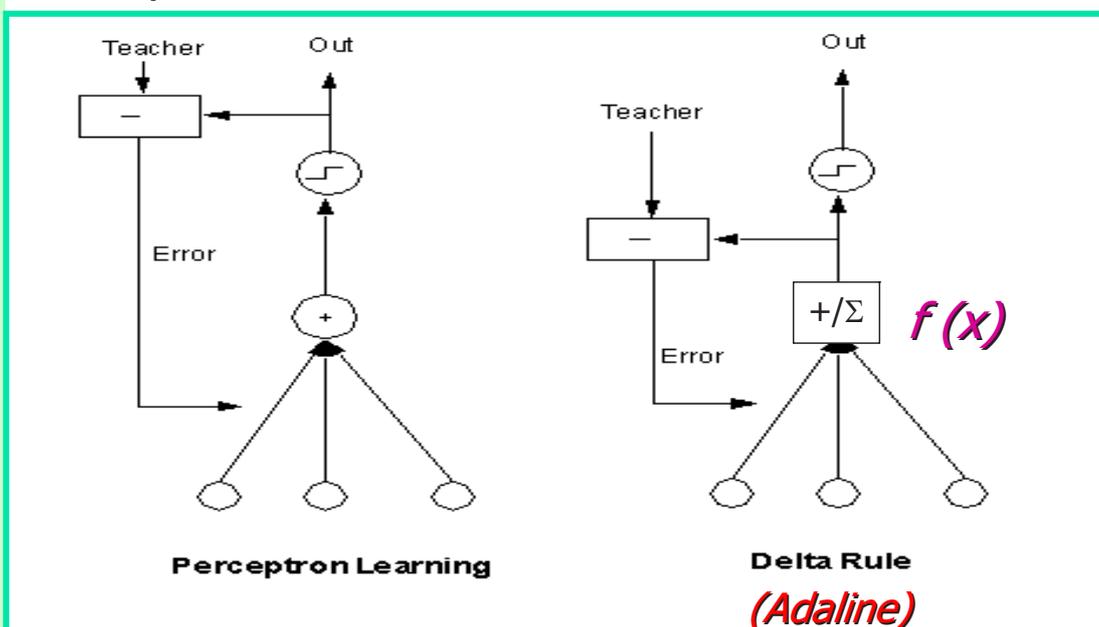
- **ADALINE** is an acronym for ADaptive LINear Element (or ADaptive LINear NEuron) developed by Bernard Widrow and Marcian Hoff (1960).
- There are several variations of Adaline. One has threshold same as perceptron and another just a bare linear function.
- The **Adaline learning** rule is also known as the least-mean-squares (LMS) rule, the delta rule, or the Widrow-Hoff rule.
- It is a training rule that minimizes the output error using (approximate) gradient descent method.

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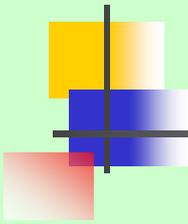
41/148

- Replace the step function in the perceptron with a **continuous (differentiable) function f** , e.g the simplest is **linear function**

- With or without the threshold, the **Adaline** is trained based on the output of the function f rather than the final output.



42/148



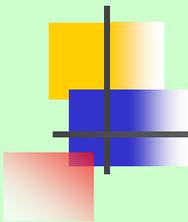
After each training pattern $\underline{x}(i)$ is presented, **the correction to apply to the weights is proportional to the error.**

$$E(i,t) = \frac{1}{2} [d(i) - f(\underline{w}(t) \cdot \underline{x}(i))]^2 \quad i=1,\dots,p$$

N.B. If f is a **linear function** $f(\underline{w}(t) \cdot \underline{x}(i)) = \underline{w}(t) \cdot \underline{x}(i)$

Summing together, our purpose is to find \underline{W} which minimizes

$$E(t) = \sum_i E(i,t)$$



General Approach gradient descent method

To find g

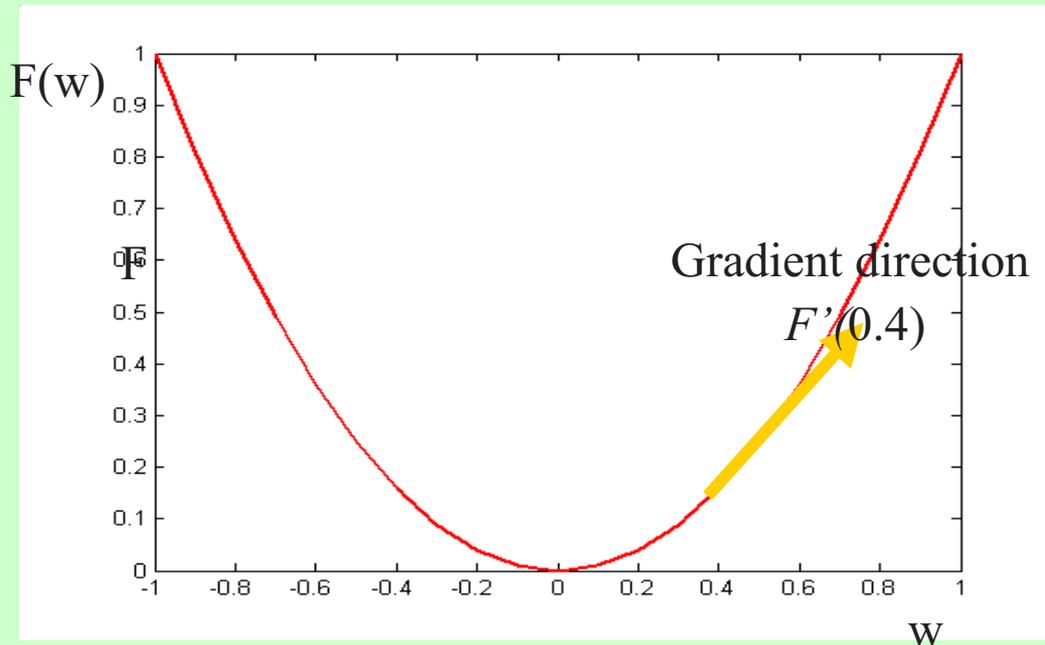
$$\underline{w}(t+1) = \underline{w}(t) + g(E(\underline{w}(t)))$$

so that \underline{w} automatically tends to the global minimum of $E(w)$.

$$\underline{w}(t+1) = \underline{w}(t) - E'(\underline{w}(t))\eta(t)$$

(see figure in the following...)

- Gradient direction is the direction of uphill
for example, in the Figure, at position 0.4, the gradient is uphill (F is E, consider one dim case)



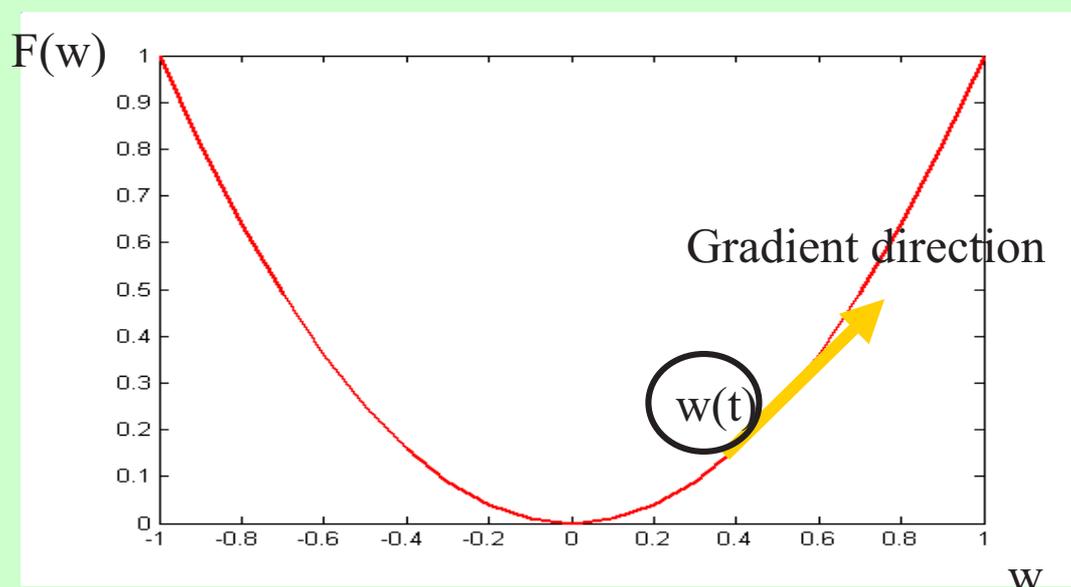
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45/148

- In gradient descent algorithm, we have

$$\underline{w}(t+1) = \underline{w}(t) - F'(w(t)) \eta(\tau)$$

therefore the ball goes downhill since $-F'(w(t))$ is downhill direction



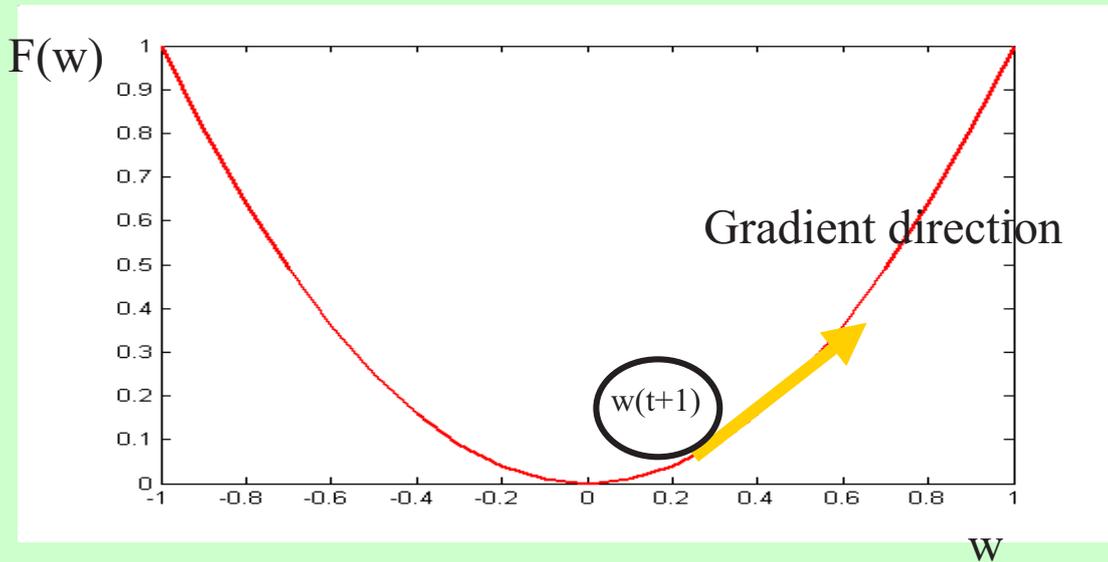
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46/148

- In gradient descent algorithm, we have

$$w(t+1) = w(t) - F'(w(t)) \eta(\tau)$$

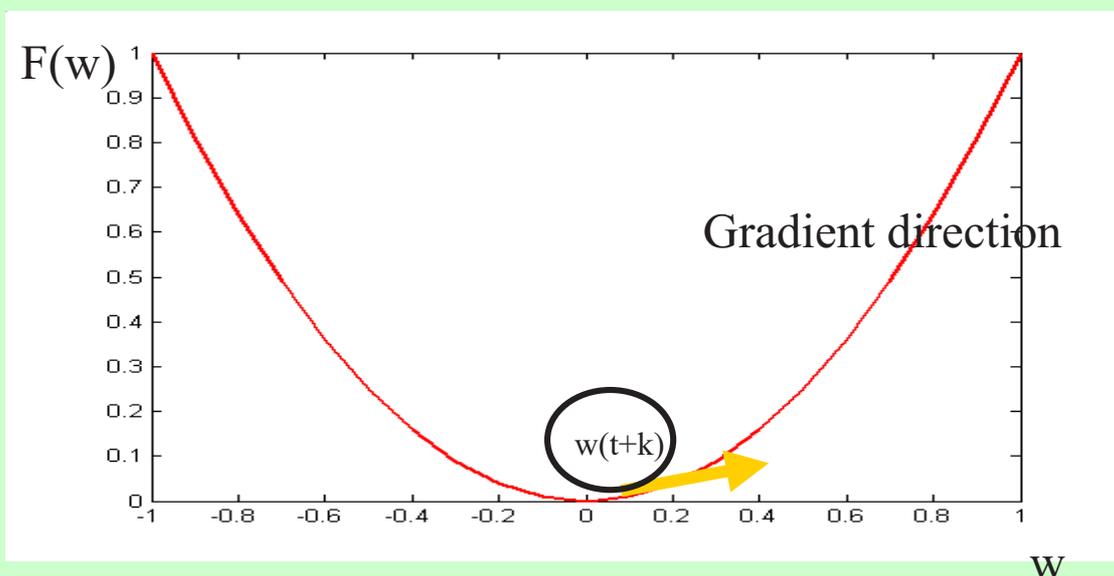
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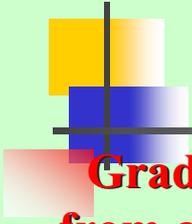
47/148

- Gradually the ball will stop at a local minima where the gradient is zero



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48/148



• In words

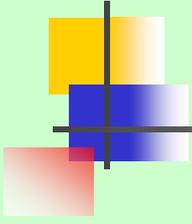
Gradient method could be thought of as a ball rolling down from a hill: the ball will roll down and finally stop at the valley

Thus, the weights are adjusted by

$$w_j(t+1) = w_j(t) + \eta(t) \sum [d(i) - f(\underline{w}(t) \cdot \underline{x}(i))] x_j(i) f'$$

This corresponds to gradient descent on the quadratic error surface E

When $f' = 1$, we have the perceptron learning rule (we have in general $f' > 0$ in neural networks). The ball moves in the right direction.



Two types of network training:

Sequential mode (on-line, stochastic, or per-pattern) :

Weights updated after each pattern is presented (Perceptron is in this class)

Batch mode (off-line or per-epoch) :

Weights updated after all patterns are presented

Comparison Perceptron and Gradient Descent Rules

- **Perceptron learning rule** guaranteed to succeed if
 - Training examples are **linearly separable**
 - Sufficiently small learning rate η
- **Linear unit training rule** uses gradient descent guaranteed to converge to hypothesis with minimum squared error given sufficiently small learning rate η
 - Even when training data contains noise
 - Even when training data **not separable by hyperplanes**

14/04/2009

51/148

Summary

Perceptron

$$\underline{W}(t+1) = \underline{W}(t) + \eta(t) [d(t) - \text{sign}(\underline{w}(t) \cdot \underline{x})] \underline{x}$$

Adaline (Gradient descent method)

$$\underline{W}(t+1) = \underline{W}(t) + \eta(t) [d(t) - f(\underline{w}(t) \cdot \underline{x})] \underline{x} f'$$

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52/148

Multi-Layer Perceptron (MLP)

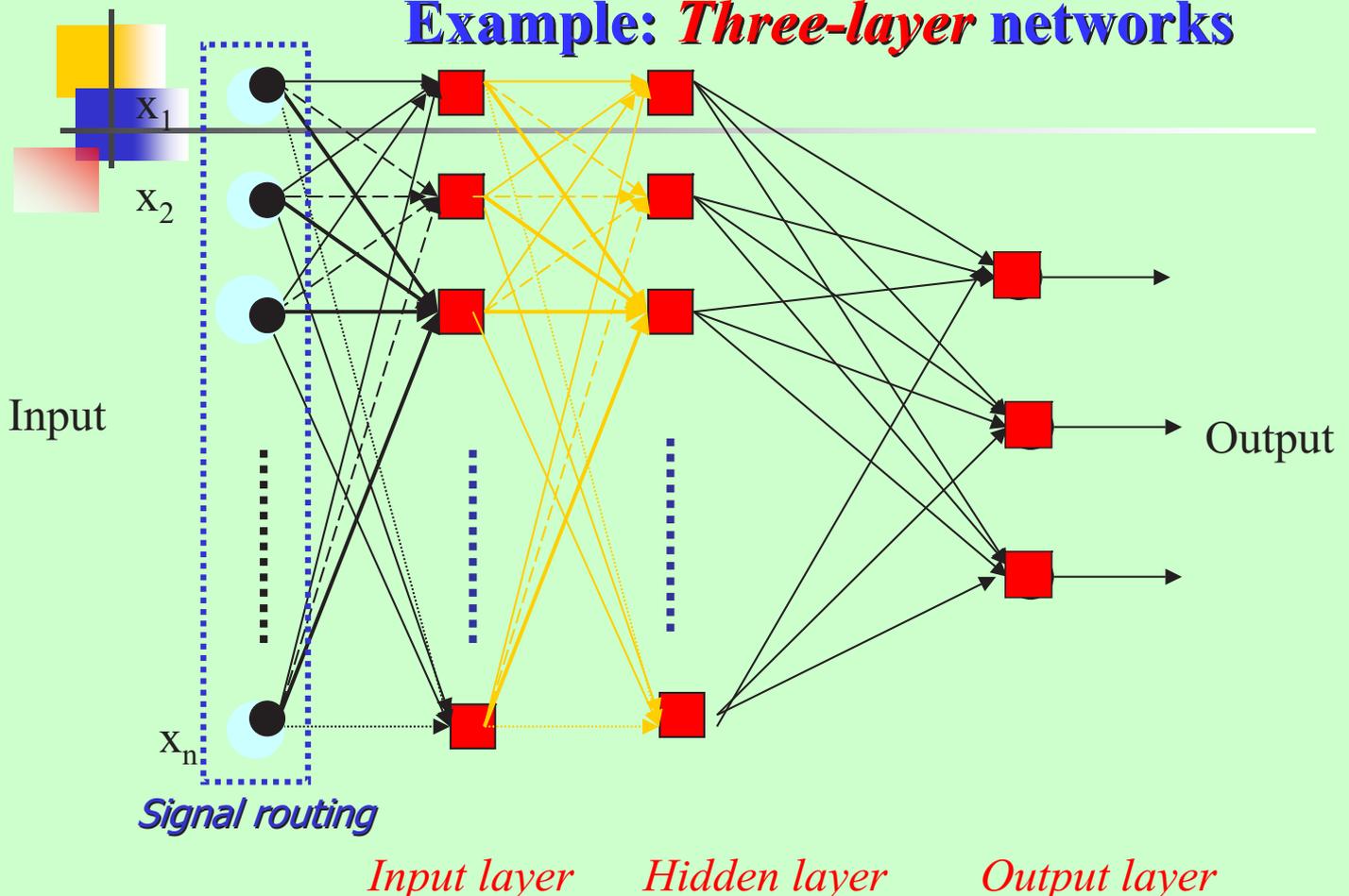
Idea: "Credit assignment problem"

- Problem of assigning 'credit' or 'blame' to individual elements involving in forming overall response of a learning system (hidden units)
- In **neural networks**, problem relates to dividing which weights should be altered, **by how much** and **in which direction**.

14/04/2009

53/148

Example: *Three-layer networks*

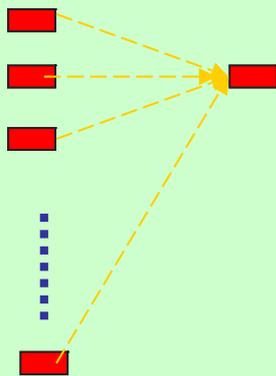


14/04/2009

54/148

Properties of architecture

- No connections within a layer
- No direct connections between input and output layers
- Fully connected between layers
- Often more than 2 layers
- Number of output units need not equal number of input units
- Number of hidden units per layer can be more or less than input or output units



Each unit '■' is a perceptron

$$y_i = f \left(\sum_{j=1}^m w_{ij} x_j + b_i \right)$$

14/04/2009

55/148

BP (Back Propagation)

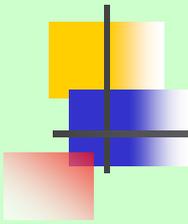
gradient descent method

+

multilayer networks

14/04/2009

56/148

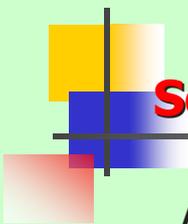


MultiLayer Perceptron I

Back Propagating Learning

14/04/2009

57/148



BP learning algorithm

Solution to "credit assignment problem" in MLP

Rumelhart, Hinton and Williams (1986)

BP has two phases:

Forward pass phase: computes 'functional signal', feedforward propagation of input pattern signals through network

Backward pass phase: computes 'error signal', propagation of error (difference between actual and desired output values) backwards through network starting at output units

14/04/2009

58/148

BP Learning for Simplest MLP_O

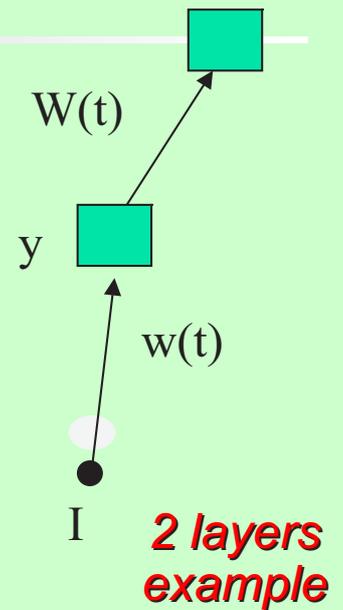
Task : Data $\{I, d\}$ to minimize

$$\begin{aligned}
 E &= (d - o)^2 / 2 \\
 &= [d - f(W(t)y(t))]^2 / 2 \\
 &= [d - f(W(t)f(w(t)I))]^2 / 2
 \end{aligned}$$

Error function at the output unit

Weight at time t is $w(t)$ and $W(t)$,
intend to find the weight w and W at time $t+1$

Where $y = f(w(t)I)$, output of the **input unit**



14/04/2009

59/148

Forward pass phase

Suppose that we have $w(t)$, $W(t)$ of time t

For given input I , we can calculate

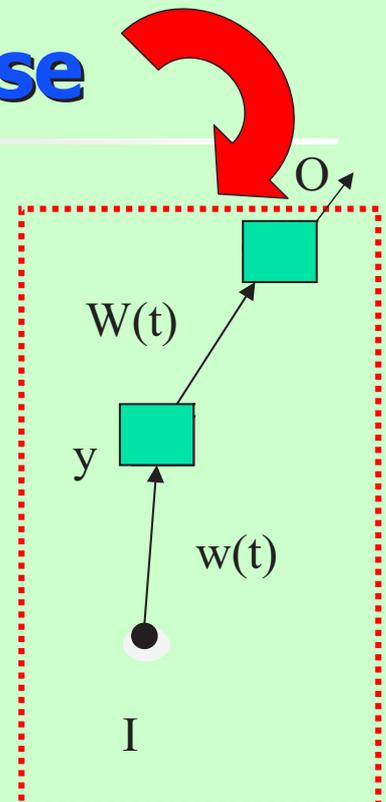
$$y = f(w(t)I)$$

and

$$\begin{aligned}
 o &= f(W(t)y) \\
 &= f(W(t)f(w(t)I))
 \end{aligned}$$

Error function of output unit will be

$$E = (d - o)^2 / 2$$

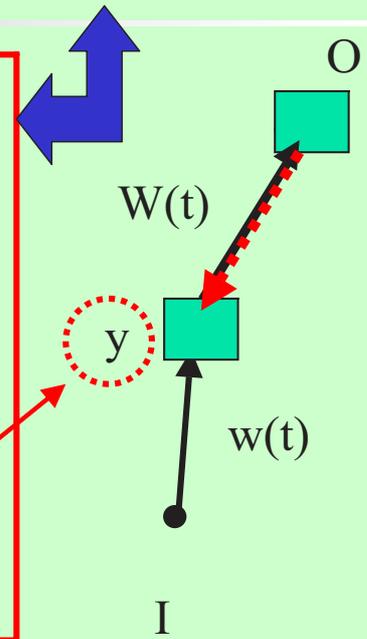


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60/148

Backward Pass Phase

$$\begin{aligned}
 W(t+1) &= W(t) - \eta \frac{dE}{dW(t)} \\
 &= W(t) - \eta \frac{dE}{df} \frac{df}{dW(t)} \\
 &= W(t) + \eta(d - o) f'(W(t)y) y
 \end{aligned}$$



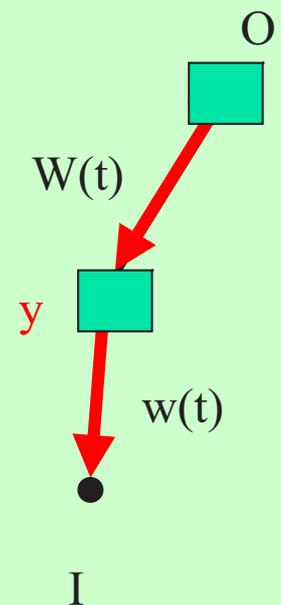
$$E = (d - o)^2 / 2 \quad o = f(W(t)y)$$

14/04/2009

61/148

Backward pass phase

$$\begin{aligned}
 W(t+1) &= W(t) - \eta \frac{dE}{dW(t)} \\
 &= W(t) - \eta \frac{dE}{df} \frac{df}{dW(t)} \\
 &= W(t) + \eta(d - o) f'(W(t)y) y \\
 &= W(t) + \eta \Delta y
 \end{aligned}$$



where $\Delta = (d - o) f'$

14/04/2009

62/148

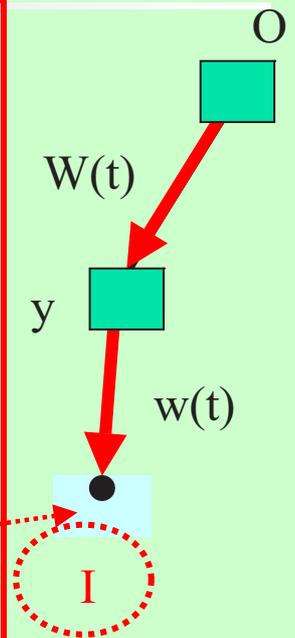
Backward pass phase

$$w(t+1) = w(t) - \eta \frac{dE}{dw(t)}$$

$$= w(t) - \eta \frac{dE}{dy} \frac{dy}{dw(t)}$$

$$= w(t) + \eta (d - o) f'(W(t)y) W(t) \frac{dy}{dw(t)}$$

$$= w(t) + \eta \Delta W(t) f'(w(t) I) I$$



$$o = f(W(t)y)$$

$$= f(W(t)f(w(t)I))$$

14/04/2009

63/148

Lecture Notes on Neural Networks and Fuzzy Systems Summary

weight updates are local

$$w_{ji}(t+1) - w_{ji}(t) = \eta \delta_j(t) I_i(t) \quad (\text{input unit})$$

$$W_{kj}(t+1) - W_{kj}(t) = \eta \Delta_k(t) y_j(t) \quad (\text{output unit})$$

output unit

$$W_{kj}(t+1) - W_{kj}(t) = \eta \Delta_k(t) y_j(t)$$

$$= \eta (d_k(t) - O_k(t)) f'(Net_k(t)) y_j(t)$$

input unit

$$w_{ji}(t+1) - w_{ji}(t) = \eta \delta_j(t) I_i(t)$$

$$= \eta f'(net_j(t)) \sum_k \Delta_k(t) W_{kj} I_i(t)$$

Once weight changes are computed for all units, weights are updated at same time (bias included as weights here)

We now compute the derivative of the activation function $f(\cdot)$.

14/04/2009

64/148

Activation Functions

- to compute δ_j and Δ_k we need to find the derivative of activation function f
- to find derivative the activation function must be smooth

Sigmoidal (logistic) function-common in MLP

$$f(\text{net}_i(t)) = \frac{1}{1 + \exp(-k \text{net}_i(t))}$$

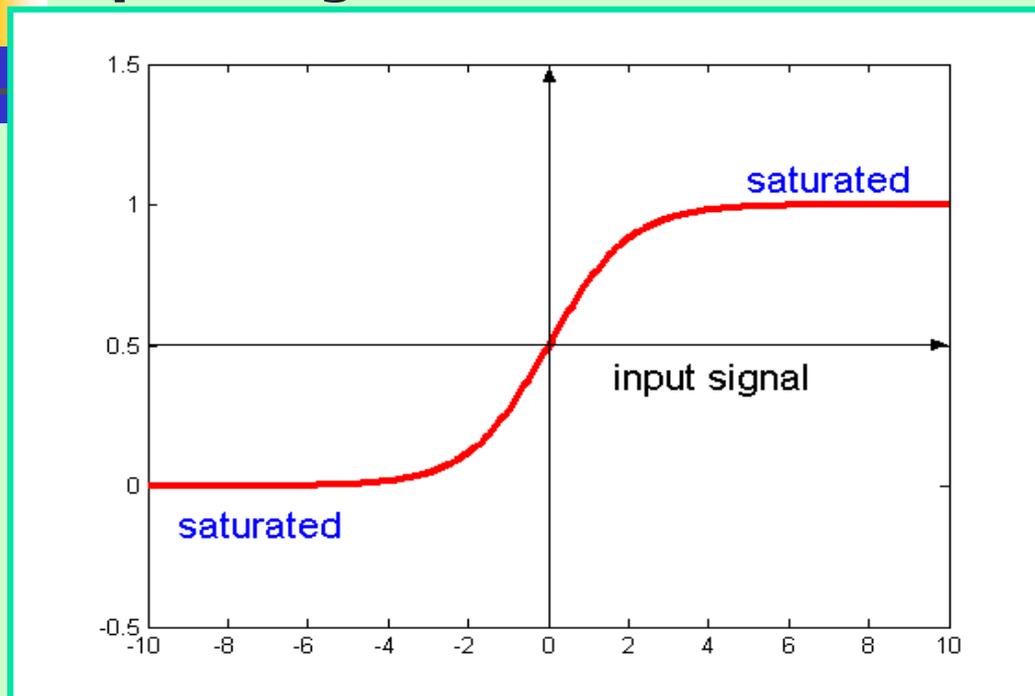
where k is a positive constant. The sigmoidal function gives value in range of 0 to 1

Input-output function of a neuron (rate coding assumption)

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65/148

Shape of sigmoidal function

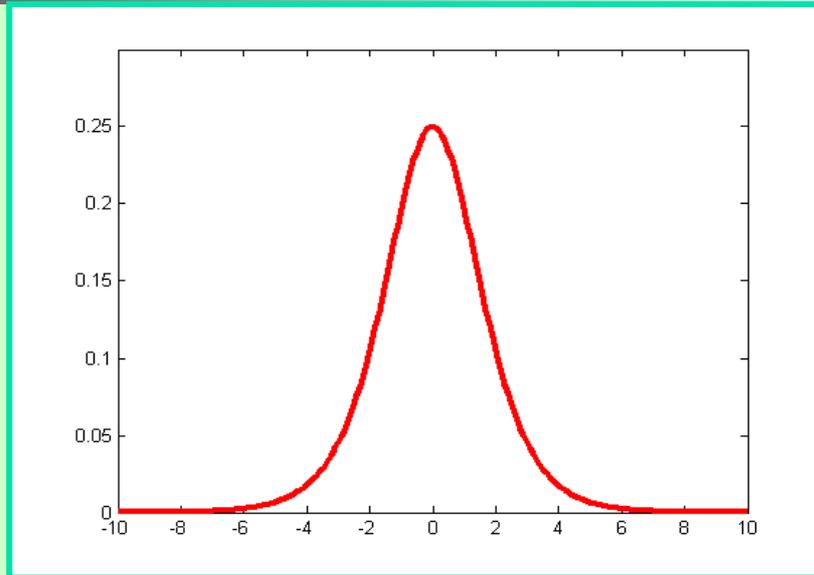


Note: when $\text{net} = 0$, $f = 0.5$

14/04/2009

66/148

Shape of sigmoidal function derivative



Derivative of sigmoidal function has max at $x=0$, is symmetric about this point falling to zero as sigmoidal approaches extreme values

14/04/2009

67/148

Returning to **local error gradients** in BP algorithm we have for **output units**

$$\begin{aligned}\Delta_i(t) &= (d_i(t) - O_i(t)) f'(Net_i(t)) \\ &= (d_i(t) - O_i(t)) kO_i(t)(1 - O_i(t))\end{aligned}$$

For **input units** we have

$$\begin{aligned}\delta_i(t) &= f'(net_i(t)) \sum_k \Delta_k(t) W_{ki} \\ &= ky_i(t)(1 - y_i(t)) \sum_k \Delta_k(t) W_{ki}\end{aligned}$$

Since degree of weight change is **proportional to derivative of activation function**, weight changes will be greatest when units receives mid-range functional signal than at extremes

14/04/2009

68/148

Network training:

- ❖ Training set shown repeatedly until stopping criteria are met
- ❖ Each full presentation of all patterns = 'epoch'
- ❖ Randomise order of training patterns presented for each epoch in order to avoid correlation between consecutive training pairs being learnt (order effects)

Two types of network training:

- **Sequential mode** (on-line, stochastic, or per-pattern)
Weights updated after each pattern is presented
- **Batch mode** (off-line or per -epoch)

14/04/2009

69/148

Advantages and disadvantages of different modes

Sequential mode:

- Less storage for each weighted connection
- Random order of presentation and updating per pattern means search of weight space is stochastic-reducing risk of local minima able to take advantage of any redundancy in training set (*i.e.* same pattern occurs more than once in training set, esp. for large training sets)
- Simpler to implement

Batch mode:

- Faster learning than sequential mode

14/04/2009

70/148

MultiLayer Perceptron II

Dynamics of MultiLayer Perceptron

Lecture No. 10: Summary of Network Training by Dr. G. S. To Simani

Summary of Network Training

Forward phase: $\underline{I}(t), \underline{w}(t), \underline{net}(t), \underline{y}(t), \underline{W}(t), \underline{Net}(t), \underline{O}(t)$

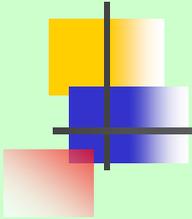
Backward phase:

Output unit

$$\begin{aligned} W_{kj}(t+1) - W_{kj}(t) &= \eta \Delta_k(t) y_j(t) \\ &= \eta (d_k(t) - O_k(t)) f'(Net_k(t)) y_j(t) \end{aligned}$$

Input unit

$$\begin{aligned} w_{ji}(t+1) - w_{ij}(t) &= \eta \delta_j(t) I_i(t) \\ &= \eta f'(net_j(t)) \sum_k \Delta_k(t) W_{kj}(t) I_i(t) \end{aligned}$$



Network training:

Training set shown repeatedly until stopping criteria are met.

Possible convergence criteria are

- Euclidean norm of the gradient vector reaches a sufficiently small denoted as θ .
- When the absolute rate of change in the average squared error per epoch is sufficiently small denoted as θ .
- **Validation** for generalization performance : stop when generalization reaching the peak (illustrate in this lecture)

14/04/2009

73/148



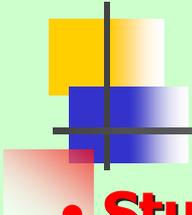
Goals of Neural Network Training

To give the correct output for input training vector (**Learning**)

To give good responses to new unseen input patterns (**Generalization**)

14/04/2009

74/148



Training and Testing Problems

- **Stuck neurons:** Degree of weight change is proportional to derivative of activation function, weight changes will be greatest when units receives mid-range functional signal than at extremes neuron. To avoid stuck neurons weights initialization should give outputs of all neurons approximate 0.5
- **Insufficient number of training patterns:** In this case, the training patterns will be learnt instead of the underlying relationship between inputs and output, i.e. network just memorizing the patterns.
- **Too few hidden neurons:** network will not produce a good model of the problem.
- **Over-fitting:** the training patterns will be learnt instead of the underlying function between inputs and output because of too many of hidden neurons. This means that the network will have a poor generalization capability.

14/04/2009

75/148



Dynamics of BP learning

Aim is to minimise an error function over all training patterns by adapting weights in MLP

Recalling the typical error function is the mean squared error as follows

$$E(t) = \frac{1}{2} \sum_{k=1}^p (d_k(t) - O_k(t))^2$$

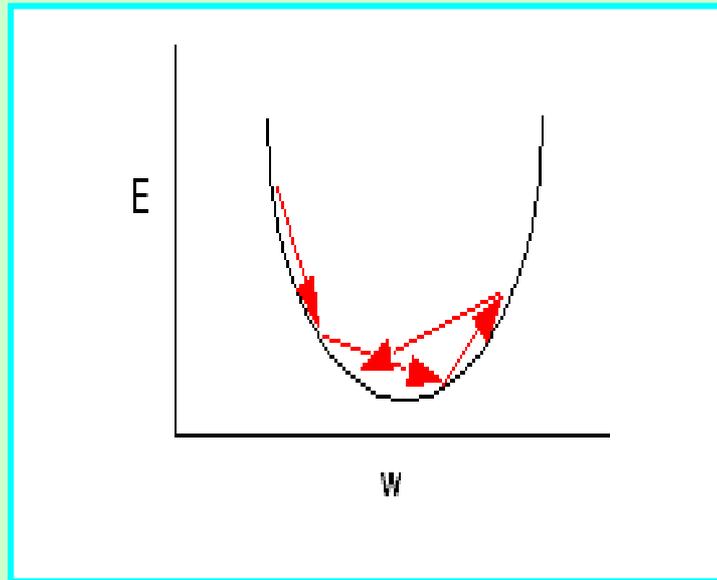
The idea is to reduce $E(t)$ to global minimum point.

14/04/2009

76/148

Dynamics of BP learning

In **single layer perceptron** with linear activation functions, the error function is simple, described by a smooth parabolic surface with a single minimum

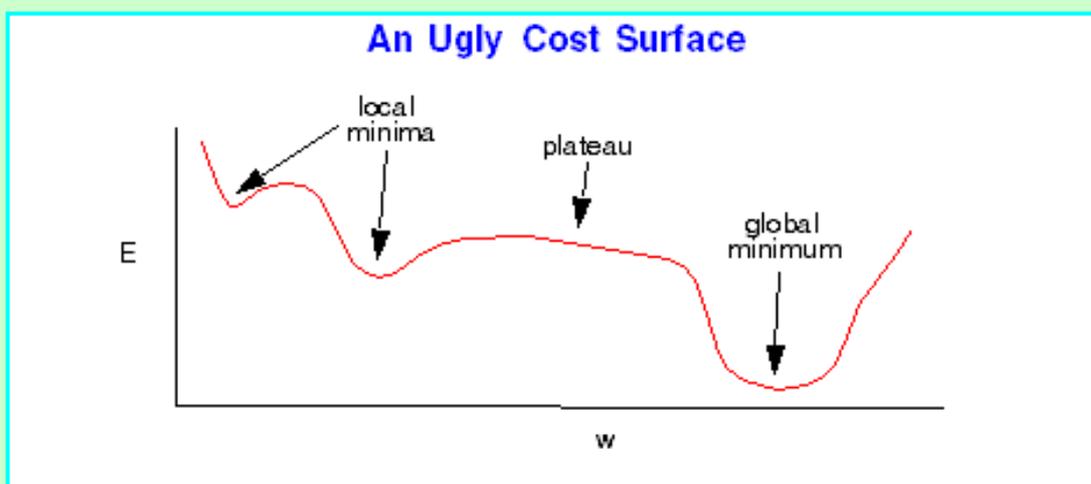


14/04/2009

77/148

Dynamics of BP learning

MLP with non-linear activation functions have complex error surfaces (e.g. plateaus, long valleys etc.) with no single minimum



For complex error surfaces the problem is learning rate must keep small to prevent divergence. **Adding momentum term is a simple approach dealing with this problem.**

14/04/2009

78/148

Momentum

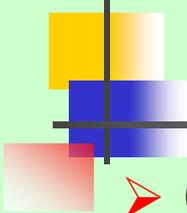
- Reducing problems of instability while increasing the rate of convergence
- Adding term to weight update equation can effectively holds as exponentially weight history of previous weights changed

Modified weight update equation is

$$w_{ij}(n+1) - w_{ij}(n) = \eta \delta_j(n) y_i(n) + \alpha [w_{ij}(n) - w_{ij}(n-1)]$$

Effect of momentum term

- If weight changes tend to have same sign, momentum term increases and gradient decrease **speed up** convergence on shallow gradient
- If weight changes tend to have opposing signs, momentum term decreases and gradient descent **slows** to reduce oscillations (stabilizes)
- Can help escape being trapped in local minima

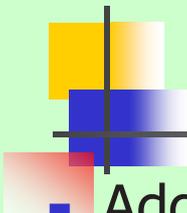


Selecting Initial Weight Values

- Choice of initial weight values is important as this decides starting position in weight space. That is, how far away from global minimum
- Aim is to select weight values which **produce midrange function signals**
- Select weight values randomly from uniform probability distribution
- Normalise weight values so number of weighted connections per unit produces **midrange function signal**

14/04/2009

81/148



Convergence of Backprop

Avoid local minimum with fast convergence:

- Add momentum
- Stochastic gradient descent
- Train multiple nets with different initial weights

Nature of convergence

- Initialize weights 'near zero' or initial networks near-linear
- Increasingly non-linear functions possible as training progresses

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82/148

Use of Available Data Set for Training

The available data set is normally split into three sets as follows:

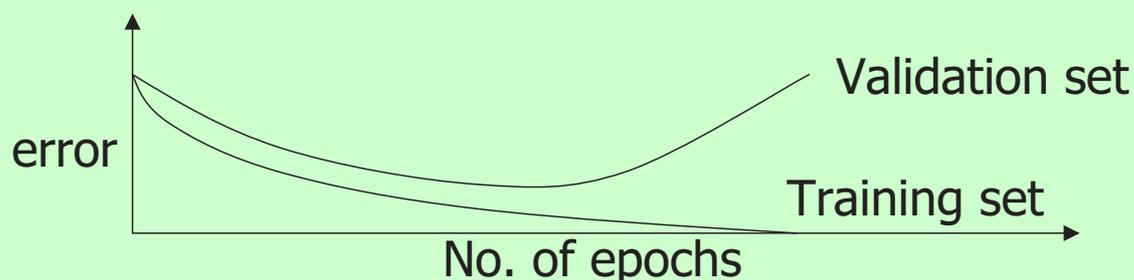
- **Training set** – use to update the weights. Patterns in this set are repeatedly in random order. The weight update equation are applied after a certain number of patterns.
- **Validation set** – use to decide when to stop training only by monitoring the error.
- **Test set** – Use to test the performance of the neural network. It should not be used as part of the neural network development cycle.

14/04/2009

83/148

Earlier Stopping - Good Generalization

- Running too many epochs may **overtrain** the network and result in **overfitting** and perform poorly in generalization.
- Keep a hold-out validation set and test accuracy after every epoch. Maintain weights for best performing network on the validation set and stop training when error increases beyond this.

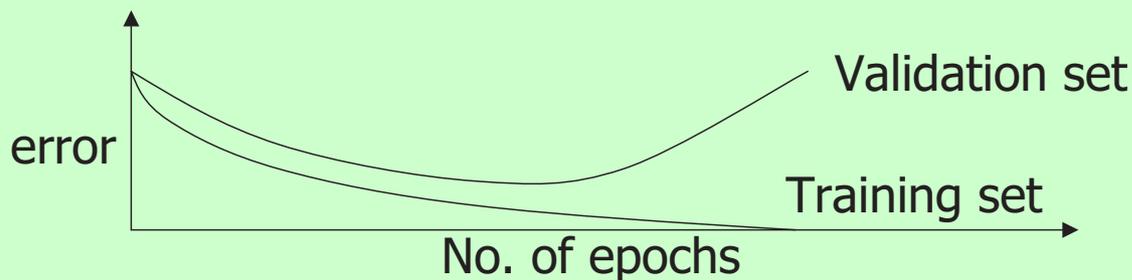


14/04/2009

84/148

Model Selection by Cross-validation

- **Too few hidden units** prevent the network from learning adequately fitting the data and learning the concept (**more than two layer networks**).
- **Too many hidden units** leads to overfitting.
- Similar **cross-validation methods** can be used to determine an appropriate number of hidden units by using the optimal test error to select the model with optimal number of hidden layers and nodes.



14/04/2009

85/148

Alternative Training Algorithm

Genetic Algorithms

History Background

- Idea of evolutionary computing was introduced in the 1960s by I. **Rechenberg** in his work "*Evolution strategies*" (*Evolutionsstrategie* in original). His idea was then developed by other researchers. **Genetic Algorithms** (GAs) were invented by John **Holland** and developed by him and his students and colleagues. This led to Holland's book "*Adaption in Natural and Artificial Systems*" published in 1975.
- In 1992 John **Koza** has used **genetic algorithm to evolve programs** to perform certain tasks. He called his method "**Genetic Programming**" (GP). LISP programs were used, because programs in this language can be expressed in the form of a "parse tree", which is the object the GA works

On 14/04/2009

87/148

Biological Background

Chromosome.

- All living organisms consist of cells. In each cell there is the same set of **chromosomes**. Chromosomes are strings of **DNA** and serve as a model for the whole organism. **A chromosome consists of genes, blocks of DNA**. Each gene encodes a particular protein. Basically can be said, that each gene encodes a **trait**, for example color of eyes. Possible settings for a trait (e.g. blue, brown) are called **alleles**. Each gene has its own position in the chromosome. This position is called **locus**.
- Complete set of genetic material (all chromosomes) is called genome**. Particular set of genes in genome is called **genotype**. The genotype is with later development after birth base for the organism's **phenotype**, its physical and mental characteristics, such as eye color, intelligence etc.

14/04/2009

88/148

Biological Background

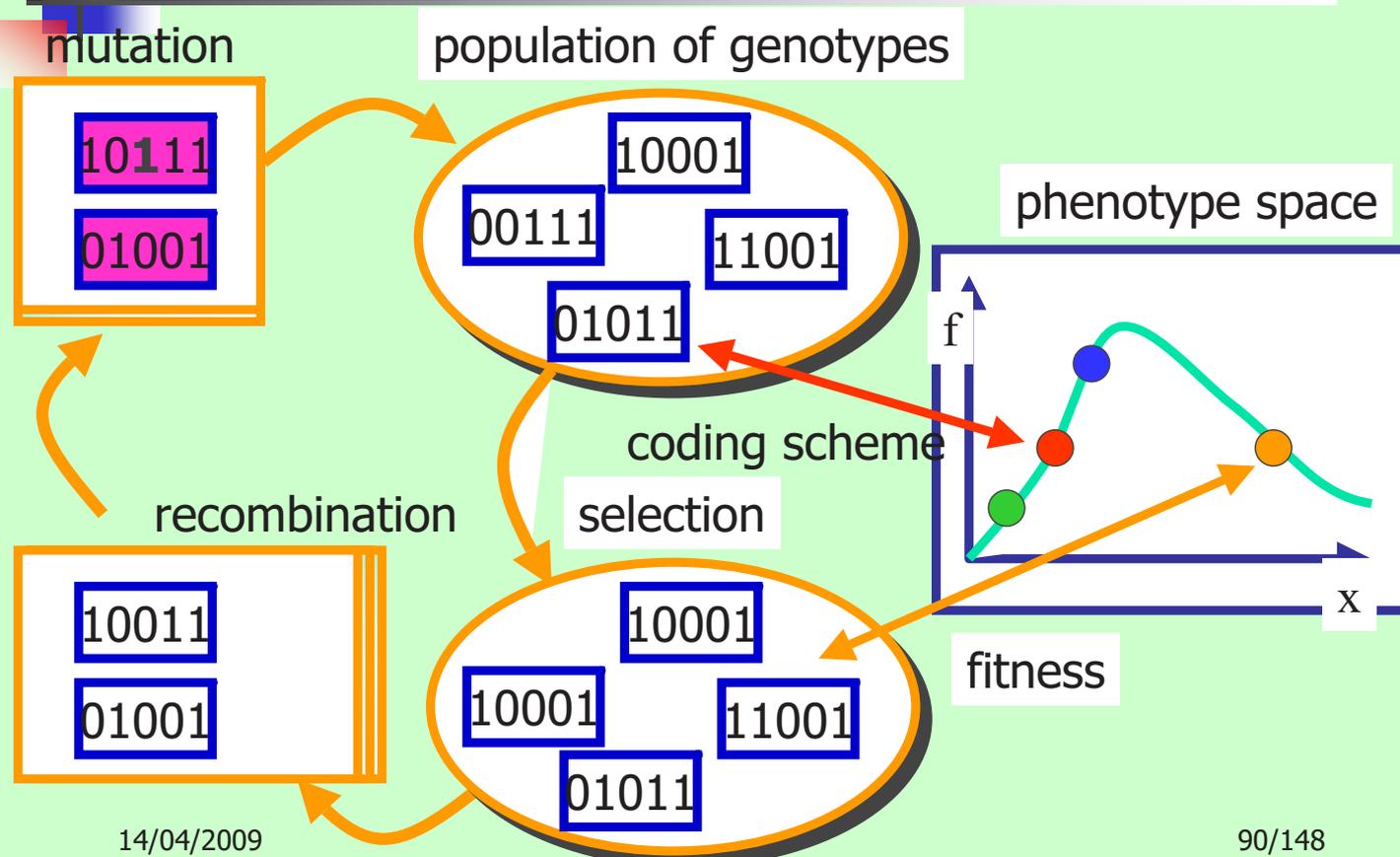
Reproduction.

- During reproduction, first occurs **recombination** (or **crossover**). Genes from parents form in some way the whole new chromosome. The new created offspring can then be mutated. **Mutation** means, that the elements of DNA are a bit changed. This changes are mainly caused by errors in copying genes from parents.
- The **fitness** of an organism is measured by **success of the organism in its life**.

14/04/2009

89/148

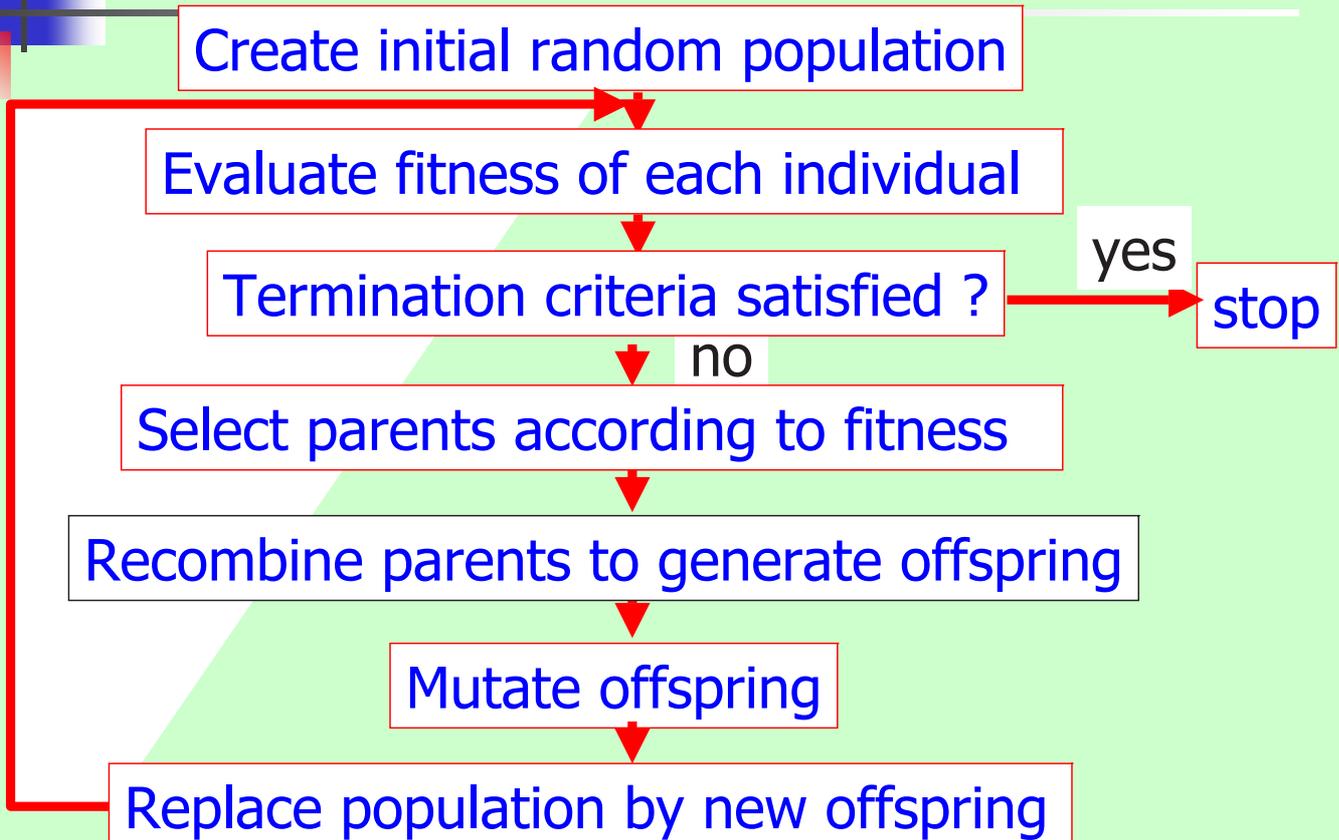
Evolutionary Algorithms



14/04/2009

90/148

Pseudo Code of an Evolutionary Algorithm



14/04/2009

91/148

A Simple Genetic Algorithm

➤ **Optimization task** : find the maximum of $f(x)$

for example $f(x) = x \cdot \sin(x)$ $x \in [0, \pi]$

• **genotype**: binary string $s \in [0, 1]^5$ e.g. 11010, 01011, 10001

• mapping : **genotype** \Rightarrow **phenotype** $n=5$

binary integer encoding: $x = \pi \cdot \sum_{i=1}^{n=5} s_i \cdot 2^{n-i-1} / (2^n - 1)$

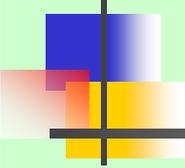
Initial population

genotype	integ.	phenotype	fitness	prop. fitness
11010	26	2.6349	1.2787	30%
01011	11	1.1148	1.0008	24%
10001	17	1.7228	1.7029	40%
00101	5	0.5067	0.2459	6%

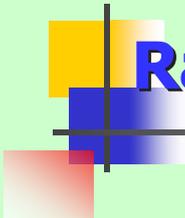
14/04/2009

92/148

Radial Basis Functions



Radial Basis Functions Overview



Radial-basis function (RBF) networks

- **RBF = radial-basis function**
- **a function which depends only on the radial distance from a point**

Radial-basis function (RBF) networks

So RBFs are functions taking the form

$$\phi (\| \underline{x} - \underline{x}_i \|)$$

where ϕ is a non-linear activation function, \underline{x} is the input and \underline{x}_i is the i 'th position, prototype, *basis* or *centre vector*.

The idea is that points near the centres will have similar outputs (i.e. if $\underline{x} \sim \underline{x}_i$ then $f(\underline{x}) \sim f(\underline{x}_i)$) since they should have similar properties.

The simplest is the linear RBF : $\phi(x) = ||\underline{x} - \underline{x}_i||$

Typical RBFs include

(a) Multi-quadrics

$$\phi (r) = (r^2 + c^2)^{1/2}$$

for some $c > 0$

(b) Inverse multi-quadrics

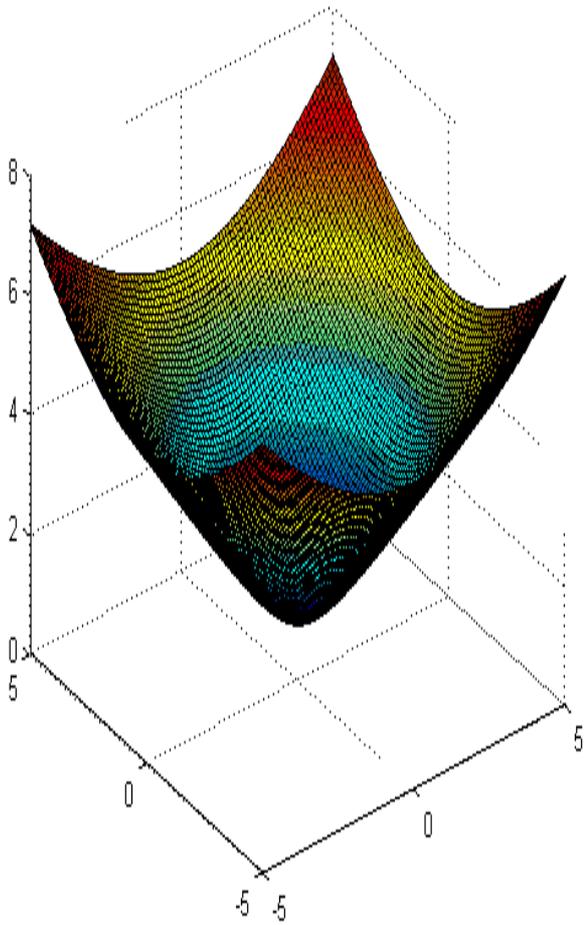
$$\phi (r) = (r^2 + c^2)^{-1/2}$$

for some $c > 0$

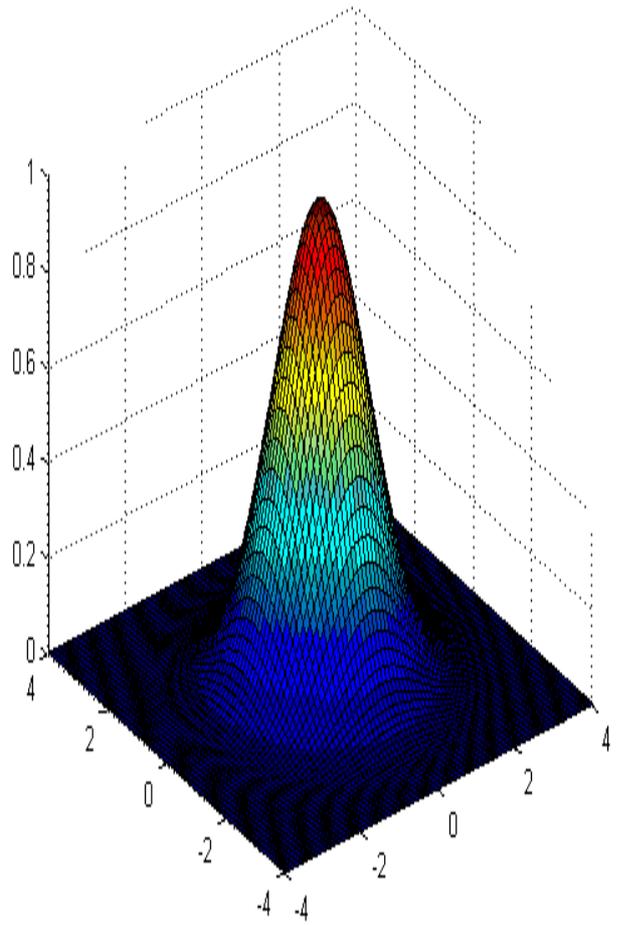
(c) Gaussian

$$\phi(r) = \exp\left(-\frac{r^2}{2\sigma^2}\right)$$

for some $\sigma > 0$

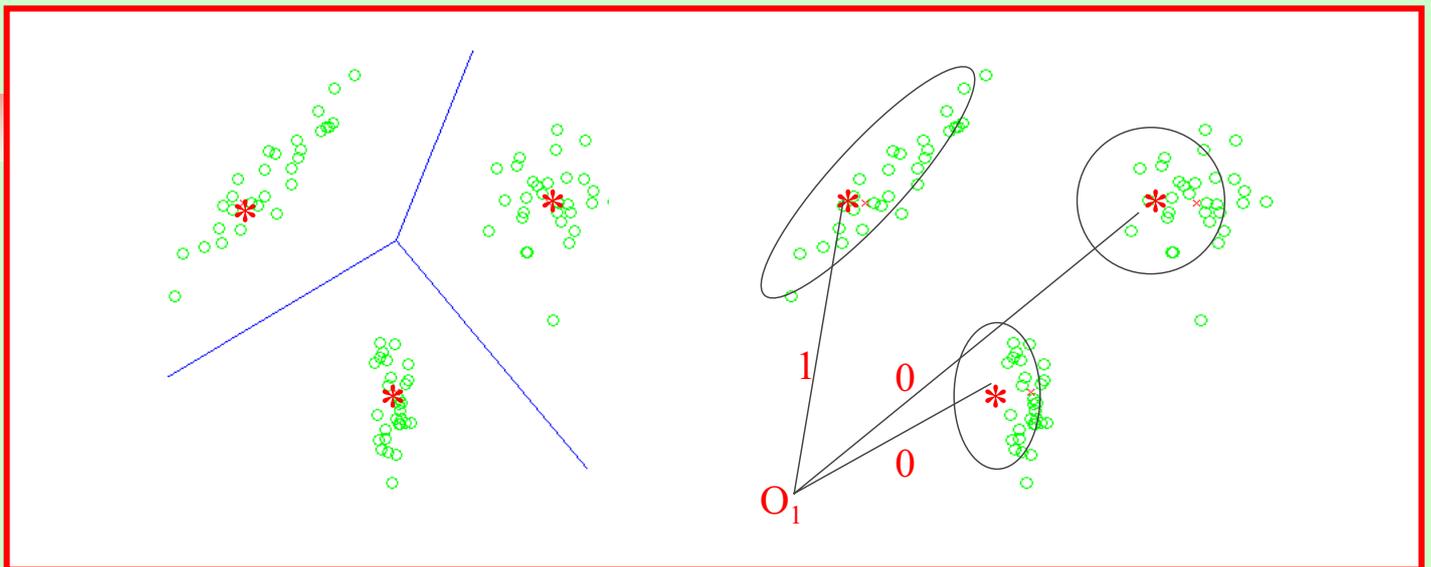


'nonlocalized' functions



'localized' functions

- Idea is to use a weighted sum of the outputs from the basis functions to represent the data.
- Thus centers can be thought of as prototypes of input data.



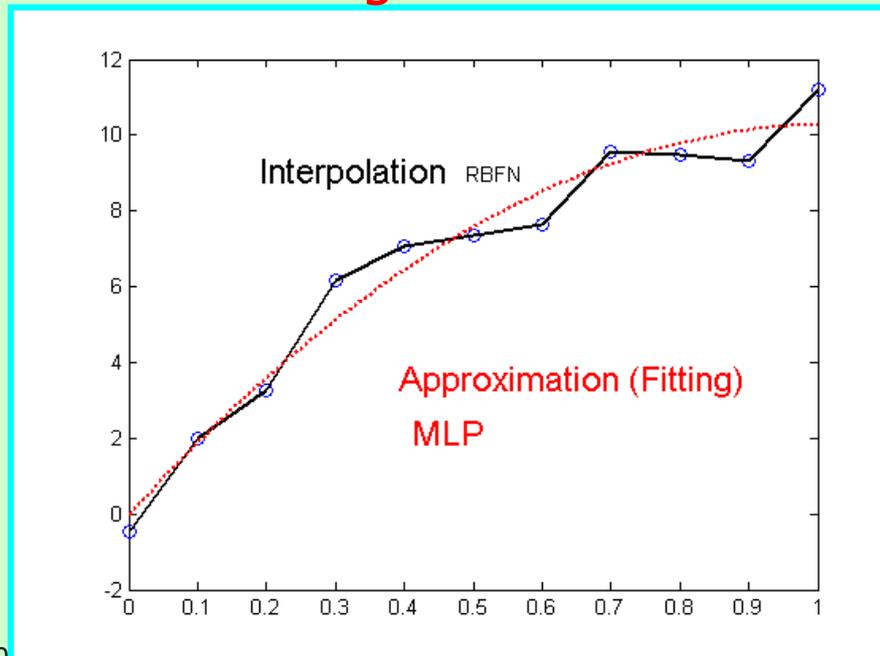
MLP
distributed

vs

RBF
local

Starting point: exact interpolation

Each input pattern x must be mapped onto a target value d



14/04/2009

99/148

That is, given a set of N vectors \underline{x}_i and a corresponding set of N real numbers, d_i (the targets), find a function F that satisfies the interpolation condition:

$$F(\underline{x}_i) = d_i \quad \text{for } i = 1, \dots, N$$

or more exactly find:

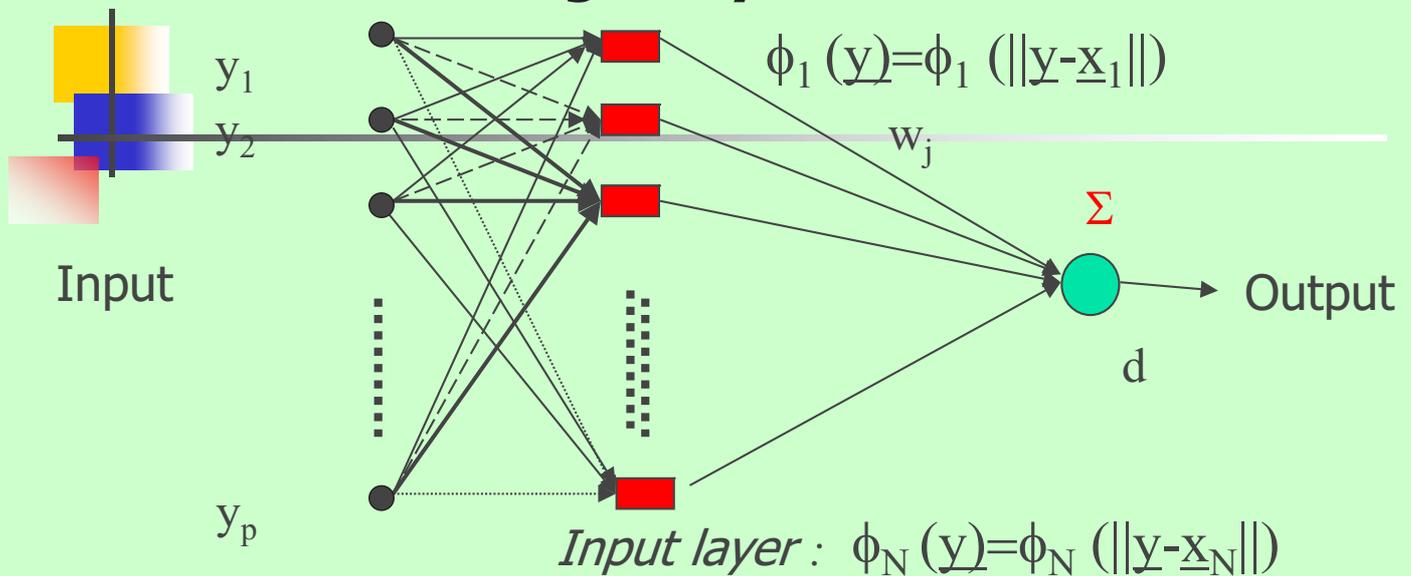
$$F(\underline{x}) = \sum_{j=1}^N w_j \phi(\|\underline{x} - \underline{x}_j\|)$$

satisfying:

$$F(\underline{x}_i) = \sum_{j=1}^N w_j \phi(\|\underline{x}_i - \underline{x}_j\|) = d_i$$

14/04/2009

100/148



- output = $\sum w_i \phi_i(\underline{y} - \underline{x}_i)$
- adjustable parameters are weights w_j
- number of **input units** \leq number of data points
- Form of the basis functions decided in advance

14/04/2009

101/148

To summarize:

- ❖ For a given data set containing N points (\underline{x}_i, d_i) , $i=1, \dots, N$
- ❖ Choose a RBF function ϕ
- ❖ Calculate $\phi(\underline{x}_j - \underline{x}_i)$
- ❖ Solve the linear equation $\Phi \underline{W} = \underline{D}$
- ❖ Get the unique solution
- ❖ Done

➤ Like MLP's, RBFNs can be shown to be able to approximate any function to arbitrary accuracy (using an arbitrarily large numbers of basis functions).

➤ Unlike MLP's, however, they have the property of 'best approximation' i.e. there exists an RBFN with minimum approximation error.

14/04/2009

102/148

Problems with exact interpolation

can produce poor generalisation performance as only data points constrain mapping

Overfitting problem

Bishop(1995) example

Underlying function $f(x)=0.5+0.4\text{sine}(2\pi x)$
sampled randomly for 30 points

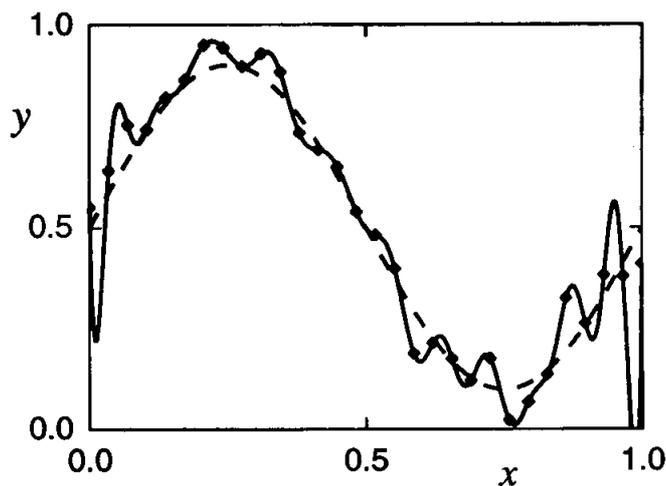
added Gaussian noise to each data point

30 data points 30 hidden RBF units

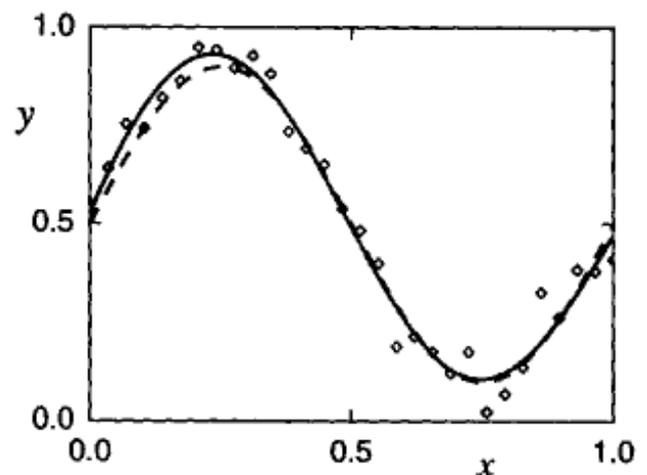
fits all data points but creates oscillations due added noise
and unconstrained between data points

14/04/2009

103/148



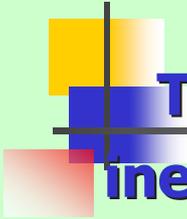
All Data Points



5 Basis functions

14/04/2009

104/148

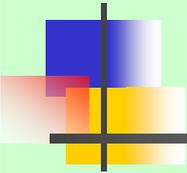


To fit an RBF to every data point is very inefficient due to the computational cost of matrix inversion and is very bad for generalization so:

- ✓ Use less RBF's than data points, *i.e.* $M < N$
- ✓ Therefore don't necessarily have RBFs centred at data points
- ✓ Can include bias terms
- ✓ Can have Gaussian with general covariance matrices but there is a trade-off between complexity and the number of parameters to be found eg for d rbf's we have:

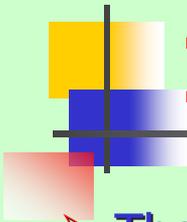
14/04/2009

105/148



Fuzzy Modelling and Identification

Fuzzy Clustering with Application to Data-Driven Modelling

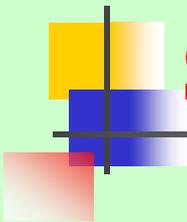


Introduction

- The ability to cluster data (concepts, perceptions, etc.)
 - essential feature of human intelligence.
- A cluster is a set of objects that are more similar to each other than to objects from other clusters.
- Applications of clustering techniques in pattern recognition and image processing.
- Some machine-learning techniques are based on the notion of similarity (decision trees, case-based reasoning)
- Non-linear regression and black-box modelling can be based on the partitioning data into clusters.

14/04/2009

107/148



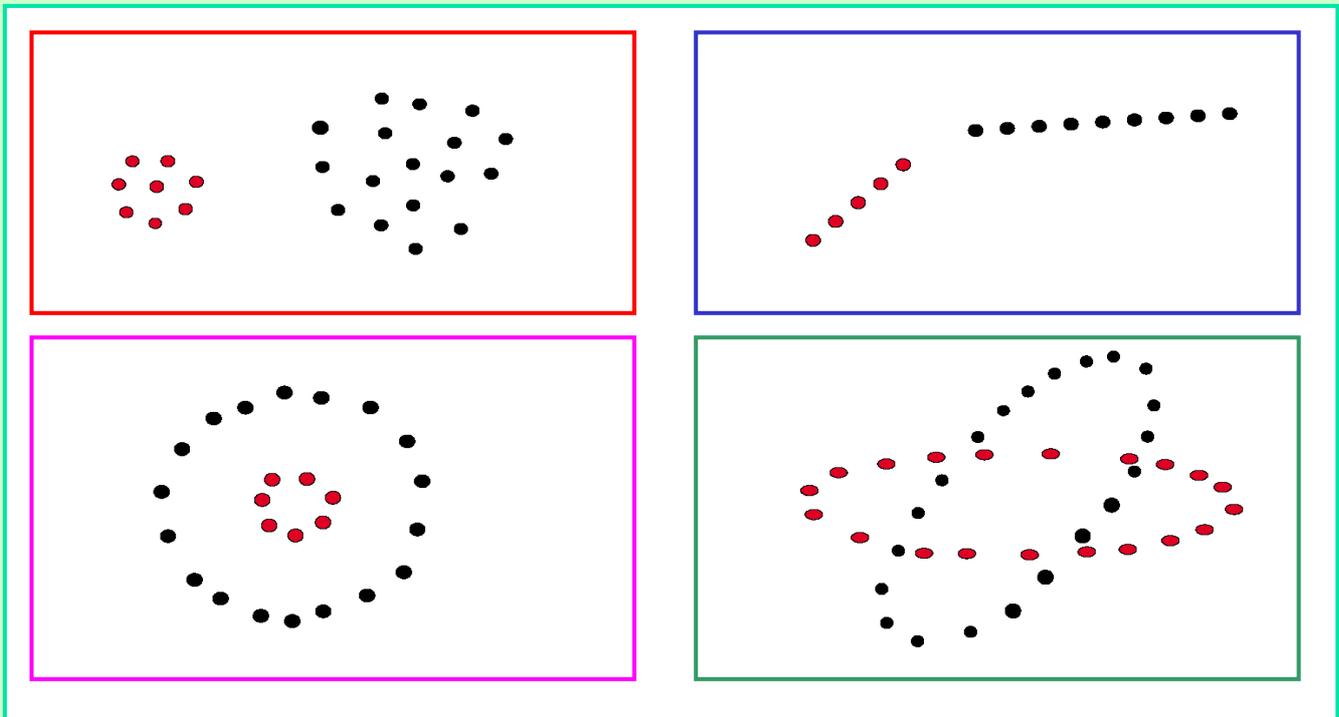
Section Outline

- **Basic concepts in clustering**
 - data set
 - partition matrix
 - distance measures
- **Clustering algorithms**
 - fuzzy c-means
 - Gustafson–Kessel
- **Application examples**
 - system identification and modelling
 - diagnosis

14/04/2009

108/148

Examples of Clusters



14/04/2009

109/148

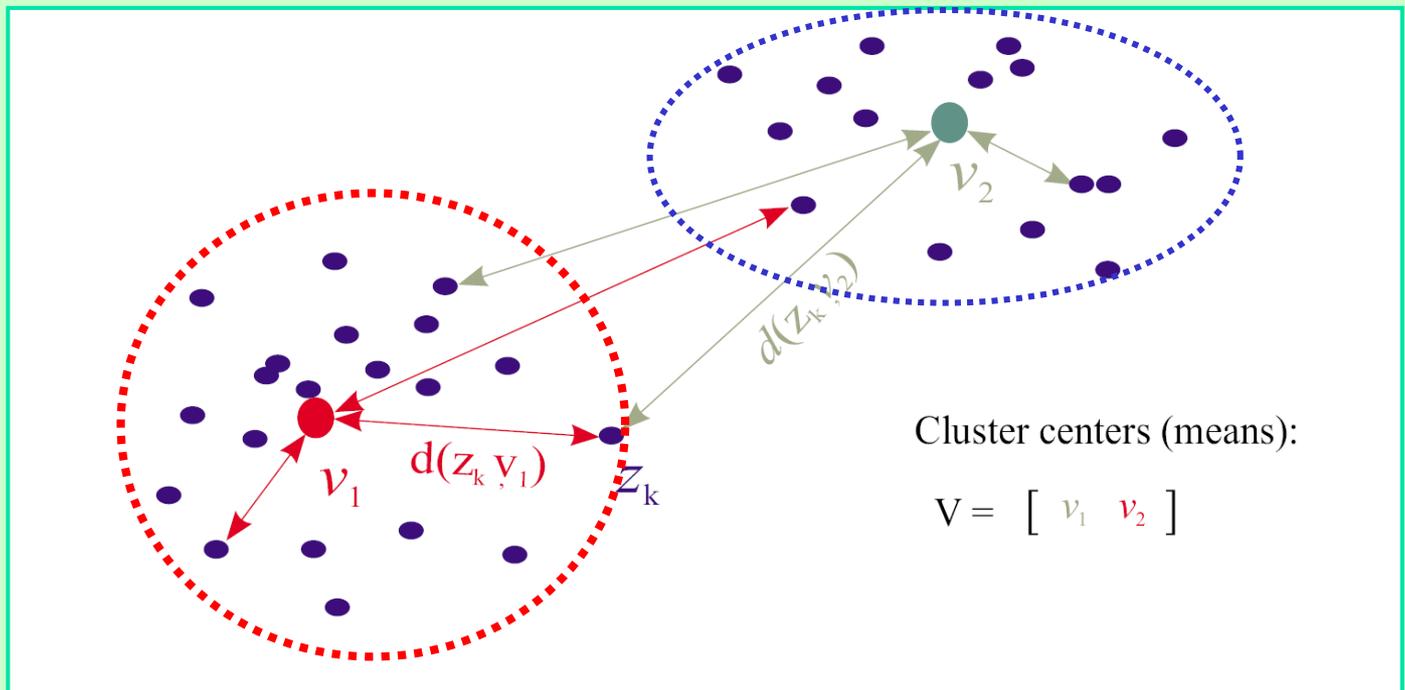
Problem Formulation

- **Given** is a set of data in R^n and the (estimated) number of clusters to look for (a difficult problem, more on this later).
- **Find** the partitioning of the data into subsets (clusters), such that samples within a subset are more similar to each other than to samples from other subsets.
- **Similarity** is mathematically formulated by using a distance measure (i.e., a dissimilarity function).
- Usually, each cluster will have a **prototype** and the distance is measured from this prototype.

14/04/2009

110/148

Distance Measure



14/04/2009

111/148

Distance Measures

➤ Euclidean norm:

$$\blacksquare d^2(\mathbf{z}_j, \mathbf{v}_i) = (\mathbf{z}_j - \mathbf{v}_i)^T (\mathbf{z}_j - \mathbf{v}_i)$$

➤ Inner-product norm:

$$\blacksquare d^2_{A_i}(\mathbf{z}_j, \mathbf{v}_i) = (\mathbf{z}_j - \mathbf{v}_i)^T A_i (\mathbf{z}_j - \mathbf{v}_i)$$

➤ Many other possibilities . . .

14/04/2009

112/148

Fuzzy Clustering: an Optimisation Approach

➤ Objective function (least-squares criterion):

$$J(\mathbf{Z}; \mathbf{V}, \mathbf{U}, \mathbf{A}) = \sum_{i=1}^c \sum_{j=1}^N \mu_{i,j}^m d_{\mathbf{A}_i}^2(\mathbf{z}_j, \mathbf{v}_i)$$

➤ subject to constraints:

$$0 \leq \mu_{i,j} \leq 1, \quad i = 1, \dots, c, \quad j = 1, \dots, N \quad \text{membership degree}$$

$$0 < \sum_{j=1}^N \mu_{i,j} < 1, \quad i = 1, \dots, c \quad \text{no cluster empty}$$

$$\sum_{i=1}^c \mu_{i,j} = 1, \quad j = 1, \dots, N \quad \text{total membership}$$

14/04/2009

113/148

Fuzzy Algorithm

Repeat:

1. Compute cluster prototypes (means):

$$\mathbf{v}_i = \frac{\sum_{k=1}^N \mu_{i,k}^m \mathbf{z}_k}{\sum_{k=1}^N \mu_{i,k}^m}$$

2. Calculate distances:

$$d_{ik} = (\mathbf{z}_k - \mathbf{v}_i)^T (\mathbf{z}_k - \mathbf{v}_i)$$

3. Update partition matrix:

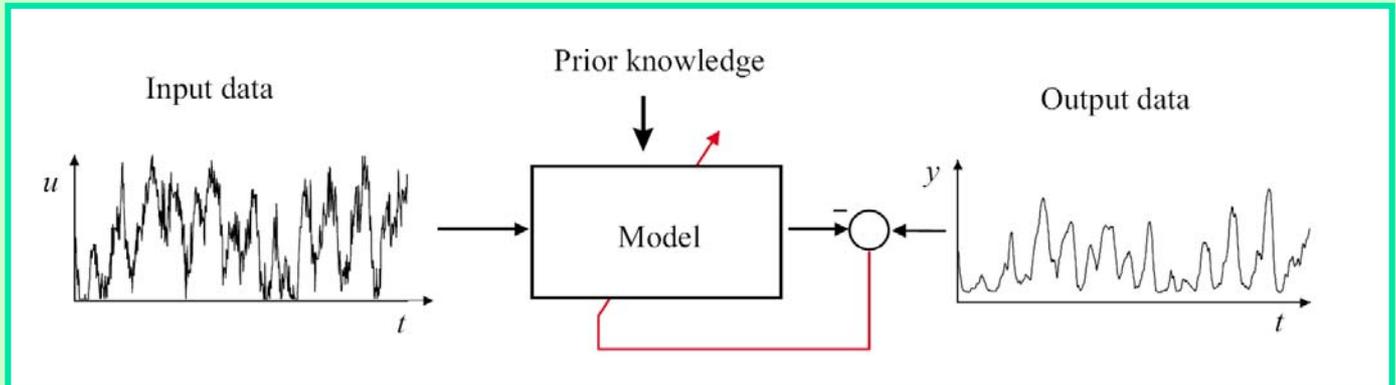
$$\mu_{ik} = \frac{1}{\sum_{j=1}^c (d_{ik}/d_{jk})^{1/(m-1)}}$$

until $\|\Delta \mathbf{U}\| < \epsilon$

$(i = 1, \dots, c, \quad k = 1, \dots, N)$

Data-Driven (Black-Box)

Modelling

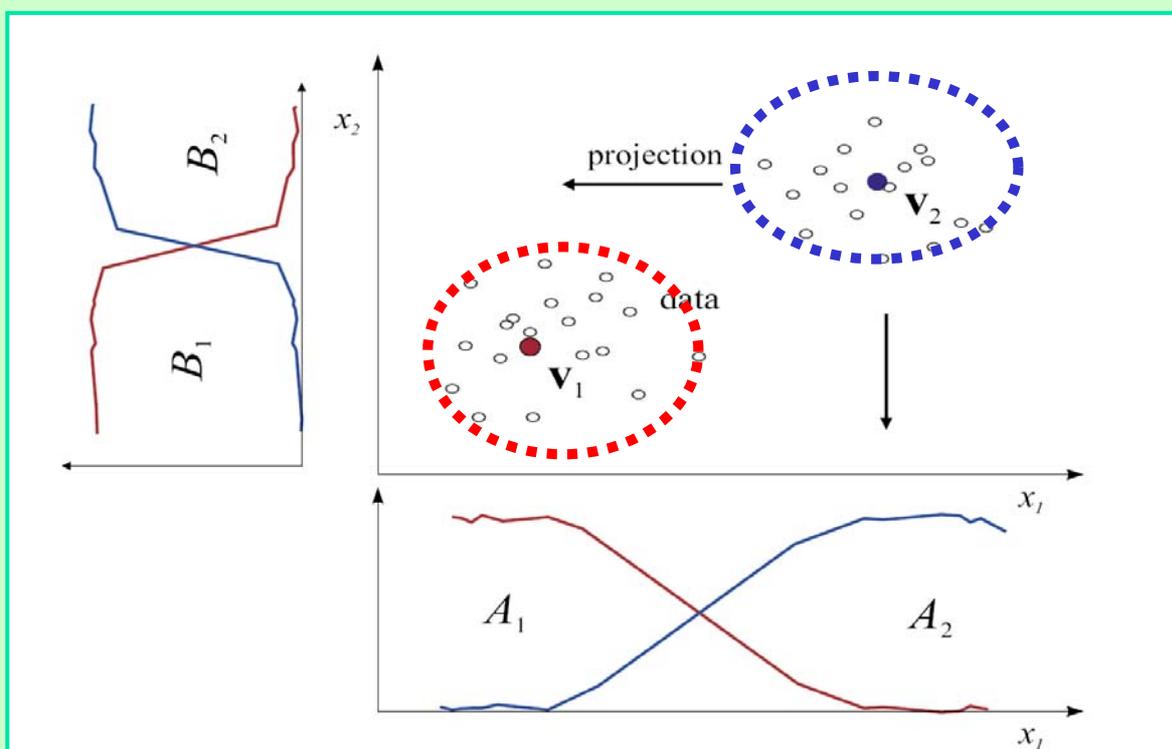


- **Linear model** (for linear systems only, limited in use)
- **Neural network** (black box, unreliable extrapolation)
- **Rule-based model** (more transparent, 'grey-box')

14/04/2009

115/148

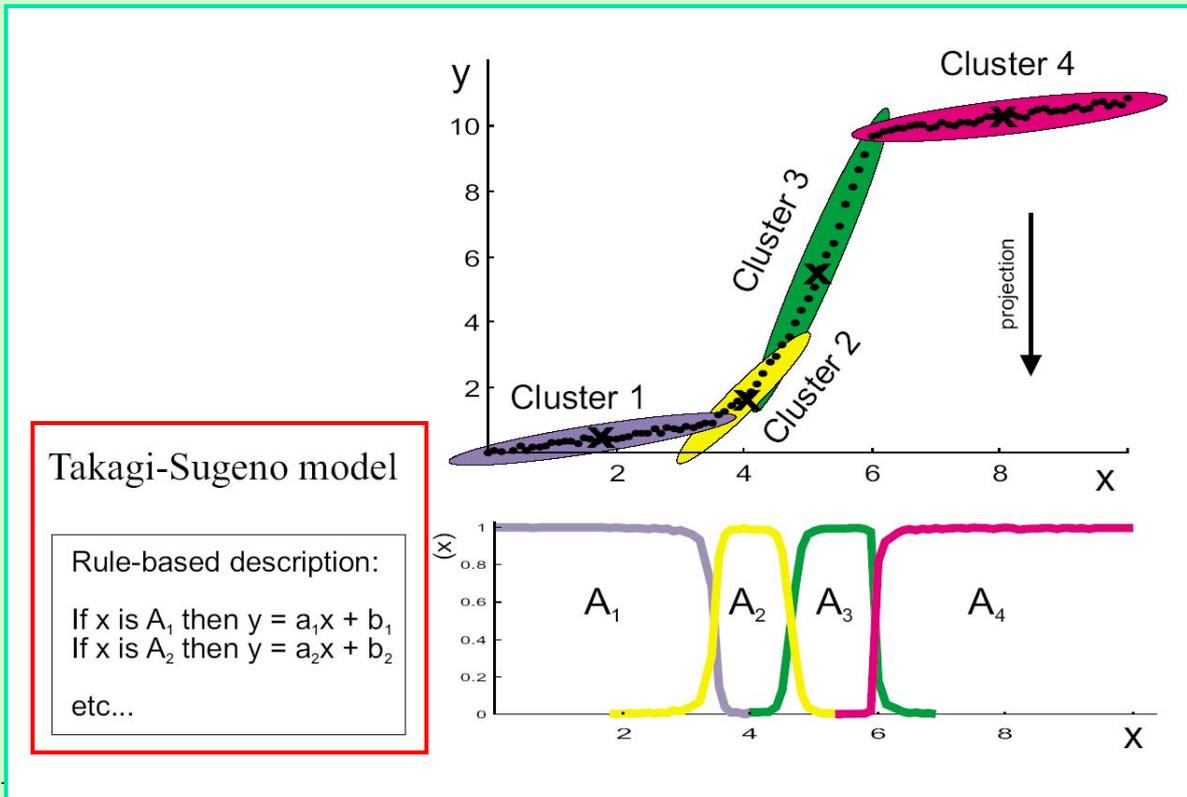
Extraction of Rules by Fuzzy Clustering



14/04/2009

116/148

Extraction of Rules by Fuzzy Clustering



48

Example: Non-linear Autoregressive System (NARX)

$$x(k+1) = f(x(k)) + \epsilon(k)$$

$$f(x) = \begin{cases} 2x - 2, & 0.5 < x \\ -2x, & -0.5 \leq x < 0.5 \\ 2x + 2, & x \leq -0.5 \end{cases}$$

Structure Selection and Data Preparation

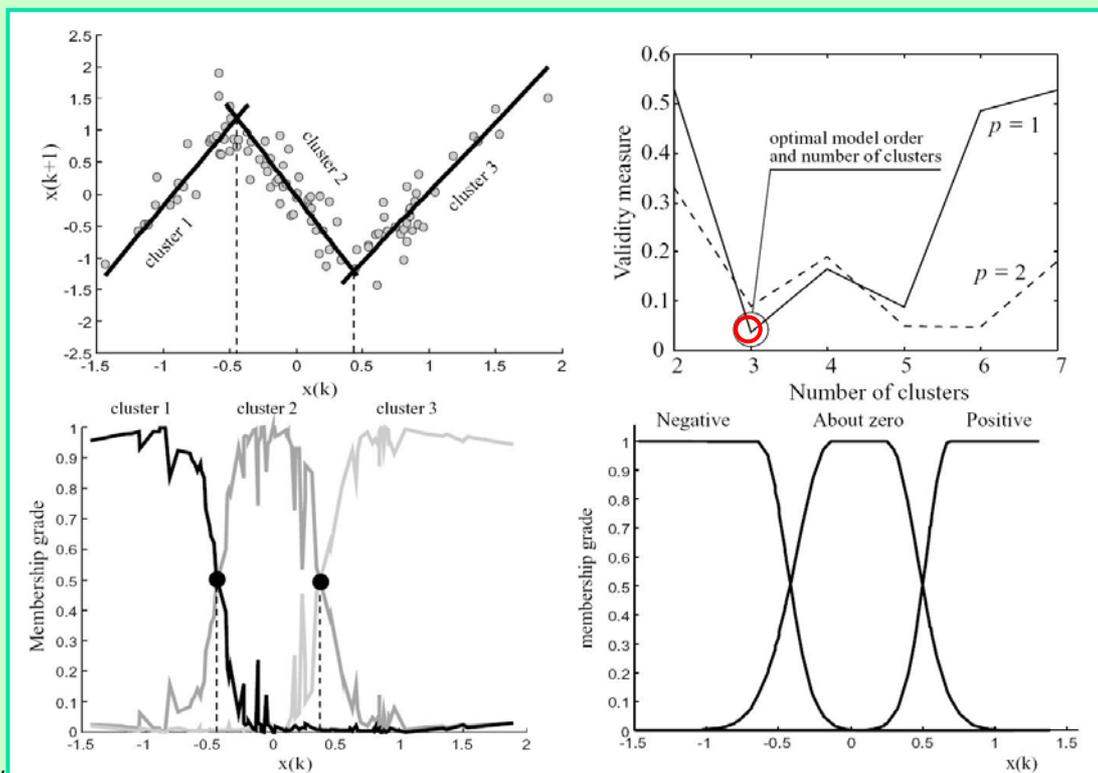
1. Choose model order p

$$x(k+1) = f(\underbrace{x(k), x(k-1), \dots, x(k-p+1)}_{\mathbf{x}(k)})$$

2. Form pattern matrix \mathbf{Z} to be clustered

$$\mathbf{Z}^T = \begin{bmatrix} x(1) & x(2) & \dots & x(p) & x(p+1) \\ x(2) & x(3) & \dots & x(p+1) & x(p+2) \\ \vdots & \vdots & & \vdots & \vdots \\ x(N-p) & x(N-p+1) & \dots & x(N-1) & x(N) \end{bmatrix}$$

Clustering Results



Rules Obtained

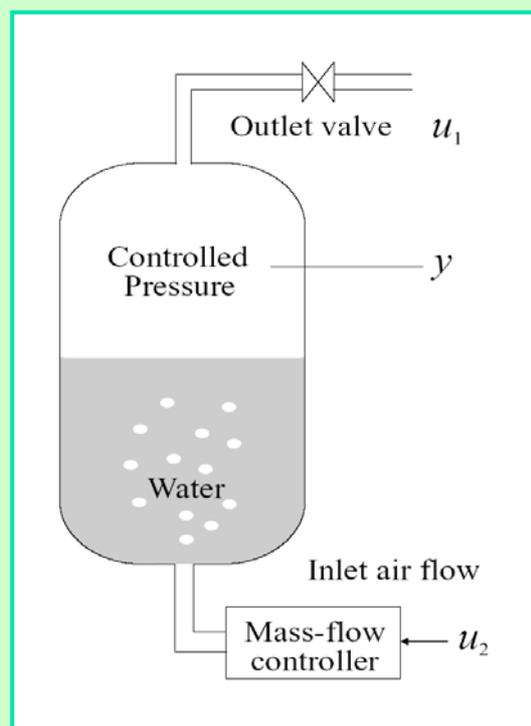
- 1) If $x(k)$ is *Positive* then $x(k+1) = 2.0244x(k) - 2.0289$
- 2) If $x(k)$ is *About zero* then $x(k+1) = -1.8852x(k) + 0.0005$
- 3) If $x(k)$ is *Negative* then $x(k+1) = 1.9050x(k) + 1.9399$

original function:
$$f(x) = \begin{cases} 2x - 2, & 0.5 < x \\ -2x, & -0.5 \leq x < 0.5 \\ 2x + 2, & x \leq -0.5 \end{cases}$$

14/04/2009

121/148

Identification of Pressure Dynamics

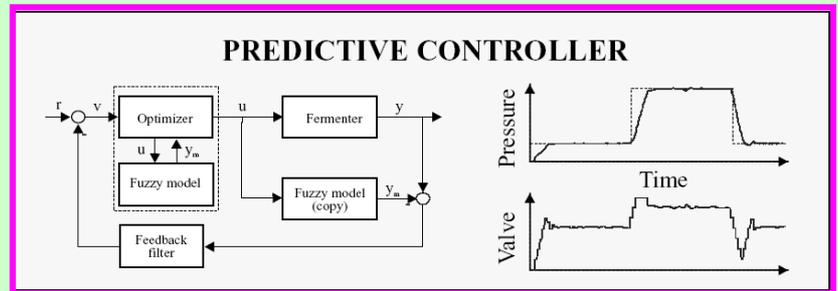
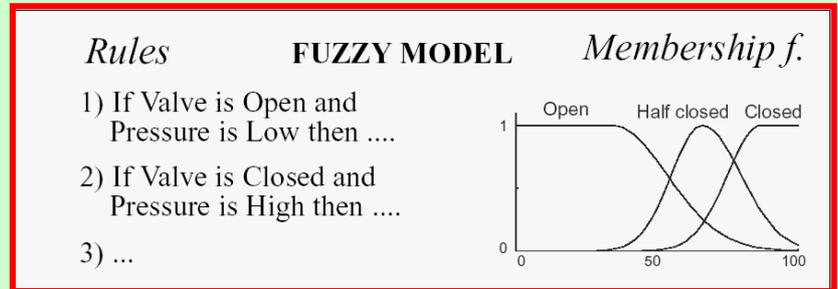
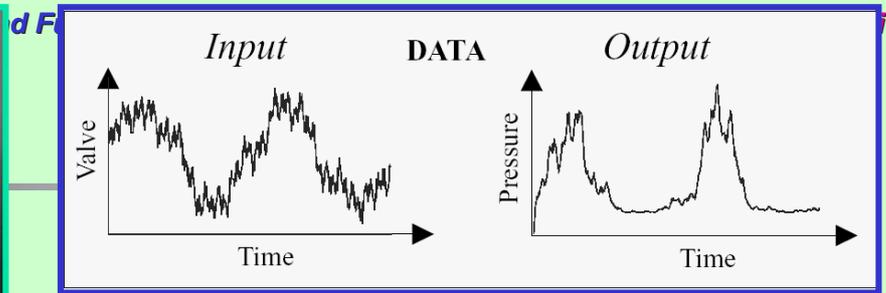


14/04/2009

122/148



14/04/2009



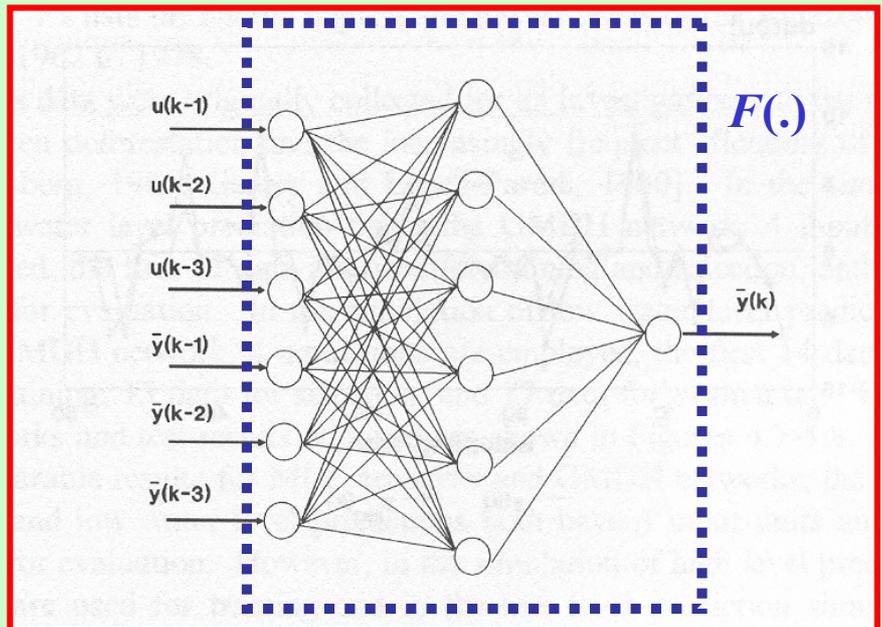
123/148

Application Examples

**Neural Networks for
Non-linear Identification, Prediction and Control**

Nonlinear Dynamic System

- Take a static NN
- From static to dynamic NN
- "Quasi-static" NN
- Add inputs, outputs and delayed signals



$$\tilde{y}(k) = F(u(k-1), u(k-2), u(k-3), \tilde{y}(k-1), \tilde{y}(k-2), \tilde{y}(k-3))$$

Example of Quasi-static NN
with 3 delayed inputs and outputs

14/04/2009

125/148

Nonlinear System Identification

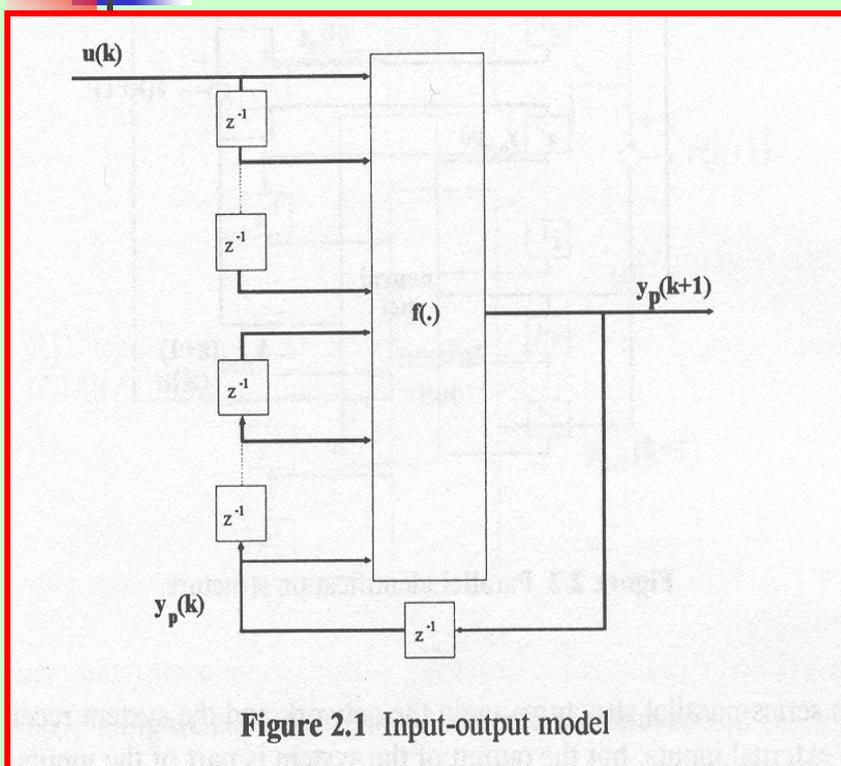


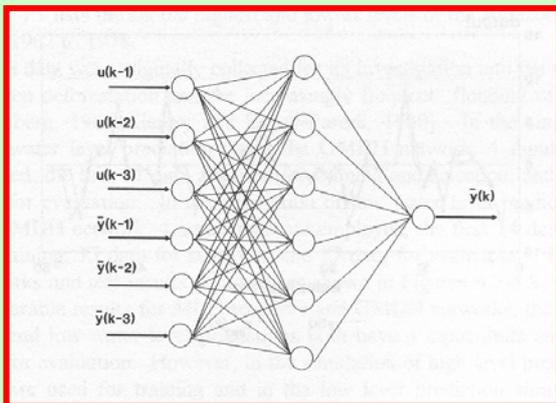
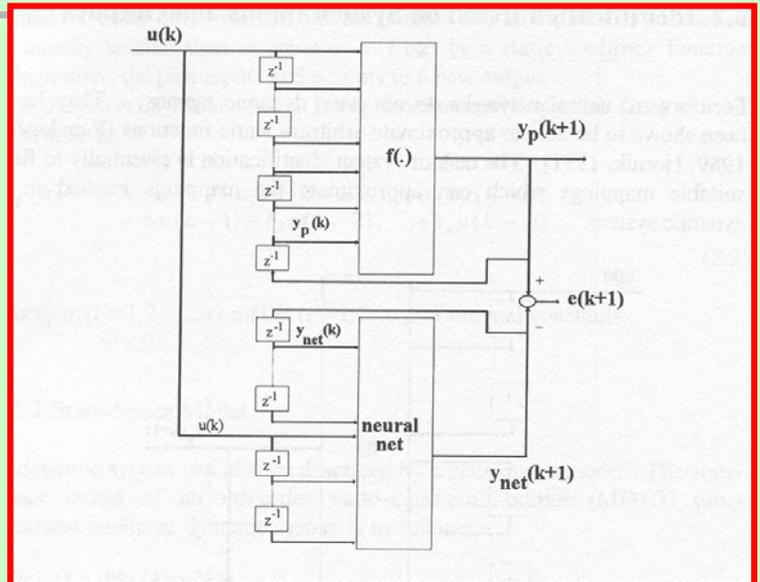
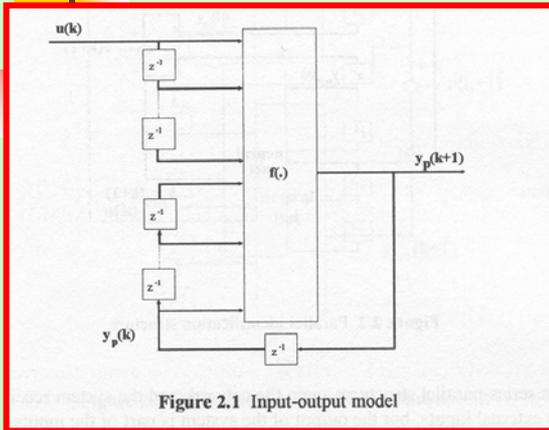
Figure 2.1 Input-output model

- $f(\cdot)$, unknown target function
- Nonlinear dynamic model
- Approximated via a quasi-static NN
- Nonlinear dynamic system identification
- Recall "linear system identification"

14/04/2009

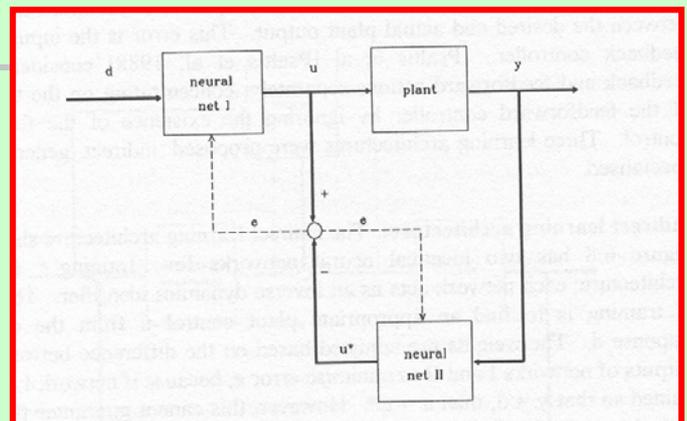
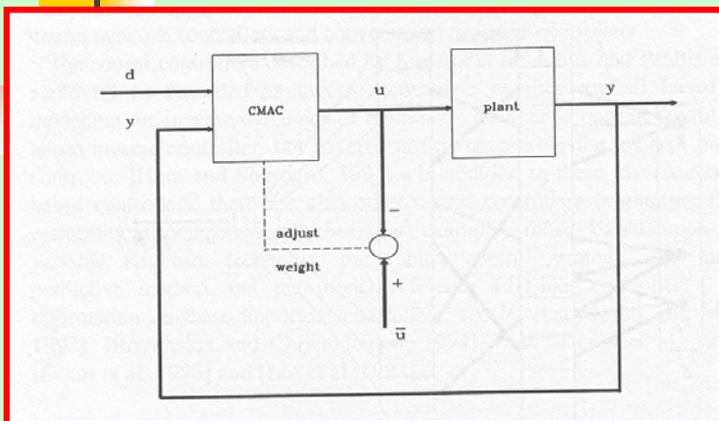
126/148

Nonlinear System Identification



Target function: $y_p(k+1) = f(.)$
 Identified function: $y_{NET}(k+1) = F(.)$
 Estimation error: $e(k+1)$

Nonlinear System Neural Control



d : reference/desired response
 y : system output/desired output
 u : system input/controller output
 \hat{u} : desired controller input
 u^* : NN output
 e : controller/network error

The goal of training is to find an appropriate plant control u from the desired response d . The weights are adjusted based on the difference between the outputs of the networks I & II to minimise e . If network I is trained so that $y = d$, then $u = u^*$. Networks act as inverse dynamics identifiers.

Neural Networks for Control

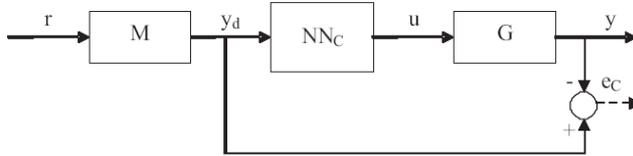


Figure 1: Direct Inverse Control using neural networks

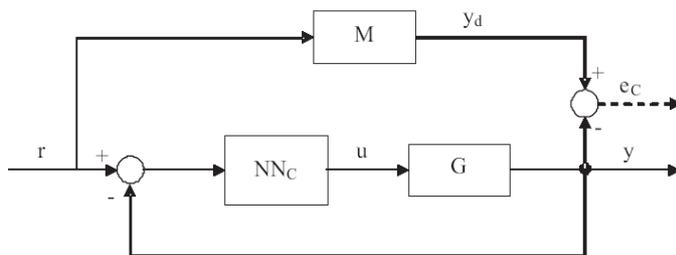


Figure 2: Model Reference Control using neural networks

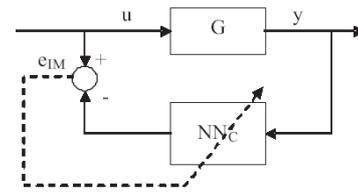


Figure 3: Training the neural network NN_C

↑

←

Figures 1 and 3 Problems.

- Open-loop unstable models
- Disturbances

Neural Model Reference Adaptive Control

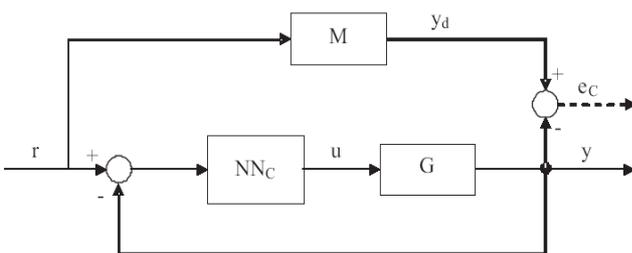


Figure 2: Model Reference Control using neural networks

The signal e_c is used to train or adapt online the weights of the controller NN_C . Two are the approaches used to design a MRAC control for an unknown plant: **Direct and Indirect Control.**

Direct Control: This procedure aims at designing a controller without having a plant model. As the knowledge of the plant is needed in order to train the neural network which corresponds to the controller (*i.e.* NN_C), until present, no method has been proposed to deal with this problem.

Neural Model Reference Adaptive Control

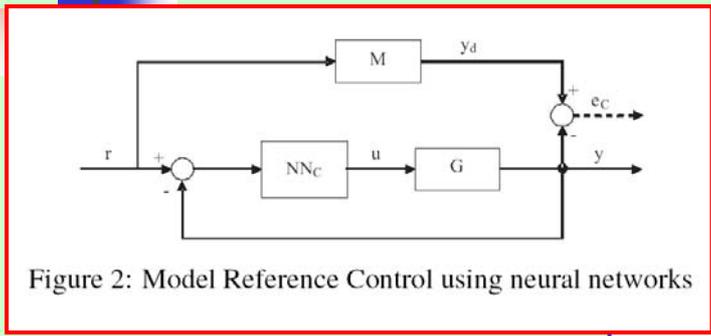


Figure 2: Model Reference Control using neural networks

- The signal e_c is used to train or adapt online the weights of the **neural controller NN_C** .

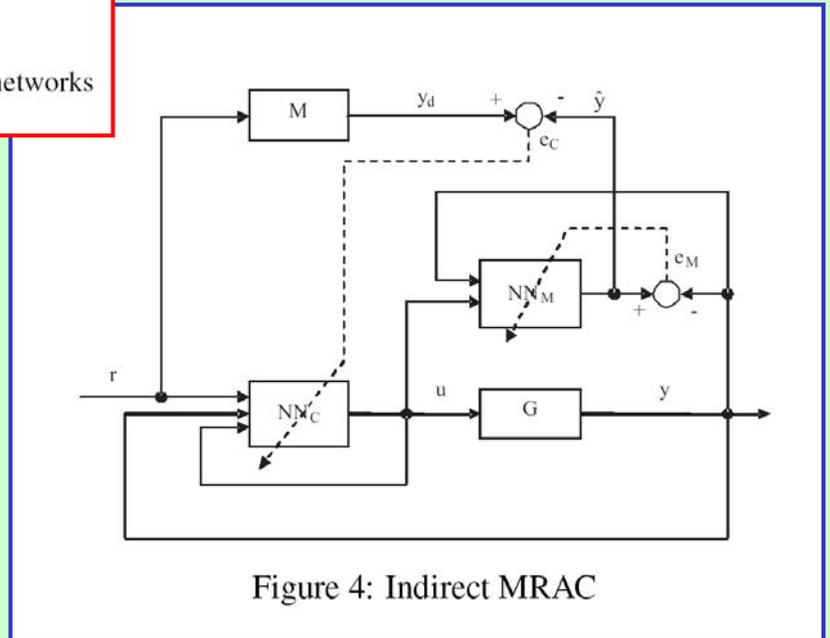


Figure 4: Indirect MRAC

Indirect Control: NN_M & NN_C

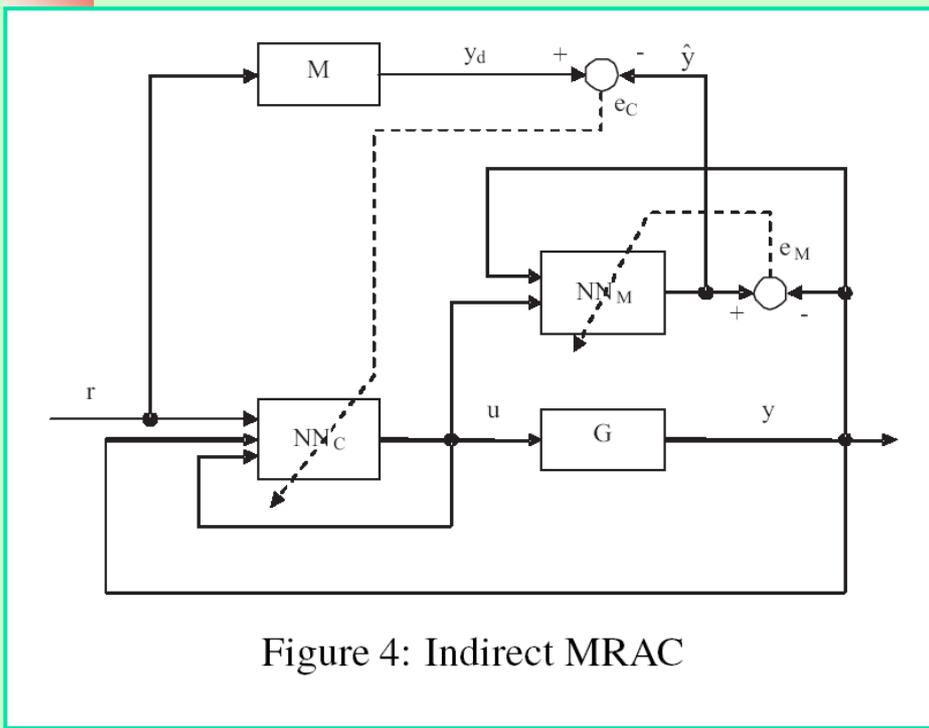


Figure 4: Indirect MRAC

This approach uses two neural networks: one for modelling the plant dynamics (NN_M), and another one trained to control the **real plant (G)** so as its behaviour is as close as possible to the **reference model (M)** via the neural controller (NN_C).

Indirect Control (1)

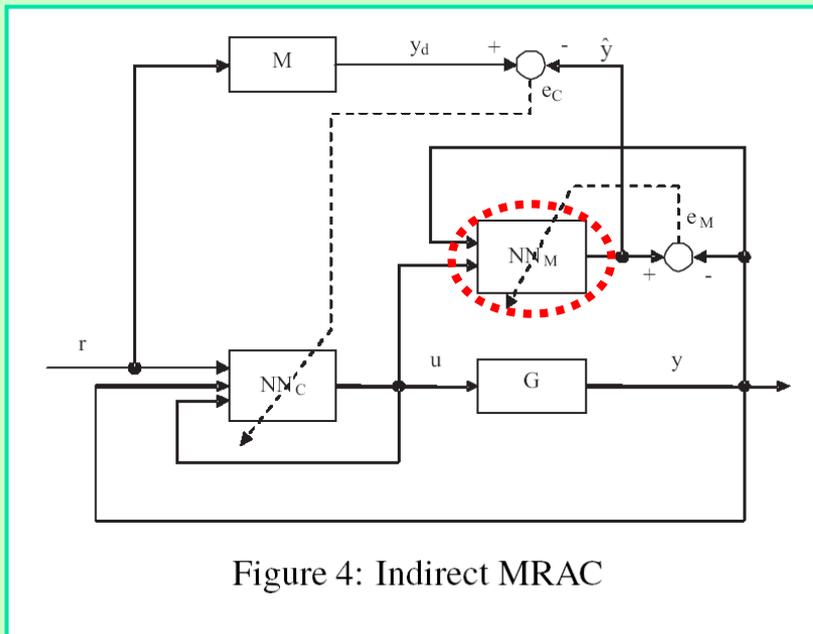


Figure 4: Indirect MRAC

The **neural network** NN_M is trained to approximate the plant **G** input/output relation using the signal e_M . This is usually done offline, using a batch of data gathered from **the plant in open loop**.

14/04/2009

133/148

Indirect Control (2)

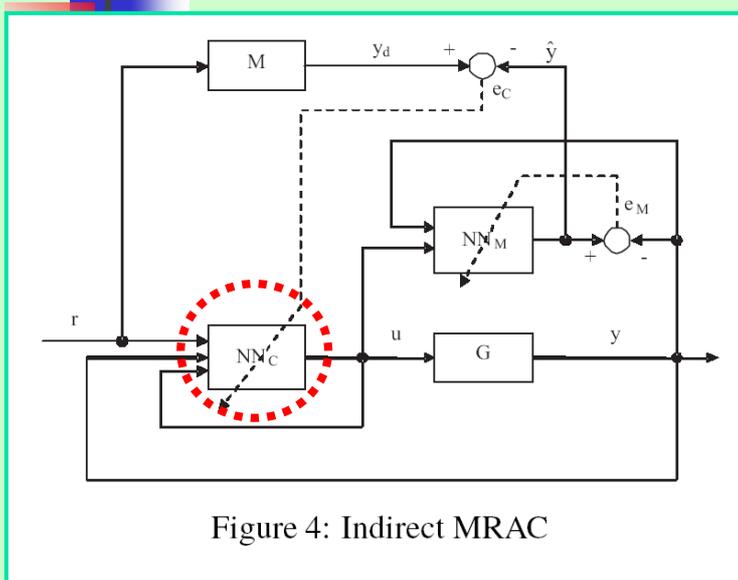


Figure 4: Indirect MRAC

Then, NN_M is fixed, its output and behaviour are known and easy to compute.

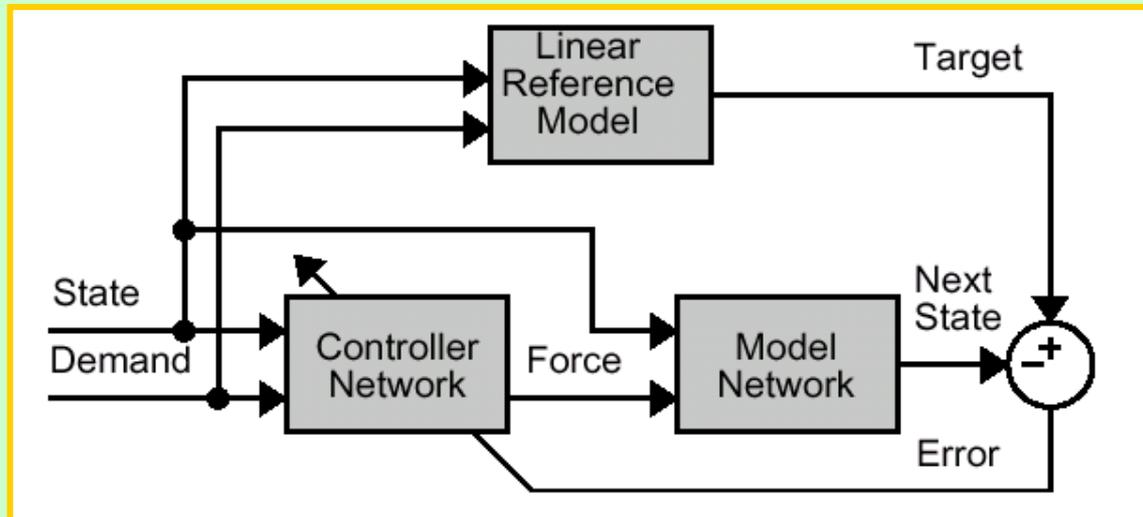
Once the model NN_M is trained, it is used to train the network NN_C which will act as the controller. The model NN_M is used instead of the real plant's output because the real plant is unknown, so back-propagation algorithms can not be used. In this way, the control error e_C is calculated as the difference between the desired reference model output y_d and \hat{y} , which is the closed loop predicted output.

14/04/2009

134/148

Model Reference Control

Matlab and Simulink solution



Neural controller, reference model, neural model

14/04/2009

135/148

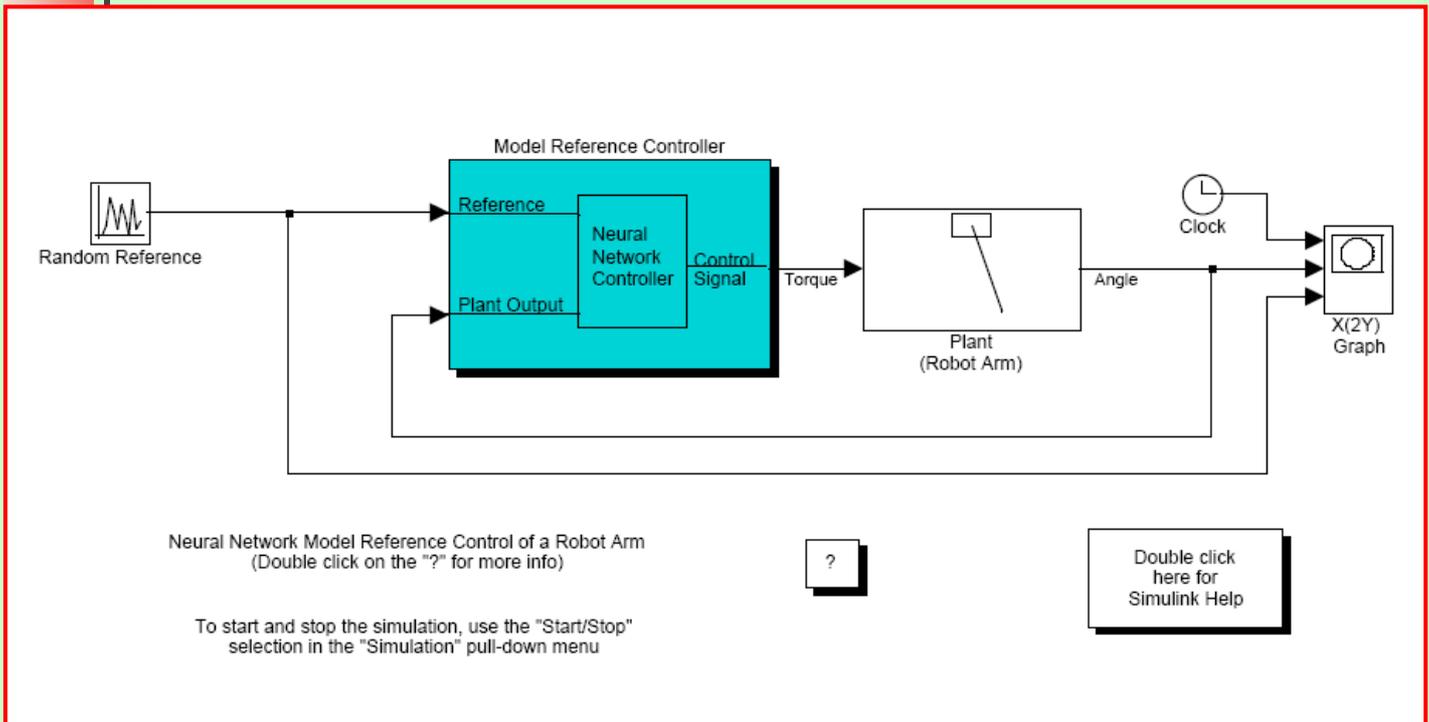
Matlab NNtool GUI (Graphical User Interface)



14/04/2009

135/148

Control of a Robot Arm Example



14/04/2009

137/148

Control of a Robot Arm Example

Model Reference Control

File Window Help

Model Reference Control

Network Architecture

Size of Hidden Layer: 13 No. Delayed Reference Inputs: 2

Sampling Interval (sec): 0.05 No. Delayed Controller Outputs: 1

Normalize Training Data No. Delayed Plant Outputs: 2

Training Data

Maximum Reference Value: 0.7 Controller Training Samples: 6000

Minimum Reference Value: -0.7

Maximum Interval Value (sec): 2 Reference Model: Browse

Minimum Interval Value (sec): 0.1 robotref

Generate Training Data Import Data Export Data

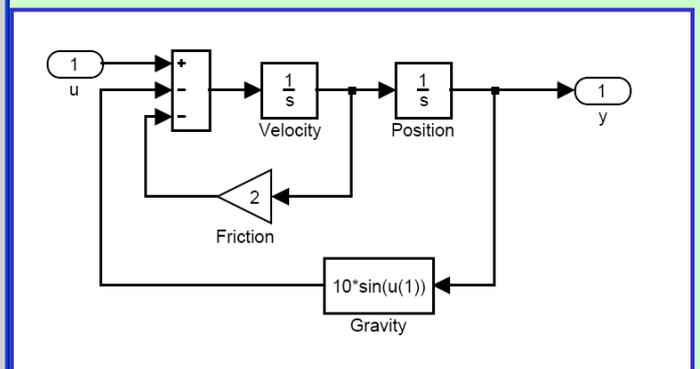
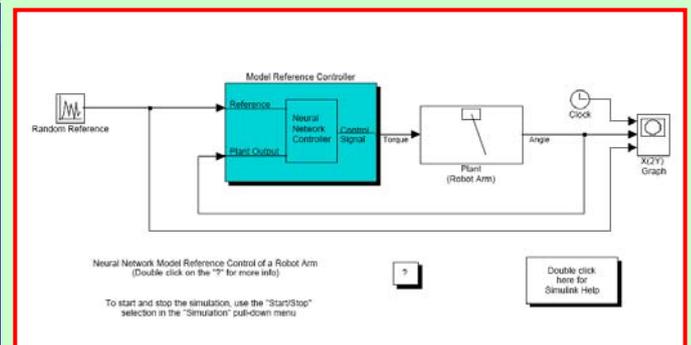
Training Parameters

Controller Training Epochs: 10 Controller Training Segments: 30

Use Current Weights Use Cumulative Training

Plant Identification Train Controller OK Cancel Apply

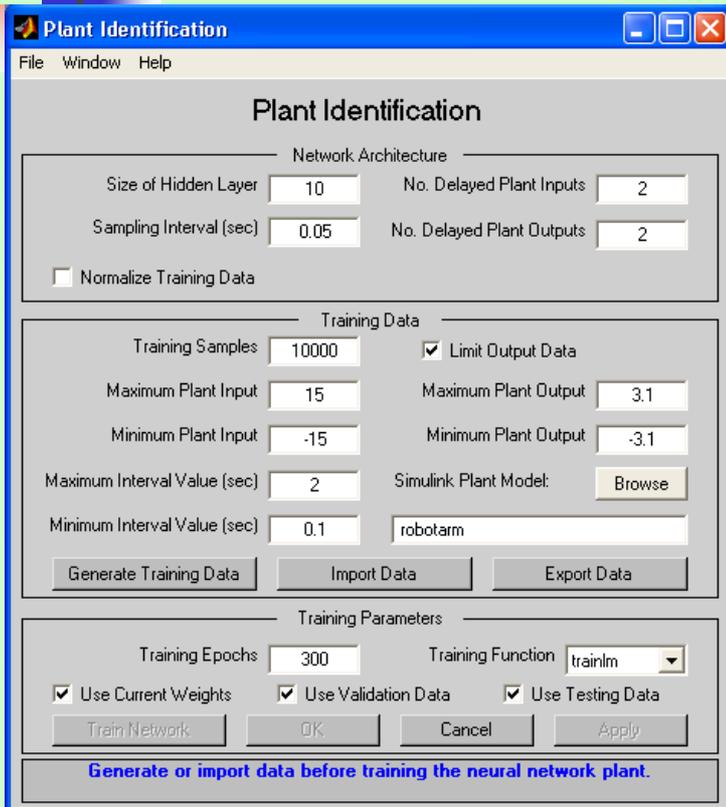
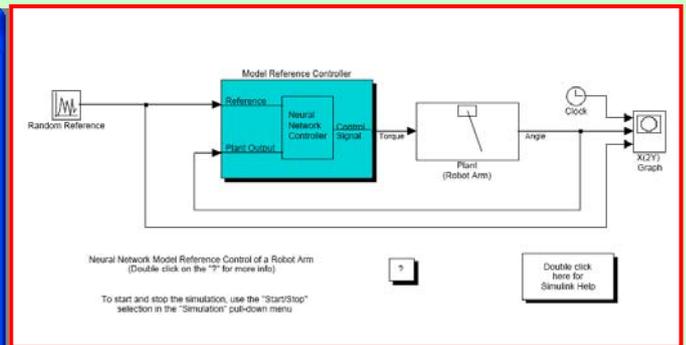
Perform plant identification before controller training.



14/04/2009

138/148

Control of a Robot Arm Example

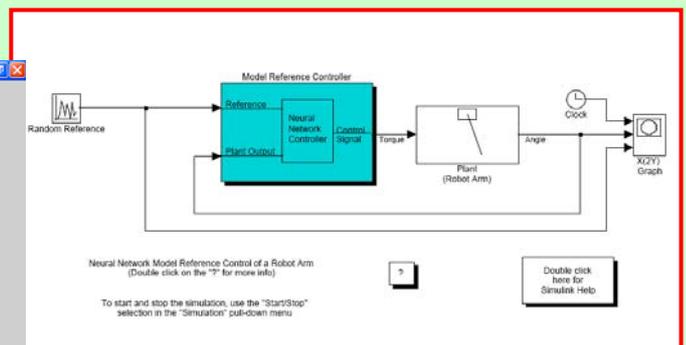
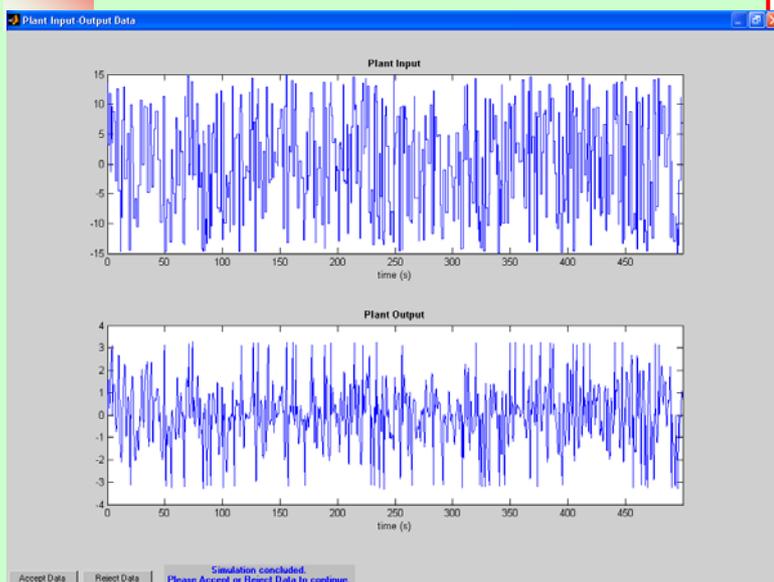
Plant Identification:

Data generation from the Reference Model for Neural Network training

14/04/2009

139/148

Control of a Robot Arm Example



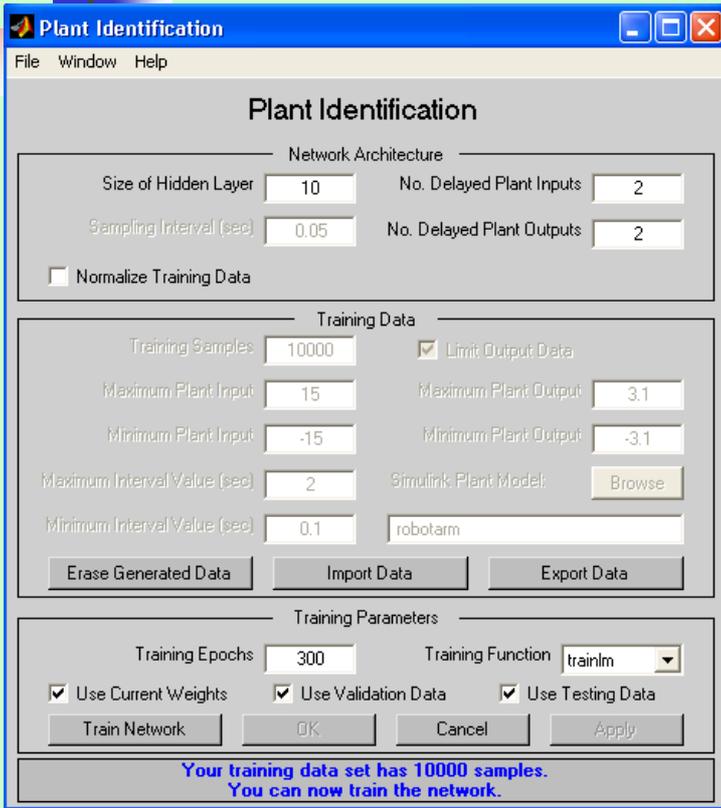
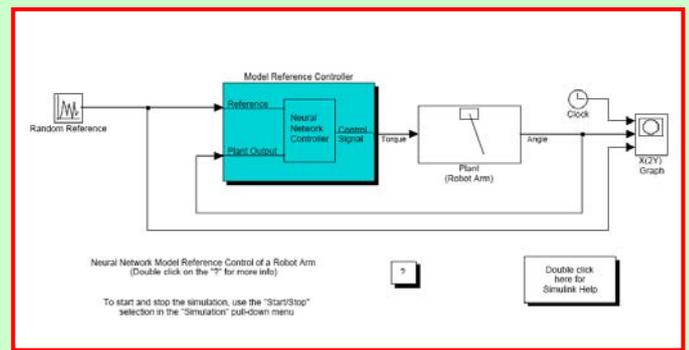
After Plant Identification:

Neural Network training

14/04/2009

140/148

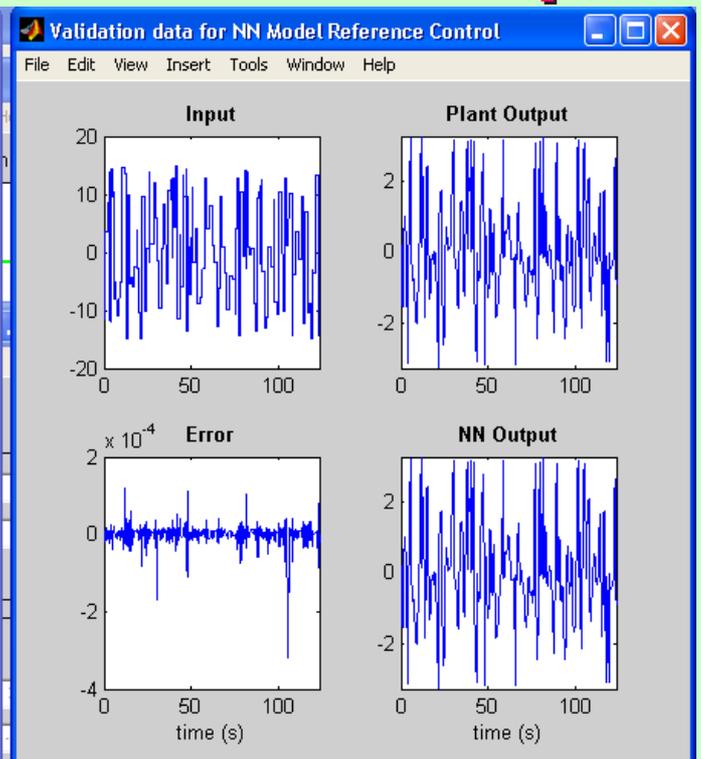
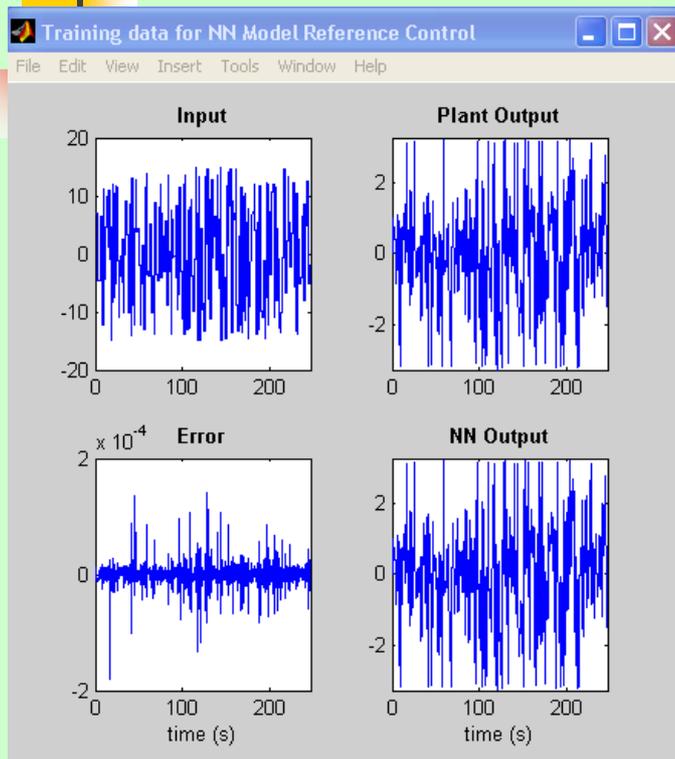
Control of a Robot Arm Example

After Plant Identification:

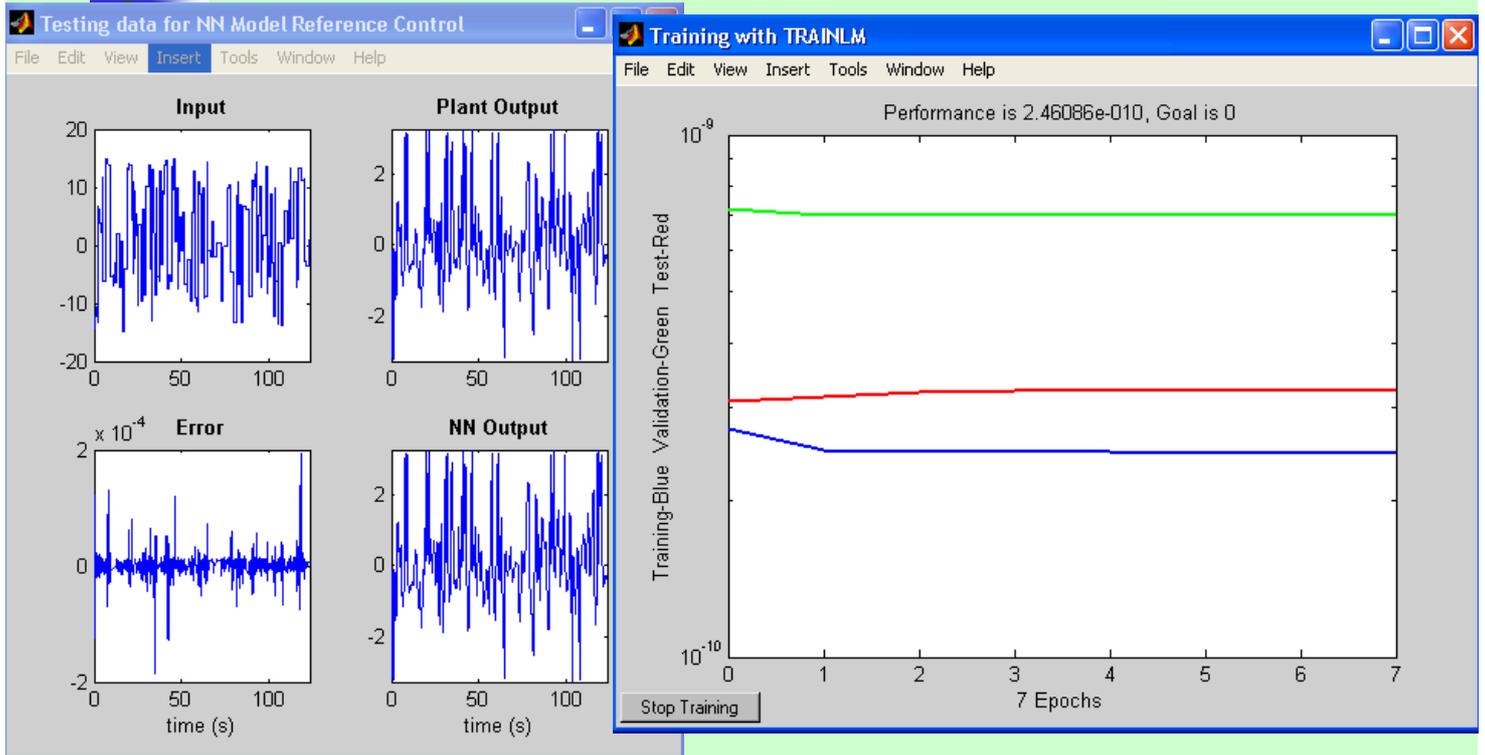
Neural Network training

Control of a Robot Arm Example



Training and Validation Data

Control of a Robot Arm Example



Testing Data and Training Results

14/04/2009

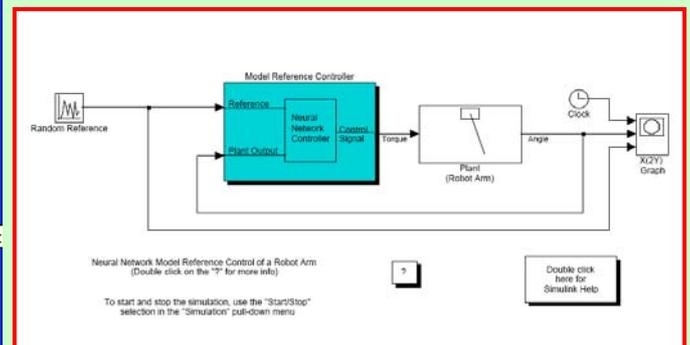
143/148

Control of a Robot Arm Example

The "Model Reference Control" dialog box is shown with the following settings:

- Network Architecture:** Size of Hidden Layer: 13; No. Delayed Reference Inputs: 2; Sampling Interval (sec): 0.05; No. Delayed Controller Outputs: 1; Normalize Training Data; No. Delayed Plant Outputs: 2.
- Training Data:** Maximum Reference Value: 0.7; Minimum Reference Value: -0.7; Controller Training Samples: 6000; Maximum Interval Value (sec): 2; Minimum Interval Value (sec): 0.1; Reference Model: robotref.
- Training Parameters:** Controller Training Epochs: 10; Controller Training Segments: 30; Use Current Weights; Use Cumulative Training.

Buttons include "Generate Training Data", "Import Data", "Export Data", "Plant Identification", "Train Controller", "OK", "Cancel", and "Apply". A note at the bottom states: "Generate or import data before training the neural network controller."

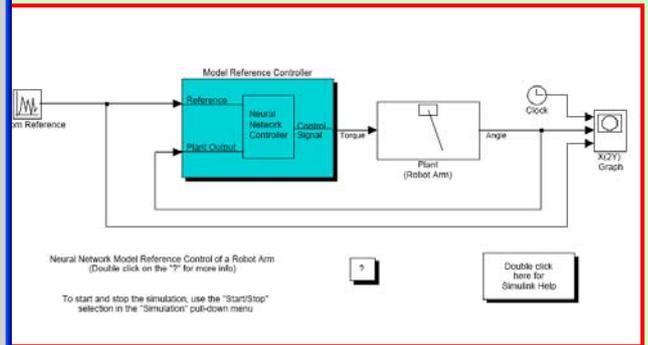
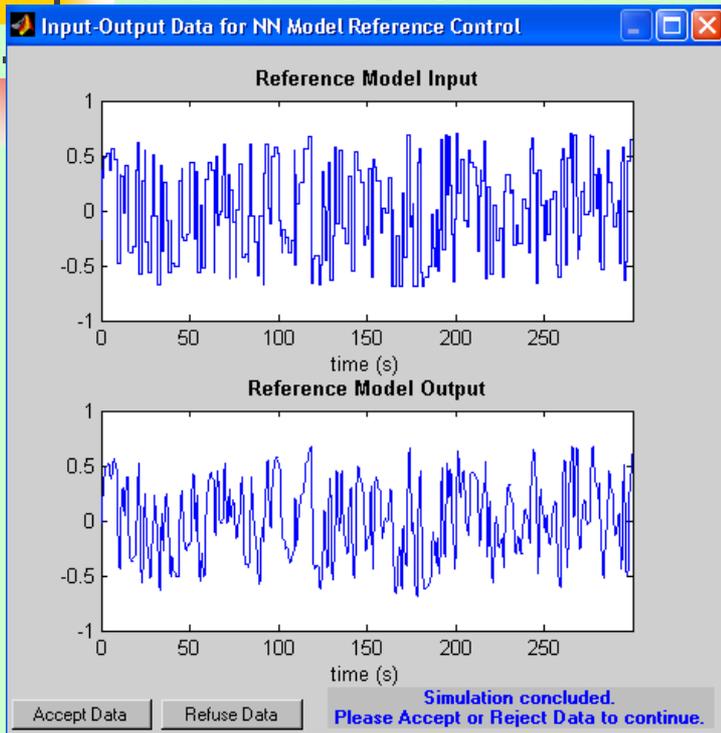


Plant identification with a NN Data Generation for NN Controller Identification

14/04/2009

144/148

Control of a Robot Arm Example



Accept the Data Generated for NN Controller Identification

14/04/2009

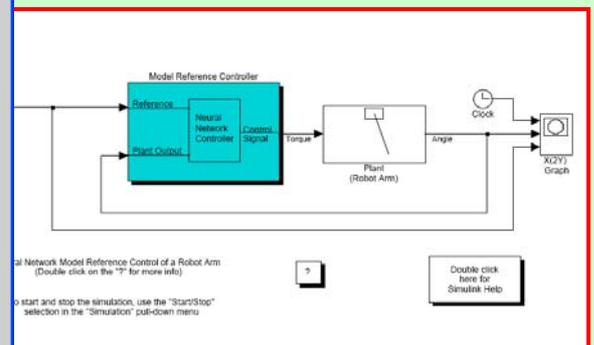
145/148

Control of a Robot Arm Example

The screenshot shows the "Model Reference Control" dialog box. It has a menu bar with "File", "Window", and "Help". The main area is divided into several sections:

- Network Architecture:**
 - Size of Hidden Layer: 13
 - No. Delayed Reference Inputs: 2
 - Sampling Interval (sec): 0.05
 - No. Delayed Controller Outputs: 1
 - Normalize Training Data
 - No. Delayed Plant Outputs: 2
- Training Data:**
 - Maximum Reference Value: 0.7
 - Controller Training Samples: 6000
 - Minimum Reference Value: -0.7
 - Maximum Interval Value (sec): 2
 - Reference Model: Browse
 - Minimum Interval Value (sec): 0.1
 - robotref
- Training Parameters:**
 - Controller Training Epochs: 10
 - Controller Training Segments: 30
 - Use Current Weights
 - Use Cumulative Training

Buttons at the bottom include "Erase Generated Data", "Import Data", "Export Data", "Plant Identification", "Train Controller", "OK", "Cancel", and "Apply". A status bar at the bottom says: "Your training data set has 6000 samples. You can now train the network."

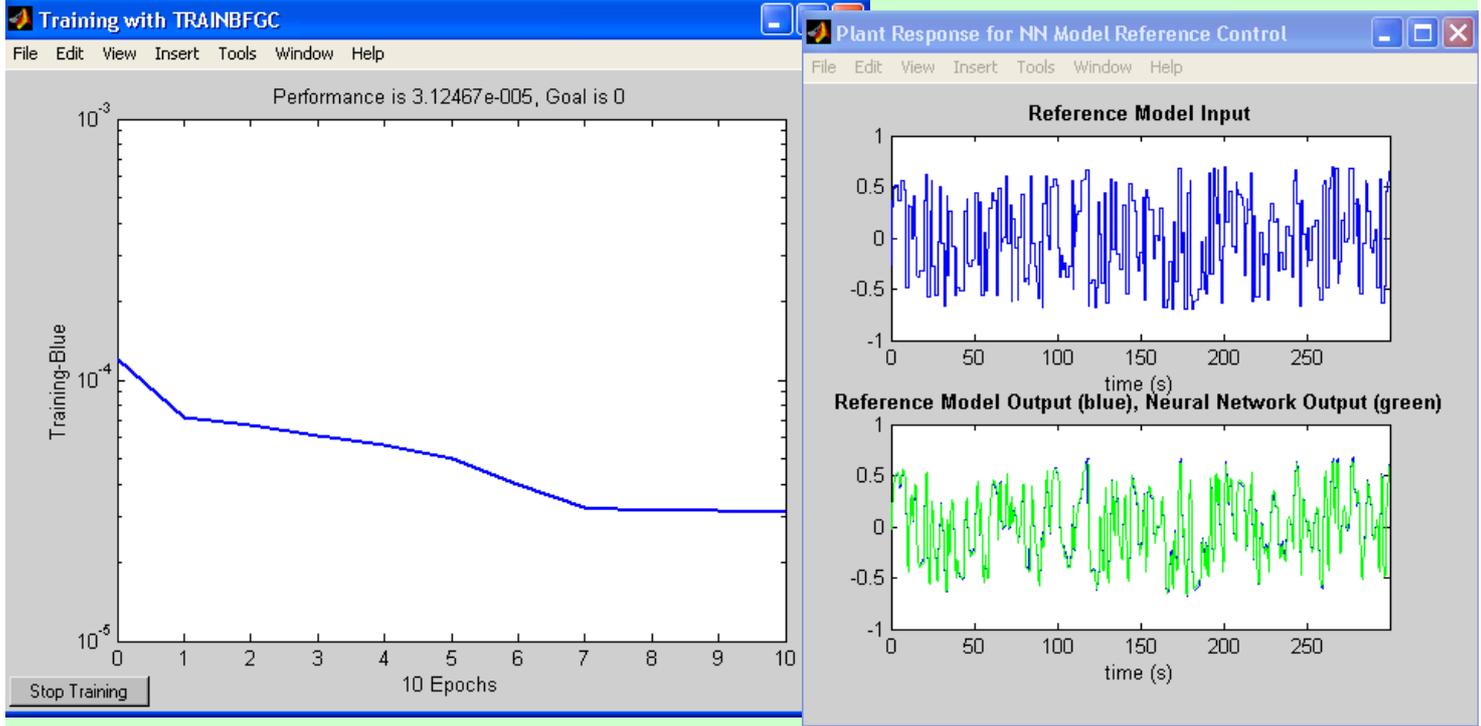


NN Controller Training

14/04/2009

146/148

Control of a Robot Arm Example

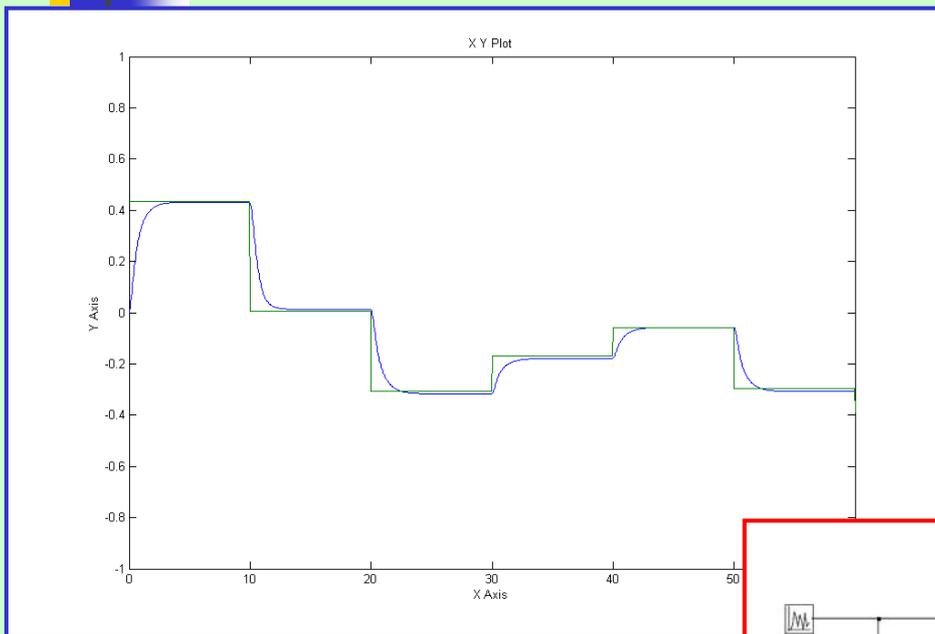


NN Controller Training and Results

14/04/2009

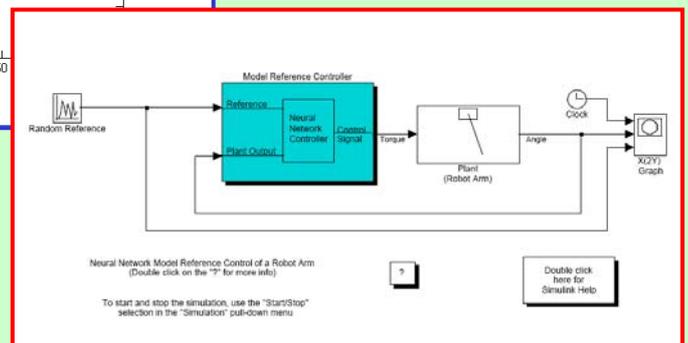
147/148

Control of a Robot Arm Example



Reference and Tracked Output Signals

Simulation Final Results



14/04/2009

148/148