Automazione (Laboratorio)

Reti Neurali e Modelli Fuzzy per L'identificazione, Predizione E Controllo

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References

Textbook (suggested):

- *Neural Networks for Identification, Prediction, and Control*, by Duc Truong Pham and Xing Liu. Springer Verlag; (December 1995). ISBN: 3540199594
- Nonlinear Identification and Control: A Neural Network Approach, by G.
 P. Liu. Springer Verlag; (October 2001). ISBN: 1852333421
- Fuzzy Modeling for Control, by Robert Babuska. Springer; 1st edition (May 1, 1998) ISBN-10: 0792381548, ISBN-13: 978-0792381549.
- *Multi-Objective Optimization using Evolutionary Algorithms*, by Deb Kalyanmoy. John Wiley & Sons, Ltd, Chichester, England, 2001.



Course Overview

- Introduction

 - Course introduction Introduction to neural network Issues in neural network
- 2. Simple neural network i. Perceptron ii. Adaline
- 3. Multilayer Perceptron

 i. Basics
- 4. Genetic Algorithms: overview
- Radial basis networks: overview
- 6. Fuzzy Systems: overview
- 7. Application examples



Machine Learning

- Improve automatically with experience
- Imitating human learning
 - Human learning
 Fast recognition and classification of complex classes of objects and concepts and fast adaptation
 - Example: neural networks
- Some techniques assume statistical source
 Select a statistical model to model the source
- Other techniques are based on reasoning or inductive inference (e.G. Decision tree)

Machine Learning Definition

A computer program is said to **learn** from experience **E** with respect to some class of tasks **T** and performance measure **P**, if its performance at tasks in **T**, as measured by **P**, improves with experience.



Examples of Learning Problems

Example 1: handwriting recognition.

- T: recognizing and classifying handwritten words within images.
- P: percentage of words correctly classified.
- E: a database of handwritten words with given classification.

Example 2: learn to play checkers.

- T: play checkers.
- P: percentage of games won in a tournament.
- E: opportunity to play against itself (war games...).



Type of Training Experience

Direct or indirect?

- Direct: board state -> correct move
- Indirect: credit assignment problem (degree of credit or blame for each move to the final outcome of win or loss)

Teacher or not ?

- Teacher selects board states and provide correct moves Or
- Learner can select board states

Is training experience representative of performance goal?

- Training playing against itself
- Performance evaluated playing against world champion



Issues in Machine Learning

- What algorithms can approximate functions well and when?
- How does the number of training examples influence accuracy?
- How does the complexity of hypothesis representation impact it?
- How does noisy data influence accuracy?
- How do you reduce a learning problem to a set of function approximation?



- Machine learning is useful for data mining, poorly understood domain (face recognition) and programs that must dynamically adapt.
- Draws from many diverse disciplines.
- Learning problem needs well-specified task, performance metric and training experience.
- Involve searching space of possible hypotheses. Different learning methods search different hypothesis space, such as numerical functions, neural networks, decision trees, symbolic rules.



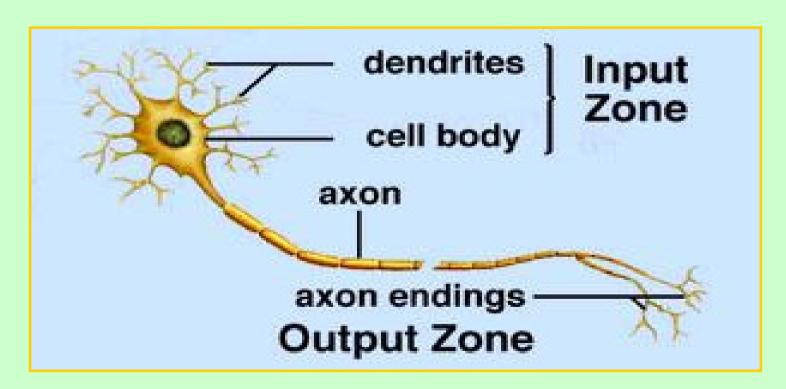
Introduction to Neural Networks

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Brain

- 10¹¹ neurons (processors)
- On average 1000-10000 connections

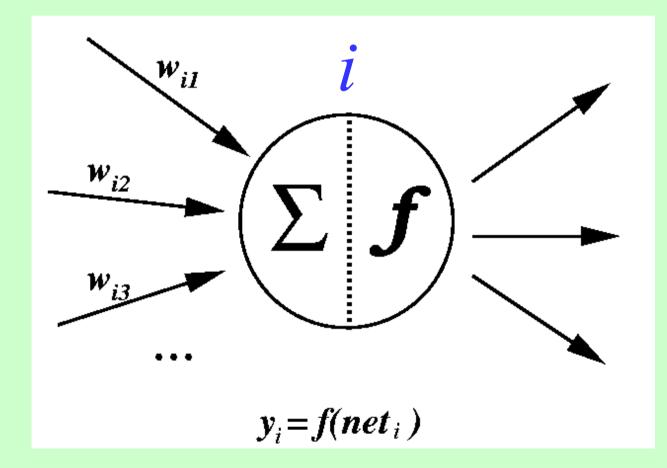




Lecture Notes on Neural Networks and Fuzzy Systems ACTIFICIAL NOTE: The Property of the Prope

bias

$$net_i = \sum_j w_{ij} y_j + b^{2}$$





Artificial Neuron

- Input/Output Signal may be.
 - Real value.
 - Unipolar {0, 1}.
 - Bipolar {-1, +1}.
- Weight: W_{ij} strength of connection.

Note that w_{ij} refers to the weight from **unit** j **to unit** i (not the other way round).

Artificial Neuron

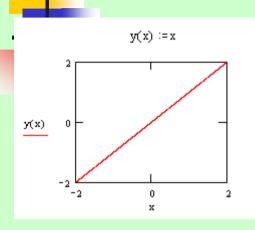
The bias b is a constant that can be written as $w_{i0}y_0$ with $y_0 = b$ and $w_{i0} = 1$ such that

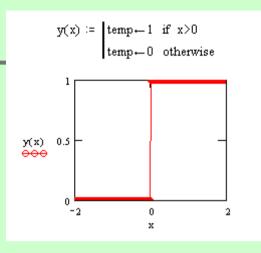
$$net _{i} = \sum_{j=0}^{n} w_{ij} y_{j}$$

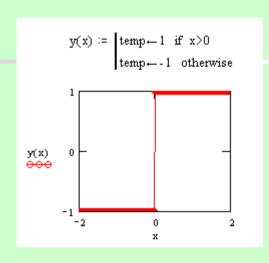
- The function f is the unit's activation function. In the simplest case, f is the identity function, and the unit's output is just its net input. This is called a *linear unit*.
- Other activation functions are: step function,
 sigmoid function and Gaussian function.

Lecture Notes on Neural Networks and Fuzzy-Systems FUNCTIONS

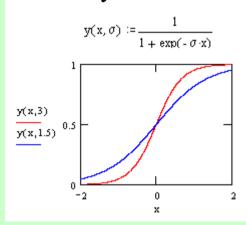
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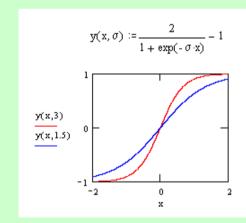




Identity function



Binary Step function



Bipolar Sigmoid function

Bipolar Step function

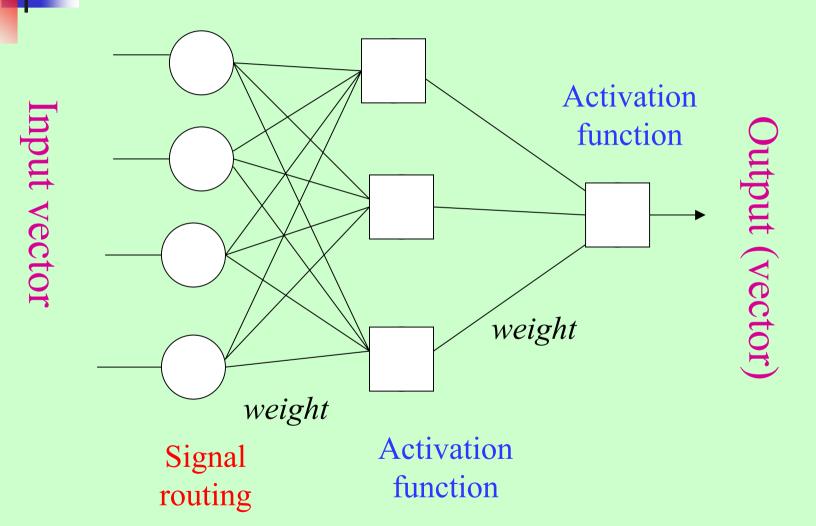
$$y(x) = \frac{1}{\sqrt{2\pi\sigma}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$



Gaussian function

Sigmoid function

Lecture Notes on Neural Networks and Fuzzy Systems Silvio Simani Artificial Neural Networks (ANN)



16/170

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Historical Development of ANN...

- William James (1890): describes in words and figures simple distributed networks and Hebbian learning
- McCulloch & Pitts (1943): binary threshold units that perform logical operations (they proof universal computation)
- Hebb (1949): formulation of a physiological (local) learning rule
- Roseblatt (1958): the perceptron— a first real learning machine
- Widrow & Hoff (1960): ADALINE and the Widrow-Hoff supervised learning rule



Historical Development of ANN

- Kohonen (1982) : Self-organizing maps
- Hopfield (1982): Hopfield Networks
- Rumelhart, Hinton & Williams (1986):
 Back-propagation & Multilayer Perceptron
- Broomhead & Lowe (1988): Radial basis functions (RBF)
- Vapnik (1990) Support Vector Machine

When Should ANN Solution Be Considered?

- The solution to the problem cannot be explicitly described by an algorithm, a set of equations, or a set of rules.
- There is some evidence that an input-output mapping exists between a set of input and output variables.
- There should be a large amount of data available to train the network.

02/05/2008 19/170

Problems That Can Lead to **Poor** Performance ?

- The network has to distinguish between very similar cases with a very high degree of accuracy.
- The train data does not represent the ranges of cases that the network will encounter in practice.
- The network has a several hundred inputs.
- The main discriminating factors are not present in the available data. E.g. Trying to assess the loan application without having knowledge of the applicant's salaries.
- The network is required to implement a very complex function.

Applications of Artificial Neural Networks

- Manufacturing : fault diagnosis, fraud detection.
- Retailing: fraud detection, forecasting, data mining.
- Finance: fraud detection, forecasting, data mining.
- Engineering: fault diagnosis, signal/image processing.
- Production : fault diagnosis, forecasting.
- Sales & marketing : forecasting, data mining.

Data Pre-processing

Neural networks very **rarely** operate on the raw data. An initial **pre-processing** stage is essential. Some examples are as follows:

■ Feature extraction of images: for example, the analysis of x-rays requires pre-processing to extract features which may be of interest

within a specified region.

Representing input variables with numbers. For example "+1" is the person is married, "0" if divorced, and "-1" if single. Another example is representing the pixels of an image: 255 = bright white, 0 = black. To ensure the generalization capability of a neural network, the data should be encoded in form which allows for interpolation.



Data Pre-processing

Categorical Variable

- A categorical variable is a variable that can belong to one of a number of discrete categories. For example, red, green, blue.
- Categorical variables are usually encoded using 1 out-of n coding. e.g. for three colors, red = (1 0 0), green =(0 1 0) Blue =(0 0 1).
- If we used red = 1, green = 2, blue = 3, then this type of encoding imposes an ordering on the values of the variables which does not exist.



Data Pre-processing

CONTINUOUS VARIABLES

• A continuous variable can be directly applied to a neural network. However, if the dynamic range of input variables are not approximately the same, it is better to *normalize* all input variables of the neural network.

Example of Normalized Input Vector

- Input vector : (2 4 5 6 10 4)*
- Mean of vector : $\mu = \frac{1}{6} \sum_{i=1}^{6} x_i = 5.167$ Standard deviation : $\sigma = \sqrt{\frac{1}{6-1} \sum_{i=1}^{6} (x_i \mu)^2} = 2.714$
- Normalized vector: $x_N = \frac{x_i \mu}{\sigma} = (-1.17 0.43 0.06 \ 0.31 \ 1.78 0.43)^t$
- Mean of normalized vector is zero
- Standard deviation of normalized vector is unity



Simple Neural Networks

Simple Perceptron

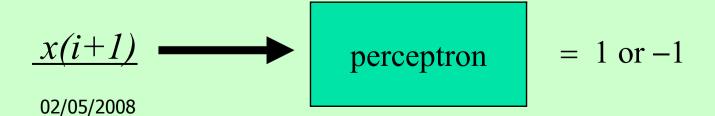




- The Perceptron
- Linearly separable problem
- Network structure
- Perceptron learning rule
- Convergence of Perceptron

Lecture Notes on Neural Networks and Fuzzy Systems THE PERCEPTRON

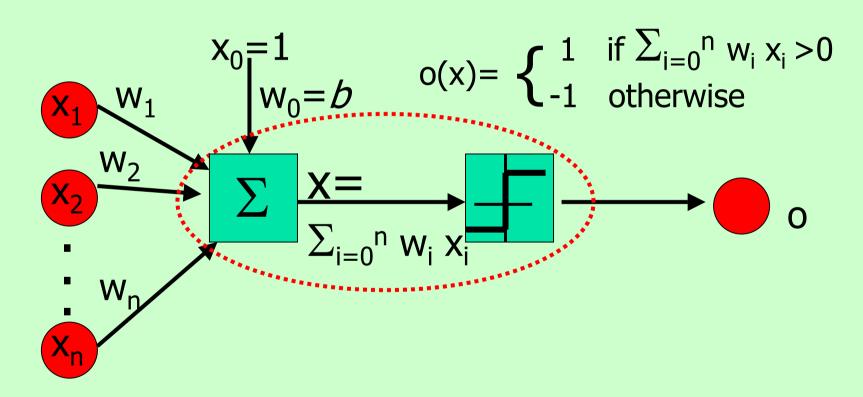
- The perceptron was a simple model of ANN introduced by Rosenblatt of MIT in the 1960' with the idea of learning.
- > Perceptron is designed to accomplish a simple pattern recognition task: after learning with real value training data $\{x(i), d(i), i = 1, 2, ..., p\}$ where d(i) = 1 or -1
- For a new signal (pattern) $\underline{x(i+1)}$, the perceptron is capable of telling you to which class the new signal belongs





Perceptron

Linear Threshold Unit (LTU)



Lecture Notes on Neural Networks and Fuzzy Systems The Perceptron IS

$$y = f(\sum_{i=1}^{m} w_i x_i + b) = f(\sum_{i=0}^{m} w_i x_i)$$

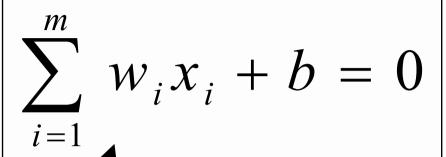
We can always treat the bias *b* as another weight with inputs equal 1

where f is the hard limiter function i.e.

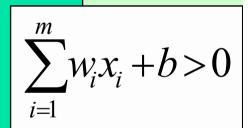
$$y = \begin{cases} 1 & \text{if } \sum_{i=1}^{m} w_i x_i + b > 0 \\ -1 & \text{if } \sum_{i=1}^{m} w_i x_i + b \le 0 \end{cases}$$



capable of solving linearly separable problem?



$$\sum_{i=1}^{m} w_i x_i + b < 0$$



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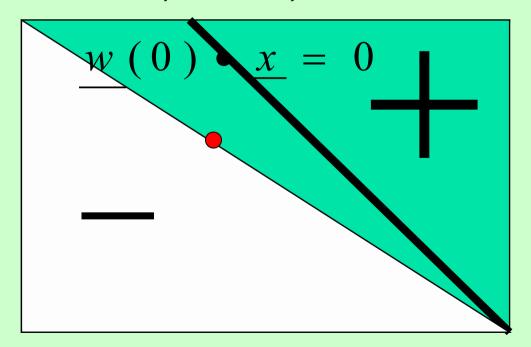
31/170



Learning rule

An algorithm to update the weights \underline{w} so that finally the input patterns lie on both sides of the line decided by the perceptron

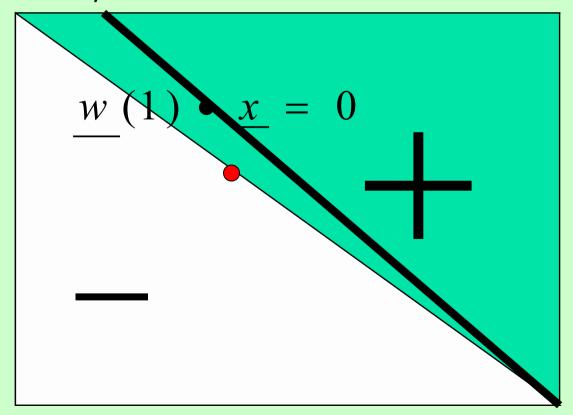
Let t be the time, at t = 0, we have



Lecture Notes on Neural Network

An algorithm to update the weights <u>w</u> so that finally the input patterns lie on both sides of the line decided by the perceptron

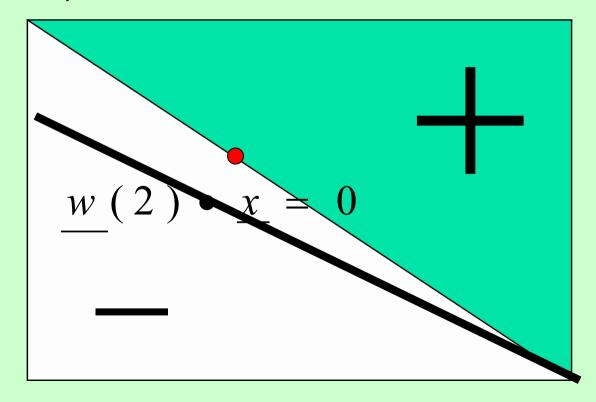
Let t be the time, at t = 1



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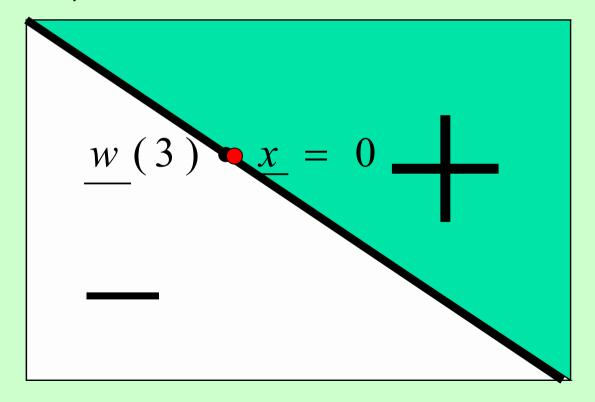
An algorithm to update the weights <u>w</u> so that finally the input patterns lie on both sides of the line decided by the perceptron

Let t be the time, at t = 2



An algorithm to update the weights <u>w</u> so that finally the input patterns lie on both sides of the line decided by the perceptron

Let t be the time, at t = 3





In Math

$$d(t) = \begin{cases} + 1 & \text{if } x(t) & \text{in } class \\ - 1 & \text{if } x(t) & \text{in } class \end{cases} -$$

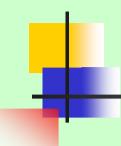
Perceptron learning rule

$$\underline{w}(t+1) = \underline{w}(t) + \eta(t)[d(t) - sign(\underline{w}(t) \bullet \underline{x}(t))] \underline{x}(t)$$

Where $\eta(t)$ is the learning rate >0,

$$sign(x) = \begin{cases} +1 & \text{if } x > 0 \\ -1 & \text{if } x < = 0, \end{cases}$$
 hard limiter function

NB: d(t) is the same as d(i) and x(t) as x(i)



In words:

• If the classification is right, do not update the weights

• If the classification is not correct, update the weight towards the opposite direction so that the output move close to the right directions.

Perceptron convergence theorem (Rosenblatt, 1962)

Let the subsets of training vectors be linearly separable. Then after finite steps of learning we have

 $\lim \underline{w}(t) = \underline{w}$ which correctly separate the samples.

The idea of proof is that to consider $||\underline{w}(t+1)-\underline{w}||-||\underline{w}(t)-\underline{w}||$ which is a decrease function of t

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Summary of Perceptron learning ...

Variables and parameters

$$\underline{x}(t) = (m+1)$$
 dim. input vectors at time t = $(b, x_1(t), x_2(t), \dots, x_m(t))$

$$\underline{w}(t) = (m+1)$$
 dim. weight vectors $= (1, w_1(t), ..., w_m(t))$

b = bias

y(t) = actual response

 $\eta(t)$ = learning rate parameter, a +ve constant < 1

d(t) = desired response

Lectur Sotes on Neural Networks Treat Systems tron learning ... Silvio Simani

$$Data \{ (\underline{x}(i), d(i)), i=1,...,p \}$$

- ✓ Present the data to the network once a point
- ✓ could be cyclic : $(\underline{x}(1), d(1)), (\underline{x}(2), d(2)), ..., (\underline{x}(p), d(p)), (\underline{x}(p+1), d(p+1)), ...$
- ✓ or randomly

(Hence we mix time t with i here)



- **1. Initialisation** Set $\underline{w}(0)=0$. Then perform the following computation for time step t=1,2,...
- **2. Activation** At time step t, activate the perceptron by applying input vector $\underline{X}(t)$ and desired response d(t)
- **3. Computation of actual response** Compute the actual response of the perceptron

$$y(t) = sign \left(\underline{w}(t) \cdot \underline{x}(t) \right)$$

where **sign** is the sign function

4. Adaptation of weight vector Update the weight vector of the perceptron

$$\underline{w}(t+1) = \underline{w}(t) + \eta(t) \left[d(t) - y(t) \right] \underline{x}(t)$$

5. Continuation



Questions remain

Where or when to stop?

By minimizing the generalization error

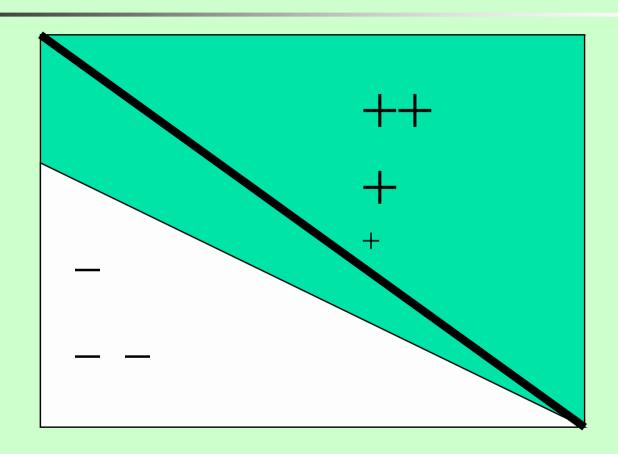
For training data $\{(\underline{x}(i), d(i)), i=1,...p\}$

How to define training error after t steps of learning?

$$E(t) = \sum_{i=1}^{p} [d(i) - sign(\underline{w}(t) \cdot \underline{x}(i)]^{2}$$



After learning t steps

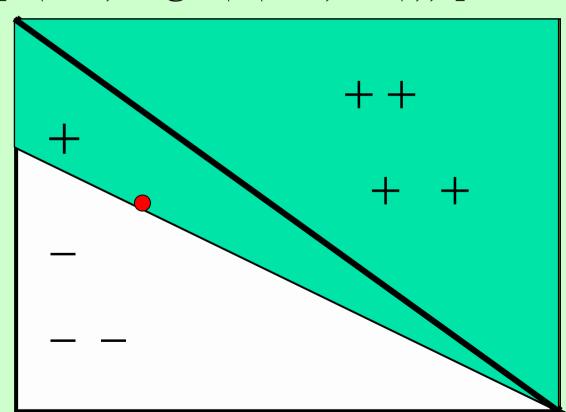


How to define generalisation error?

For a new signal $\{x(t+1),d(t+1)\}$, we have

$$E_g = [d(t+1)-sign (\underline{x}(t+1)-\underline{w}(t))]^2$$

After learning t steps





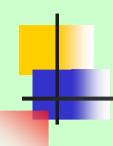
We next turn to ADALINE learning, from which we can understand the learning rule, and more general the Back-Propagation (BP) learning

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Simple Neural Network

ADALINE Learning





ADALINE

Gradient descending learning

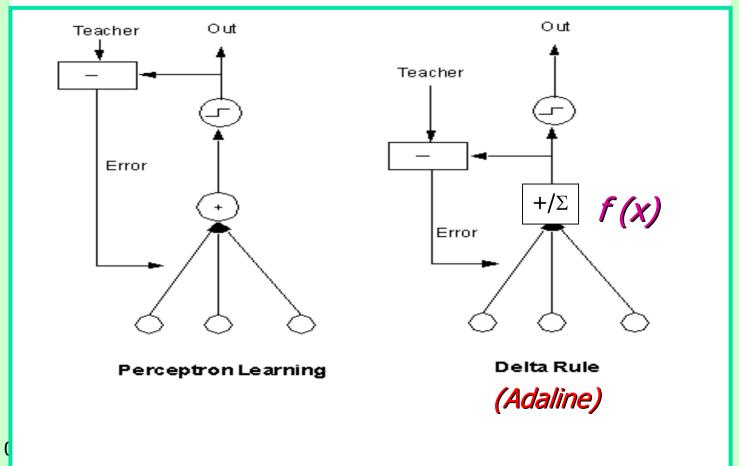
Modes of training

Unhappy Over Perceptron Training

- When a perceptron gives the right answer, no learning takes place
- Anything below the threshold is interpreted as 'no', even it is just below the threshold.
- It might be better to train the neuron based on how far below the threshold it is.

- •ADALINE is an acronym for ADAptive LINear Element (or ADAptive LInear NEuron) developed by Bernard Widrow and Marcian Hoff (1960).
- There are several variations of Adaline. One has threshold same as perceptron and another just a bare linear function.
- •The Adaline learning rule is also known as the leastmean-squares (LMS) rule, the delta rule, or the Widrow-Hoff rule.
- It is a training rule that minimizes the output error using (approximate) gradient descent method.

- Replace the step function in the perceptron with a continuous (differentiable) function f, e.g the simplest is linear function
- With or without the threshold, the Adaline is trained based on the output of the function f rather than the final output.





After each training pattern $\underline{x}(i)$ is presented, the correction to apply to the weights is proportional to the error.

$$E(i,t) = \frac{1}{2} [d(i) - f(\underline{w}(t) \cdot \underline{x}(i))]^2$$
 $i=1,...,p$

N.B. If f is a linear function $f(\underline{w}(t) \cdot \underline{x}(i)) = \underline{w}(t) \cdot \underline{x}(i)$

Summing together, our purpose is to find \underline{W} which minimizes

$$E(t) = \sum_{i} E(i,t)$$



General Approach gradient descent method

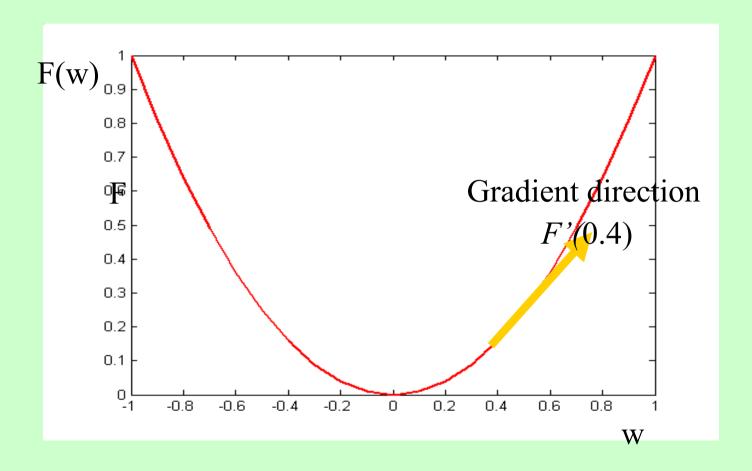
To find g $\underline{w}(t+1) = \underline{w}(t) + g(E(\underline{w}(t)))$

so that \underline{w} automatically tends to the global minimum of E(w).

$$\underline{w}(t+1) = \underline{w}(t) - E'(\underline{w}(t))\eta(t)$$

(see figure below)

• Gradient direction is the direction of uphill for example, in the Figure, at position 0.4, the gradient is uphill (F is E, consider one dim case)



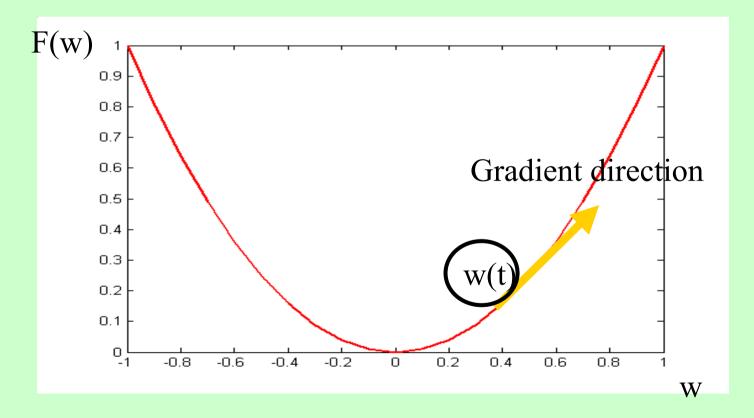
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53/170

In gradient descent algorithm, we have

$$\underline{w}(t+1) = \underline{w}(t) - F'(w(t)) \eta(\tau)$$

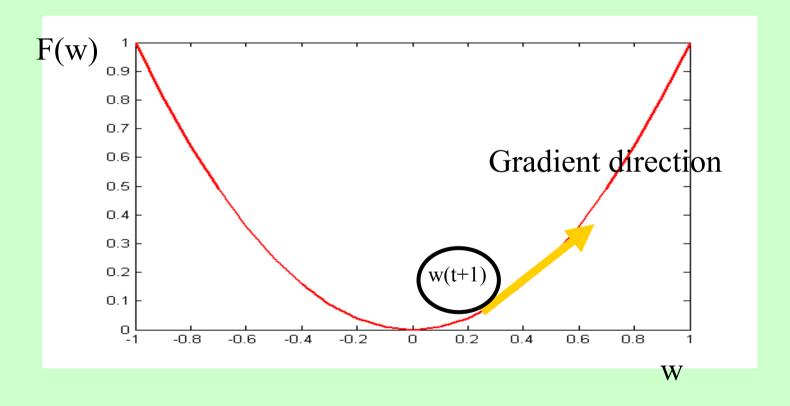
therefore the ball goes downhill since -F'(w(t)) is downhill direction



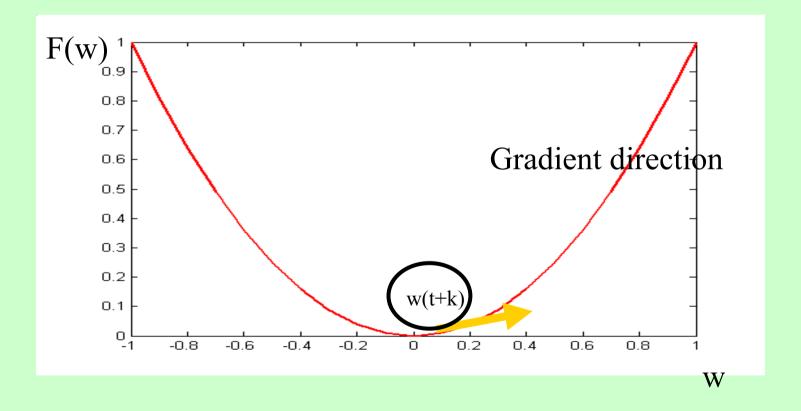
In gradient descent algorithm, we have

$$w(t+1) = w(t) - F'(w(t)) \eta(\tau)$$

therefore the ball goes downhill since – F'(w(t)) is downhill direction



 Gradually the ball will stop at a local minima where the gradient is zero



02/05/2008 56/170

In words

Gradient method could be thought of as a ball rolling down from a hill: the ball will roll down and finally stop at the valley

Thus, the weights are adjusted by

$$w_j(t+1) = w_j(t) + \eta(t) \sum \left[d(i) - f(\underline{w}(t) \cdot \underline{x}(i)) \right] x_j(i) f'$$

This corresponds to gradient descent on the quadratic error surface E

When f' = 1, we have the perceptron learning rule (we have in general f'>0 in neural networks). The ball moves in the right direction.



Two types of network training:

Sequential mode (on-line, stochastic, or per-pattern):

Weights updated after each pattern is presented (Perceptron is in this class)

Batch mode (off-line or per-epoch): Weights updated after all patterns are presented

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Comparison Perceptron and Gradient Descent Rules

- Perceptron learning rule guaranteed to succeed if
 - Training examples are linearly separable
 - Sufficiently small learning rate η
- Linear unit training rule uses gradient descent guaranteed to converge to hypothesis with minimum squared error given sufficiently small learning rate η
 - Even when training data contains noise
 - Even when training data not separable by hyperplanes



Renaissance of Perceptron

Multi-Layer Perceptron

Back-Propagation, 80'

Perceptron

Learning Theory, 90'

Support Vector Machine



Summary

Perceptron

$$\underline{W}(t+1) = \underline{W}(t) + \eta(t) [d(t) - sign(\underline{w}(t) . \underline{x})] \underline{x}$$

Adaline (Gradient descent method)

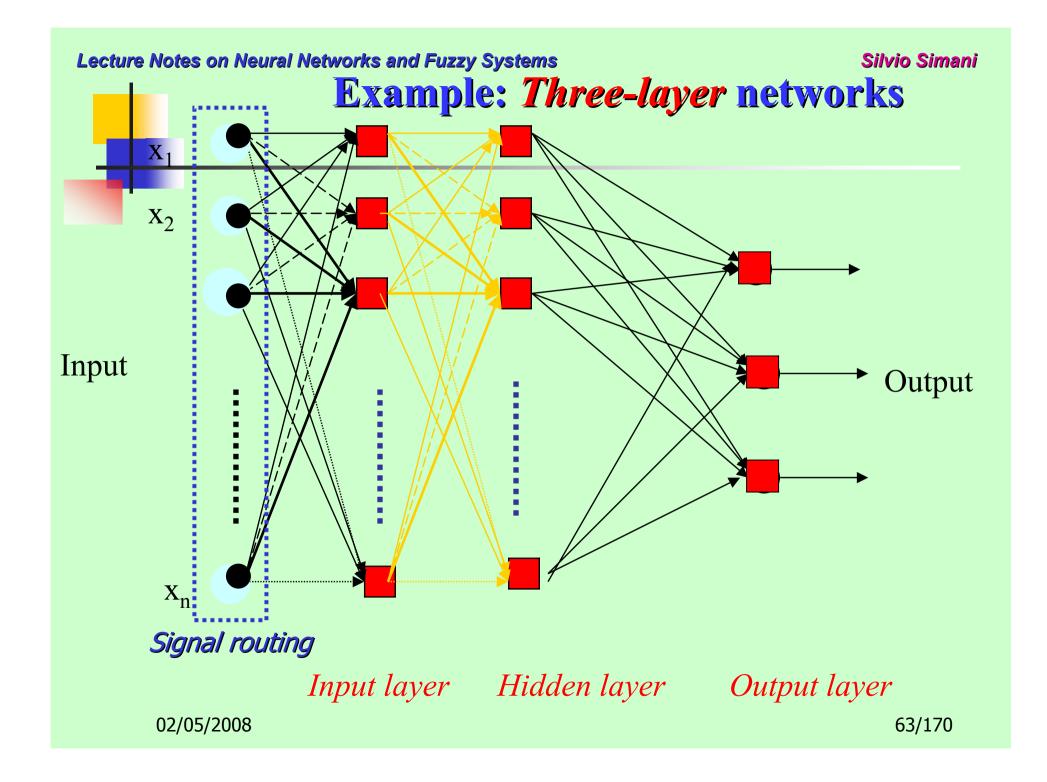
$$\underline{W}(t+1) = \underline{W}(t) + \eta(t) [d(t) - f(\underline{w}(t) \cdot \underline{x})] \underline{x} f'$$



Multi-Layer Perceptron (MLP)

Idea: Credit assignment problem

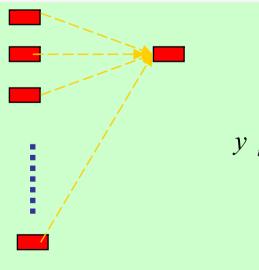
- Problem of assigning 'credit' or 'blame' to individual elements involving in forming overall response of a learning system (hidden units)
- In neural networks, problem relates to dividing which weights should be altered, by how much and in which direction.





Properties of architecture

- No connections within a layer
- No direct connections between input and output layers
- Fully connected between layers
- Often more than 2 layers
- Number of output units need not equal number of input units
- Number of hidden units per layer can be more or less than input or output units



Each unit '
'is a perceptron

$$y_{i} = f(\sum_{j=1}^{m} w_{ij} x_{j} + b_{i})$$

BP (Back Propagation)

gradient descent method



multilayer networks



MultiLayer Perceptron I

Back Propagating Learning

BP learning algorithmSolution to "credit assignment problem" in MLP

Rumelhart, Hinton and Williams (1986)

BP has two phases:

Forward pass phase: computes **'functional signal'**, feedforward propagation of input pattern signals through network

Backward pass phase: computes 'error signal', propagation of error (difference between actual and desired output values) backwards through network starting at output units

BP Learning for Simplest MLPo

Task: Data {I, d} to minimize

$$E = (d - o)^{2} / 2$$

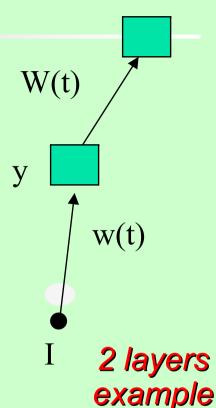
$$= [d - f(W(t)y(t))]^{2} / 2$$

$$= [d - f(W(t)f(w(t)I))]^{2} / 2$$

Error function at the output unit

Weight at time t is w(t) and W(t), intend to find the weight w and W at time t+1

Where y = f(w(t)I), output of the input unit



Forward pass phase



For given input I, we can calculate

$$y = f(w(t)I)$$

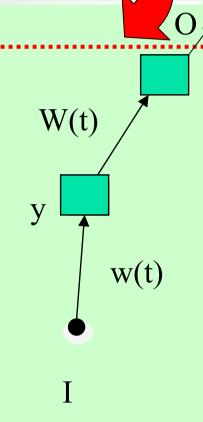
and

$$o = f(W(t) y)$$

= $f(W(t) f(w(t) I))$

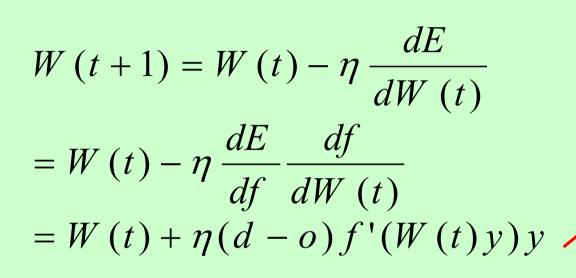
Error function of output unit will be

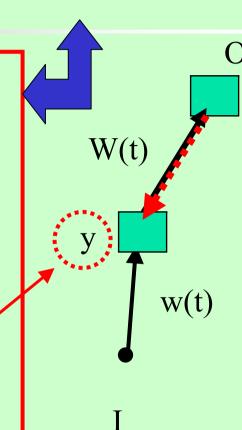
$$E = (d - o)^2/2$$



2 layers example



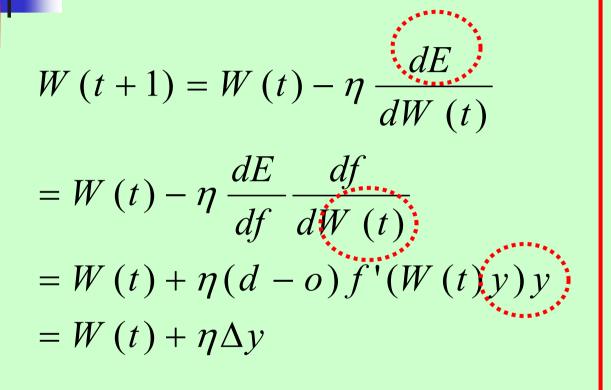


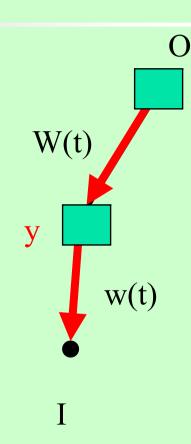


$$E = (d - o)^2 / 2$$

$$o = f(W(t) y)$$

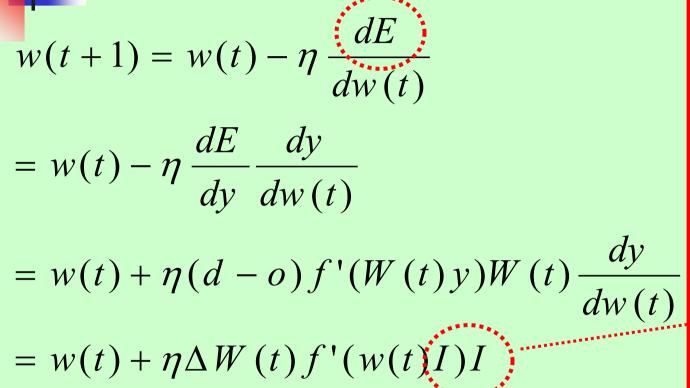


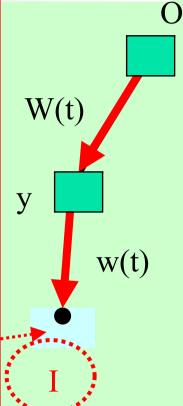




where $\Delta = (d-o)f$

Backward pass phase





$$o = f(W(t) y)$$

$$= f(W(t) f(w(t) I))$$

weight updates are local

$$w_{ji}(t+1) - w_{ji}(t) = \eta \delta_j(t) I_i(t)$$
 (input unit)

$$W_{kj}(t+1) - W_{kj}(t) = \eta \Delta_k(t) y_j(t)$$
 (output unit)

output unit

$$W_{kj}(t+1) - W_{kj}(t) = \eta \Delta_{k}(t) y_{j}(t)$$

$$= \eta (d_{k}(t) - O_{k}(t)) f'(Net_{k}(t)) y_{j}(t)$$

input unit

$$w_{ji}(t+1) - w_{ji}(t) = \eta \delta_{j}(t) I_{i}(t)$$

$$= \eta f'(net_{j}(t)) \sum_{k} \Delta_{k}(t) W_{kj} I_{i}(t)$$

Once weight changes are computed for all units, weights are updated at same time (bias included as weights here)

We now compute the derivative of the activation function f().



to compute δ_j and Δ_k we need to find the derivative of activation function f

>to find derivative the activation function must be smooth

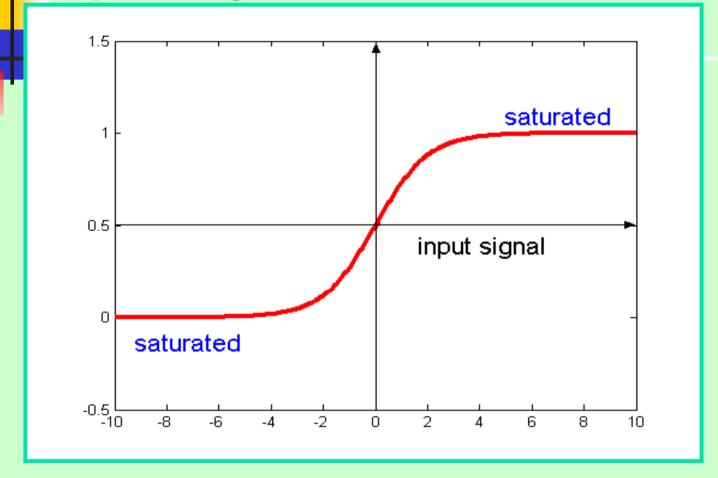
Sigmoidal (logistic) function-common in MLP

$$f(net_i(t)) = \frac{1}{1 + \exp(-knet_i(t))}$$

where k is a positive constant. The sigmoidal function gives value in range of 0 to 1

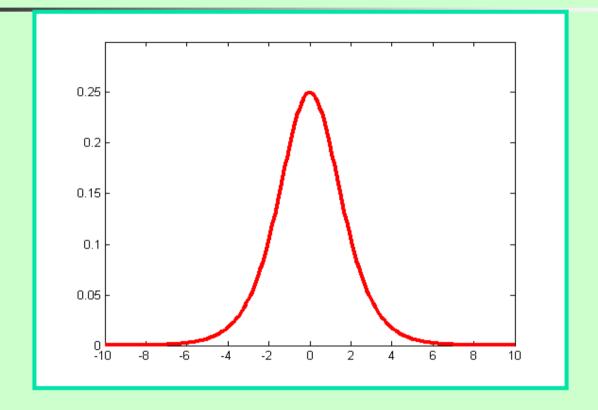
Input-output function of a neuron (rate coding assumption)
02/05/2008 74/170

Lecture Notes on Neural Networks and Fuzzy Systems
Shape of sigmoidal function



Note: when net = 0, f = 0.5





Derivative of sigmoidal function has max at x=0, is symmetric about this point falling to zero as sigmoidal approaches extreme values

02/05/2008

76/170

Returning to local error gradients in BP algorithm we have for output units

$$\Delta_{i}(t) = (d_{i}(t) - O_{i}(t)) f'(Net_{i}(t))$$

$$= (d_{i}(t) - O_{i}(t)) kO_{i}(t)(1 - O_{i}(t))$$

For input units we have

$$\delta_{i}(t) = f'(net_{i}(t)) \sum_{k} \Delta_{k}(t) W_{ki}$$

$$= ky_{i}(t)(1 - y_{i}(t)) \sum_{k} \Delta_{k}(t) W_{ki}$$

Since degree of weight change is proportional to derivative of activation function, weight changes will be greatest when units receives mid-range functional signal than at extremes

Summary of BP learning algorithm

Set learning rate η

Set initial weight values (incl.. biases): w, W

Loop until stopping criteria satisfied:

present input pattern to NN inputs compute functional signal for input units compute functional signal for output units

present Target response to output units compute error signal for output units compute error signal for input units update all weights at same time increment n to n+1 and select next I and d

end loop 02/05/2008

Lecture Notes on Neural Networks and Fuzzy Systems Network training:

- Training set shown repeatedly until stopping criteria are met
- Each full presentation of all patterns = 'epoch'
- Randomise order of training patterns presented for each epoch in order to avoid correlation between consecutive training pairs being learnt (order effects)

Two types of network training:

Sequential mode (on-line, stochastic, or per-pattern)
Weights updated after each pattern is presented

Batch mode (off-line or per -epoch)

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Advantages and disadvantages of different modes

Sequential mode:

- Less storage for each weighted connection
- Random order of presentation and updating per pattern means search of weight space is stochastic-reducing risk of local minima able to take advantage of any redundancy in training set (*i.e.* same pattern occurs more than once in training set, esp. for large training sets)
- Simpler to implement

Batch mode:

Faster learning than sequential mode



MultiLayer Perceptron II

Dynamics of MultiLayer Perceptron

Lecture No Summary of Network Training o Simani

Forward phase: $\underline{I}(t)$, $\underline{w}(t)$, $\underline{net}(t)$, $\underline{y}(t)$, $\underline{W}(t)$, $\underline{Net}(t)$, $\underline{O}(t)$

Backward phase:

Output unit

$$W_{kj}(t+1) - W_{kj}(t) = \eta \Delta_{k}(t) y_{j}(t)$$

= $\eta (d_{k}(t) - O_{k}(t)) f'(Net_{k}(t)) y_{j}(t)$

Input unit

$$w_{ji}(t+1) - w_{ij}(t) = \eta \delta_{j}(t) I_{i}(t)$$

$$= \eta f'(net_{j}(t)) \sum_{k} \Delta_{k}(t) W_{kj}(t) I_{i}(t)$$

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Network training:

Training set shown repeatedly until stopping criteria are met.

Possible convergence criteria are

- \triangleright Euclidean norm of the gradient vector reaches a sufficiently small denoted as θ .
- \triangleright When the absolute rate of change in the average squared error per epoch is sufficiently small denoted as θ .
- ➤ Validation for generalization performance : stop when generalization reaching the peak (illustrate in this lecture)

Goals of Neural Network Training

To give the correct output for input training vector (Learning)

To give good responses to new unseen input patterns (Generalization)



Training and Testing Problems

- Stuck neurons: Degree of weight change is proportional to derivative of activation function, weight changes will be greatest when units receives mid-range functional signal than at extremes neuron. To avoid stuck neurons weights initialization should give outputs of all neurons approximate 0.5
- Insufficient number of training patterns: In this case, the training patterns will be learnt instead of the underlying relationship between inputs and output, i.e. network just memorizing the patterns.
- Too few hidden neurons: network will not produce a good model of the problem.
- Over-fitting: the training patterns will be learnt instead of the underlying function between inputs and output because of too many of hidden neurons. This means that the network will have a poor generalization capability.

Lecture Notes on Neural Networks and Fuzzy Systems

Dynamics of BP learning Airn is to minimise an error function over all training patterns by adapting weights in MLP

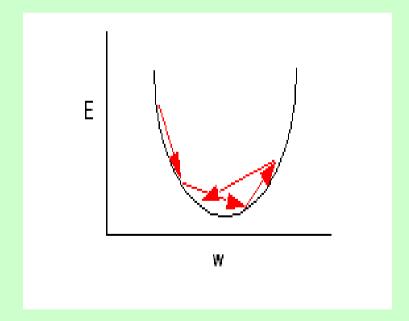
Recalling the typical error function is the mean squared error as follows

$$E(t) = \frac{1}{2} \sum_{k=1}^{p} (d_k(t) - O_k(t))^2$$

The idea is to reduce E(t) to global minimum point.

02/05/2008

In single layer perceptron with linear activation functions, the error function is simple, described by a smooth parabolic surface with a single minimum

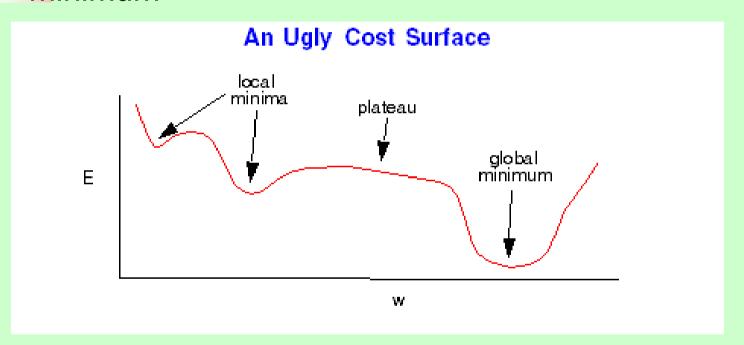


02/05/2008 87/170

Lecture Notes on Neural Networks and Fuzzy Systems

Dynamics of BP learning

MLP with nonlinear activation functions have complex error surfaces (e.g. plateaus, long valleys etc.) with no single minimum



For complex error surfaces the problem is learning rate must keep small to prevent divergence. Adding momentum term is a simple approach dealing with this problem.

02/05/2008 88/170

Momentum

- Reducing problems of instability while increasing the rate of convergence
- Adding term to weight update equation can effectively holds as exponentially weight history of previous weights changed

Modified weight update equation is

$$w_{ij}(n+1) - w_{ij}(n) = \eta \delta_{j}(n) y_{i}(n) + \alpha [w_{ij}(n) - w_{ij}(n-1)]$$

Effect of momentum term

- ➤ If weight changes tend to have same sign momentum term increases and gradient decrease speed up convergence on shallow gradient
- ➤ If weight changes tend have opposing signs momentum term decreases and gradient descent slows to reduce oscillations (stabilizes)
- Can help escape being trapped in local minima

02/05/2008 90/170

Selecting Initial Weight Values

- ➤ Choice of initial weight values is important as this decides starting position in weight space. That is, how far away from global minimum
- ➤ Aim is to select weight values which produce midrange function signals
- Select weight values randomly from uniform probability distribution
- Normalise weight values so number of weighted connections per unit produces midrange function signal

Avoid local minumum with fast convergence:

- Add momentum
- Stochastic gradient descent
- Train multiple nets with different initial weights

Nature of convergence

- Initialize weights 'near zero' or initial networks near-linear
- Increasingly non-linear functions possible as training progresses

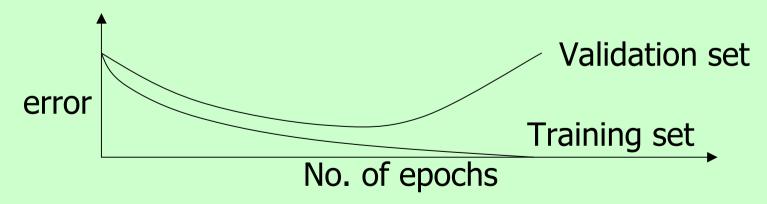
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Use of Available Data Set for Training

The available data set is normally split into three sets as follows:

- Training set use to update the weights. Patterns in this set are repeatedly in random order. The weight update equation are applied after a certain number of patterns.
- Validation set use to decide when to stop training only by monitoring the error.
- Test set Use to test the performance of the neural network. It should not be used as part of the neural network development cycle.

- network and result in overfitting and perform poorly in generalization.
- Keep a hold-out validation set and test accuracy after every epoch. Maintain weights for best performing network on the validation set and stop training when error increases increases beyond this.

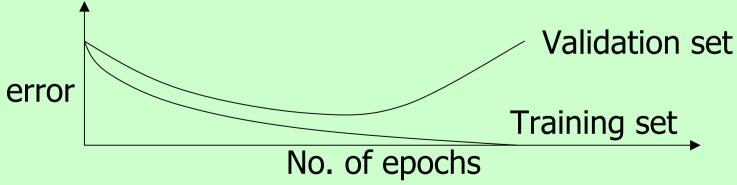


02/05/2008

94/170

Light Notice of Selection by Cross-validation

- learning adequately fitting the data and learning the concept (more than two layer networks).
- Too many hidden units leads to overfitting.
- Similar cross-validation methods can be used to determine an appropriate number of hidden units by using the optimal test error to select the model with optimal number of hidden layers and nodes.



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95/170

Alternative training algorithm



Genetic Algorithms

- Idea of evolutionary computing was introduced in the 1960s by I.
 Rechenberg in his work "Evolution strategies" (Evolutionsstrategie in original). His idea was then developed by other researchers. Genetic
 Algorithms (GAs) were invented by John Holland and developed by him and his students and colleagues. This lead to Holland's book "Adaption in Natural and Artificial Systems" published in 1975.
- In 1992 John Koza has used genetic algorithm to evolve programs to perform certain tasks. He called his method "Genetic Programming" (GP). LISP programs were used, because programs in this language can expressed in the form of a "parse tree", which is the object the GA works

on. _{02/05/2008}

Biological Background

Chromosome.

- All living organisms consist of cells. In each cell there is the same set of **chromosomes**. Chromosomes are strings of <u>DNA</u> and serves as a model for the whole organism. A chromosome consist of **genes**, blocks of DNA. Each gene encodes a particular protein. Basically can be said, that each gene encodes a **trait**, for example color of eyes. Possible settings for a trait (e.g. blue, brown) are called **alleles**. Each gene has its own position in the chromosome. This position is called **locus**.
- Complete set of genetic material (all chromosomes) is called **genome**.
 Particular set of genes in genome is called **genotype**. The genotype is with later development after birth base for the organism's **phenotype**, its physical and mental characteristics, such as eye color, intelligence etc.
 02/05/2008
 98/170

Lecture Notes Birofogical Background Silvio Simani Reproduction.

During reproduction, first occurs recombination (or crossover). Genes from parents form in some way the whole new chromosome. The new created offspring can then be mutated. Mutation means, that the elements of DNA are a bit changed. This changes are mainly caused by errors in copying genes from parents.

 The **fitness** of an organism is measured by success of the organism in its life.

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Evolutionary Computation

- Based on evolution as it occurs in nature
 - Lamarck, Darwin, Wallace: evolution of species, survival of the fittest
 - Mendel: genetics provides inheritance mechanism
 - Hence "genetic algorithms"
- Essentially a massively parallel search procedure
 - Start with random population of individuals
 - Gradually move to better individuals

Replace population by new offspring

02/05/2008

102/170

A Simple Genetic Algorithm

Poptimization task: find the maximum of f(x) for example $f(x)=x \cdot \sin(x)$ $x \in [0,\pi]$

- genotype: binary string $s \in [0,1]^5$ e.g. 11010, 01011, 10001
- mapping : genotype \Rightarrow phenotype $_{n=5}$ binary integer encoding: $x = \pi \bullet \sum_{i=1}^{n} s_i \bullet 2^{n-i-1} / (2^n-1)$

Initial population

genotype	integ.	phenotype	fitness	prop. fitness
11010	26	2.6349	1.2787	30%
01011	11	1.1148	1.0008	24%
10001	17	1.7228	1.7029	40%
00101	5	0.5067	0.2459	6%



Some Other Issues Regarding Evolutionary Computing

Evolution according to Lamarck.

- Individual adapts during lifetime.
- Adaptations inherited by children.
- In nature, genes don't change; but for computations we could allow this...

Baldwin effect.

- Individual's ability to learn has positive effect on evolution.
 - It supports a more diverse gene pool.
 - Thus, more "experimentation" with genes possible.

Bacteria and virus.

New evolutionary computing strategies.

Radial Basis Functions

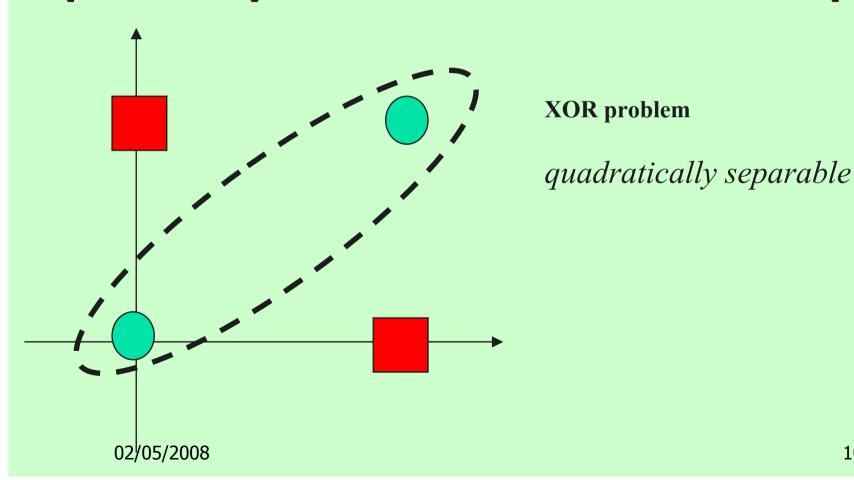


Radial Basis Functions Overview

Lecture Metes on Meural Metworks and Frzzy Systemson (RBF) networks and Frzzy Systemso

RBF = radial-basis function: a function which depends only on the radial distance from a point

106/170



Radial-basis function (RBF) networks and Fuzzy Systems (RBF) networks So RBFs are functions taking the form

$$\phi (\parallel \underline{x} - \underline{x}_i \parallel)$$

where ϕ is a nonlinear activation function, \underline{x} is the input and \underline{x}_i is the *i'th* position, prototype, *basis* or *centre* vector.

The idea is that points near the centres will have similar outputs (i.e. if $\underline{x} \sim \underline{x}i$ then $f(\underline{x}) \sim f(\underline{x}i)$) since they should have similar properties.

The simplest is the linear RBF : $\phi(x) = ||\underline{x} - \underline{x}_i||$

02/05/2008 107/170



Multiquadrics

$$\phi(r) = (r^2 + c^2)^{1/2}$$

for some c>0

(b) Inverse multiquadrics

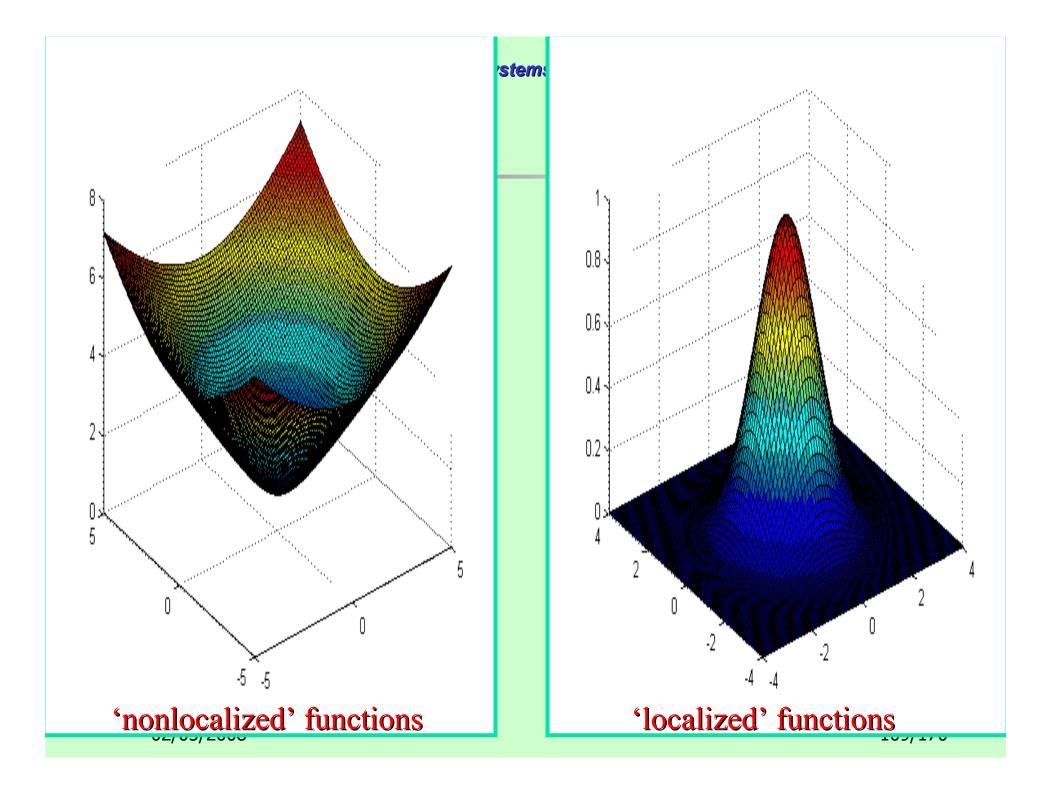
$$\phi(r) = (r^2 + c^2)^{-1/2}$$

for some c>0

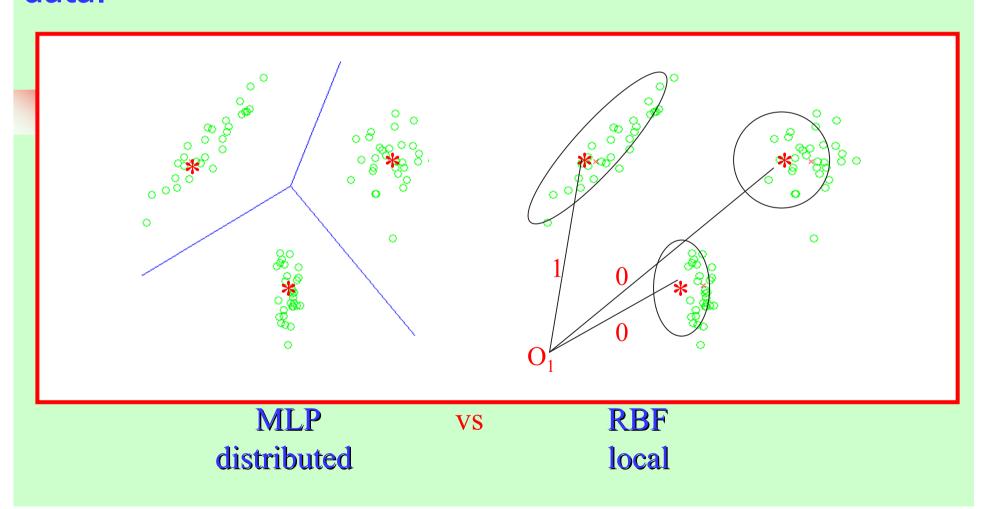
(c) Gaussian

$$\phi(r) = \exp(-\frac{r^2}{2\sigma^2})$$

for some $\sigma > 0$

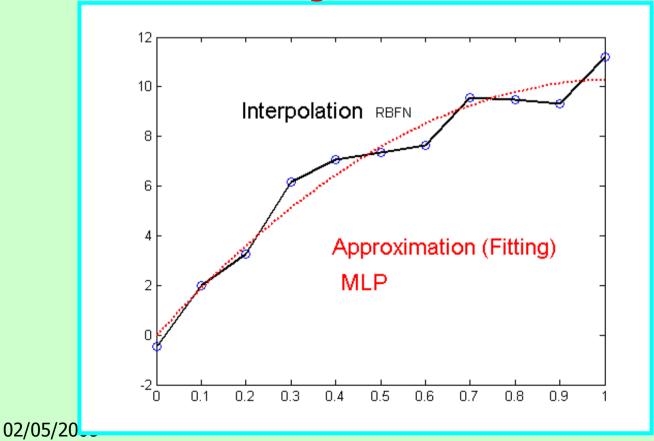


- ➤ Idea is to use a weighted sum of the outputs from the basis functions to represent the data.
- ➤ Thus centers can be thought of as prototypes of input data.



Starting point: exact interpolation

Each input pattern x must be mapped onto a target value d



That is, given a set of N vectors \underline{X}_i and a corresponding set of N real numbers, d_i (the targets), find a function F that satisfies the interpolation condition:

$$F(\underline{x}_i) = d_i$$
 for $i = 1,...,N$

or more exactly find:

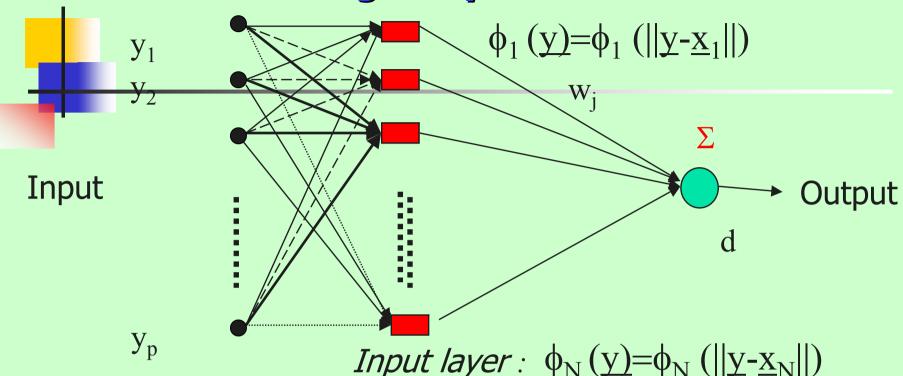
$$F(\underline{x}) = \sum_{j=1}^{N} w_j \phi(||\underline{x} - \underline{x}_j||)$$

satisfying:

$$F(\underline{x}_i) = \sum_{j=1}^N w_j \phi(||\underline{x}_i - \underline{x}_j||) = d_i$$

Lecture Notes on Neural NetworkSingles and NetworkS

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- output = $\sum W_i \phi_i (\underline{Y} \underline{X}_i)$
- adjustable parameters are weights w_i
- number of input units ≤ number of data points
- Form of the basis functions decided in advance

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113/170

To summarize:

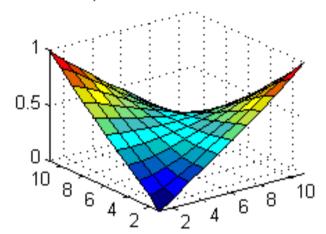
For a given data set containing N points (\underline{x}_i, d_i) , i=1,...,N

- Choose a RBF function ϕ
- Calculate $\phi(\underline{x}_i \underline{x}_i)$
- Solve the <u>linear</u> equation $\Phi W = D$
- Get the unique solution
- Done
- Like MLP's, RBFNs can be shown to be able to approximate any function to arbitrary accuracy (using an arbitrarily large numbers of basis functions).
- ➤ Unlike MLP's, however, they have the property of 'best approximation' i.e. there exists an RBFN with minimum approximation error.

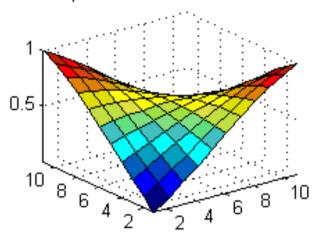


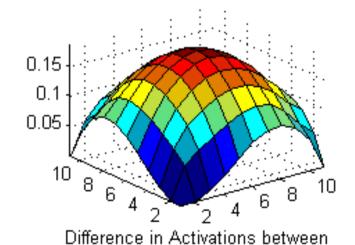
Large $\sigma = 1$



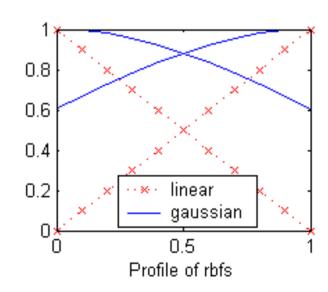


Outputs from Gaussian Rbf Net

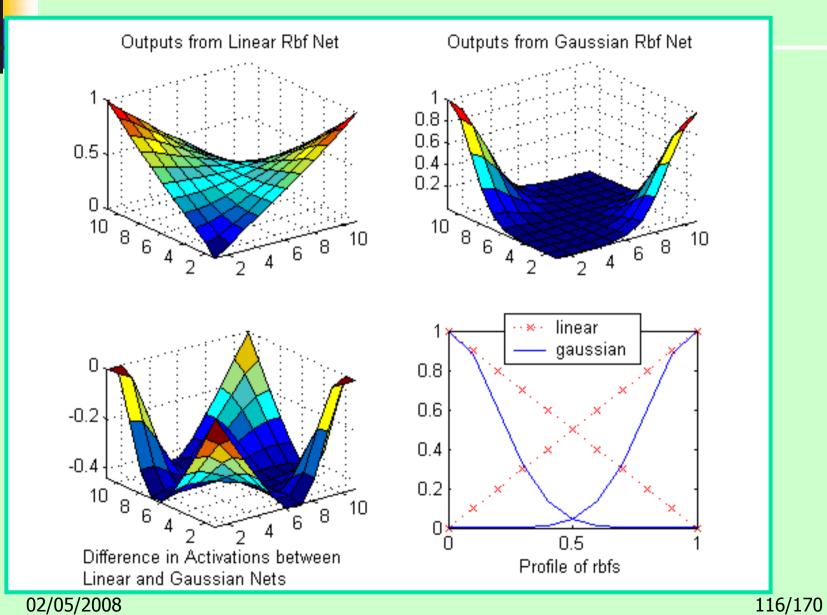




Linear and Gaussian Nets



Small $\sigma = 0.2$



Problems With exact interpolation

can produce poor generalisation performance as only data

points constrain mapping

Overfitting problem

Bishop(1995) example

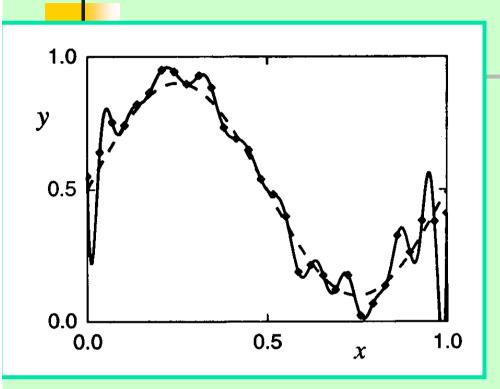
Underlying function f(x)=0.5+0.4sine $(2\pi x)$ sampled randomly for 30 points

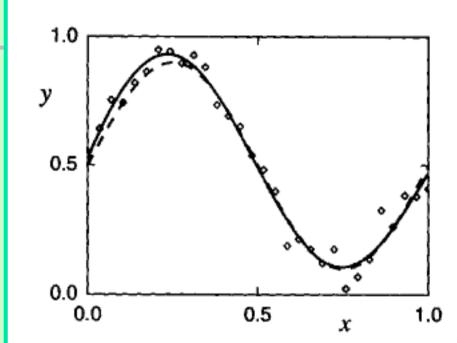
added Gaussian noise to each data point

30 data points 30 hidden RBF units

fits all data points but creates oscillations due added noise and unconstrained between data points

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All Data Points

5 Basis functions

To fit an RBF to every data point is very inefficient due to the computational cost of matrix inversion and is very bad for generalization so:

- ✓ Use less RBF's than data points I.e. M<N</p>
- ✓ Therefore don't necessarily have RBFs centred at data points
- ✓ Can include bias terms
- ✓ Can have Gaussian with general covariance matrices but there is a trade-off between complexity and the number of parameters to be found eg for *d* rbfs we have:



Fuzzy Clustering with Applications in Data-Driven Modelling



- The ability to cluster data (concepts, perceptions, etc.)
 - essential feature of human intelligence.
- > A cluster is a set of objects that are more similar to each other than to objects from other clusters.
- Applications of clustering techniques in pattern recognition and image processing.
- Some machine-learning techniques are based on the notion of similarity (decision trees, case-based reasoning)
- Non-linear regression and black-box modelling can be based on the partitioning data into clusters.

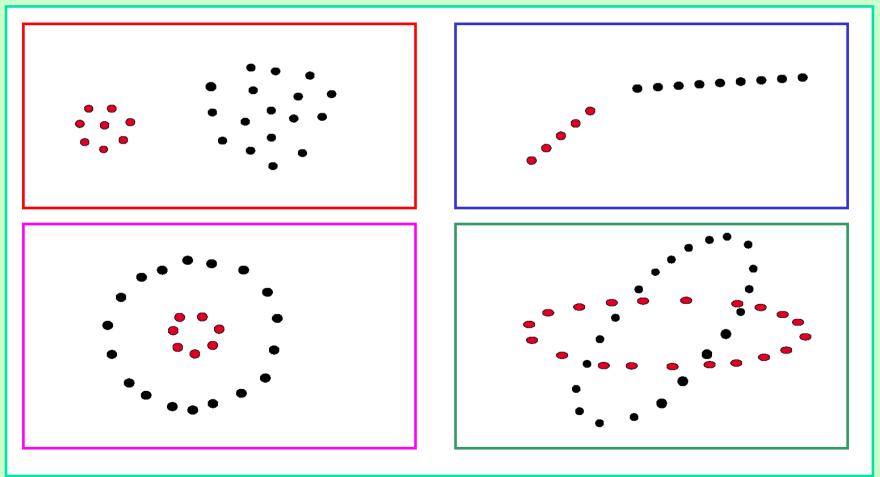


Section Outline

- > Basic concepts in clustering
 - data set
 - partition matrix
 - distance measures
- > Clustering algorithms
 - fuzzy c-means
 - Gustafson–Kessel
- > Application examples
 - system identification and modeling
 - diagnosis



Examples of Clusters



02/05/2008

123/170



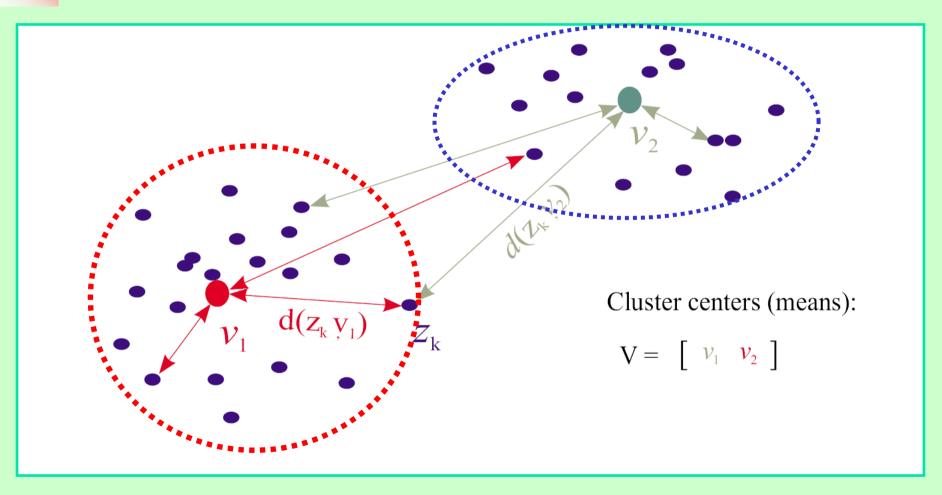
Problem Formulation

- ➢ Given is a set of data in Rⁿ and the (estimated) number of clusters to look for (a difficult problem, more on this later).
- ➤ Find the partitioning of the data into subsets (clusters), such that samples within a subset are more similar to each other than to samples from other subsets.
- Similarity is mathematically formulated by using a distance measure (i.e., a dissimilarity function).
- ➤ Usually, each cluster will have a prototype and the distance is measured from this prototype.

02/05/2008 124/170



Distance Measure





Distance Measures

> Euclidean norm:

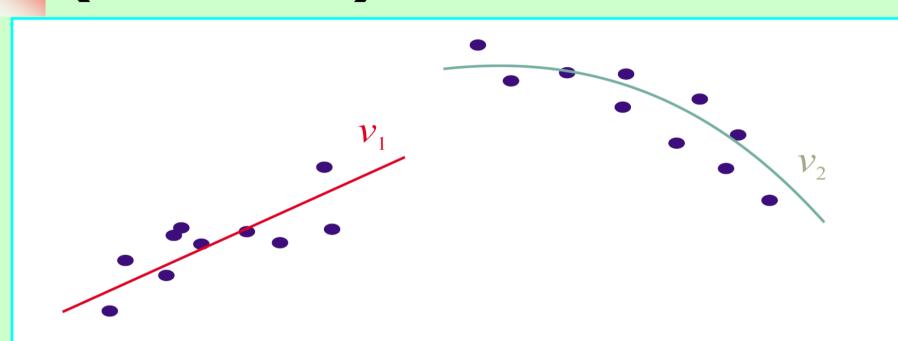
$$d^{2}(\mathbf{z}_{j}, \mathbf{v}_{i}) = (\mathbf{z}_{j} - \mathbf{v}_{i})^{T} (\mathbf{z}_{j} - \mathbf{v}_{i})$$

>Inner-product norm:

$$d^{2}\mathbf{A}_{i}(\mathbf{z}_{j}, \mathbf{v}_{i}) = (\mathbf{z}_{j} - \mathbf{v}_{i})^{T}\mathbf{A}_{i}(\mathbf{z}_{j} - \mathbf{v}_{i})$$

> Many other possibilities . . .

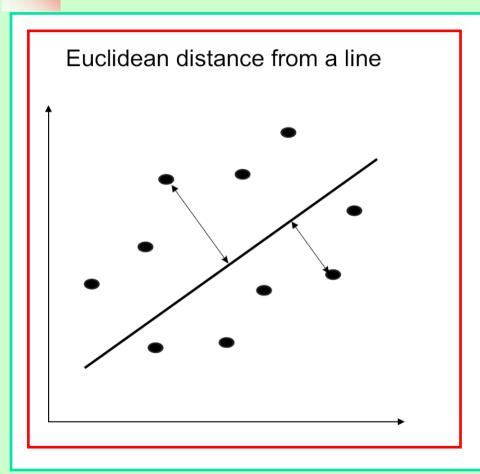
Generalized Prototypes (Varieties)

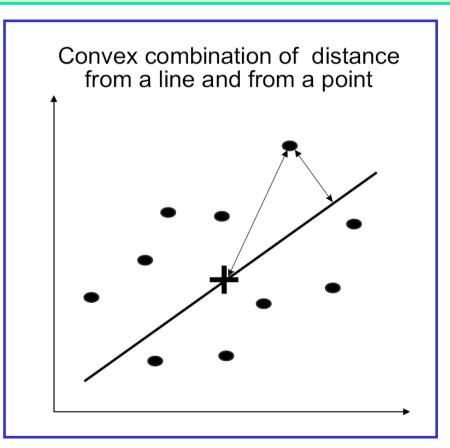


lines, circles, ellipses, regression functions, etc.

02/05/2008 127/170

Lecture Not Gorresponding Distance vio Simani Measures





02/05/2008 128/170

Lecture Not Mathematical Formulation in of Clustering

Given the data:

$$\mathbf{z}_k = [z_{1k}, z_{2k}, ..., z_{nk}]^T \in \mathbb{R}^n, k = 1, ..., N$$

Find:

the partition matrix:

$$\mathbf{U} = \begin{bmatrix} \mu_{11} & \cdots & \mu_{1k} & \cdots & \mu_{1N} \\ \vdots & \cdots & \vdots & \cdots & \vdots \\ \mu_{c1} & \cdots & \mu_{ck} & \cdots & \mu_{cN} \end{bmatrix}$$

and the cluster prototype (centres):

$$\mathbf{V} = \{\mathbf{v}_1, \ \mathbf{v}_2, \ \dots, \ \mathbf{v}_c\}, \ \mathbf{v}_i \in \mathbb{R}^n$$

Lecture Note FUPZaZeY pri Con Ustering: an **Optimisation Approach**

> Objective function (least-squares criterion):

$$J(\mathbf{Z}; \mathbf{V}, \mathbf{U}, \mathbf{A}) = \sum_{i=1}^{c} \sum_{j=1}^{N} \mu_{i,j}^{m} d_{\mathbf{A}_{i}}^{2}(\mathbf{z}_{j}, \mathbf{v}_{i})$$

> subject to constraints:

$$0 \le \mu_{i,j} \le 1,$$
 $i=1,\ldots,c,\ j=1,\ldots,N$ membership degree $0 < \sum_{j=1}^N \mu_{i,j} < 1,$ $i=1,\ldots,c$ no cluster empty
$$\sum_{i=1}^c \mu_{i,j} = 1,$$
 $j=1,\ldots,N$ total membership

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Fuzzy c-Means Algorithm

Repeat:

1. Compute cluster prototypes (means):

$$v_i = \frac{\sum_{k=1}^{N} \mu_{i,k}^m \mathbf{z}_k}{\sum_{k=1}^{N} \mu_{i,k}^m}$$

2. Calculate distances:

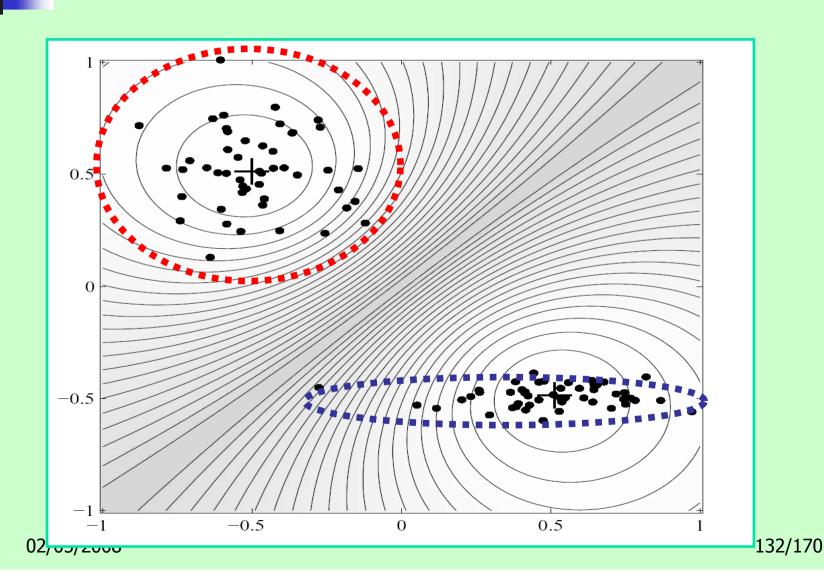
$$d_{ik} = (\mathbf{z}_k - \mathbf{v}_i)^T (\mathbf{z}_k - \mathbf{v}_i)$$

3. Update partition matrix:

$$\mu_{ik} = \frac{1}{\sum_{j=1}^{c} (d_{ik}/d_{jk})^{1/(m-1)}}$$

until
$$\|\Delta \mathbf{U}\| < \epsilon$$

Lecture Note Fatilitires to Discover Non- Silvio Simani Spherical Clusters



Lecture Note Adaptive 22 Distance Measure

>Inner-product norm:

$$d_{\mathbf{A}_i}^2(\mathbf{z}_j, \mathbf{v}_i) = (\mathbf{z}_j - \mathbf{v}_i)^T \mathbf{A}_i (\mathbf{z}_j - \mathbf{v}_i)$$

ightharpoonup norm-inducing matrix $\mathbf{A}_i = \rho_i \det(\mathbf{F}_i)^{1/n} \mathbf{F}_i^{-1}$

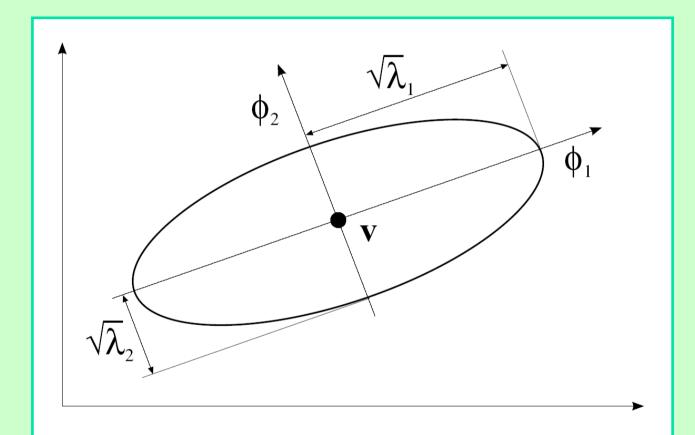
$$\mathbf{A}_i = \rho_i \det(\mathbf{F}_i)^{1/n} \mathbf{F}_i^{-1}$$

> covariance matrix

$$\mathbf{F}_i = \frac{\sum_{k=1}^{N} \mu_{ik}^m (\mathbf{z}_k - \mathbf{v}_i) (\mathbf{z}_k - \mathbf{v}_i)^T}{\sum_{k=1}^{N} \mu_{ik}^m}$$



Inner-Product Norm



ellipsoid: $(\mathbf{z} - \mathbf{v})^T \mathbf{F}^{-1} (\mathbf{z} - \mathbf{v}) = \text{const}$

Gustafson-Kessel Algorithm

Repeat:

- 1. Compute cluster prototypes (means):
- $v_i = \frac{\sum_{k=1}^{N} \mu_{i,k}^m \mathbf{z}_k}{\sum_{k=1}^{N} \mu_{i,k}^m}$

2. Compute covariance matrices:

$$\mathbf{F}_i = \frac{\sum_{k=1}^N \mu_{ik}^m (\mathbf{z}_k - \mathbf{v}_i) (\mathbf{z}_k - \mathbf{v}_i)^T}{\sum_{k=1}^N \mu_{ik}^m}$$

3. Compute distances:

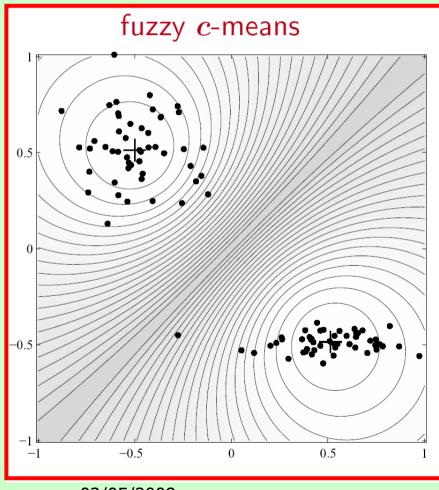
distances:
$$d_{ik} = (\mathbf{z}_k - \mathbf{v}_i)^T \rho_i \det(\mathbf{F}_i)^{1/n} \mathbf{F}_i^{-1} (\mathbf{z}_k - \mathbf{v}_i)$$

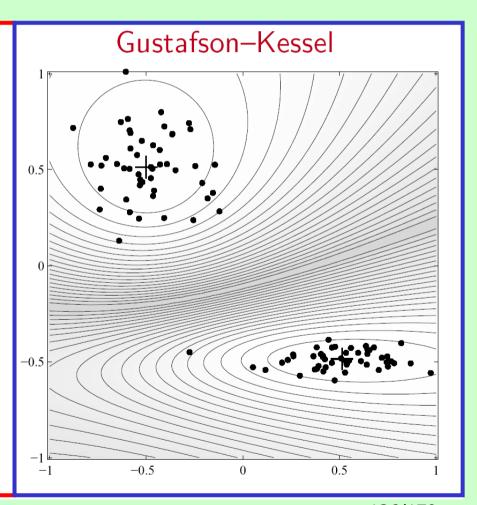
4. Compute partition matrix:

until
$$\|\Delta \mathbf{U}\| < \epsilon$$

$$\mu_{ik} = \frac{1}{\sum_{j=1}^{c} (d_{ik}/d_{jk})^{1/(m-1)}}$$

Clusters of Different Shape and Orientation





02/05/2008

136/170



Number of Clusters

Validity measures

Fuzzy hypervolume:

$$V_h = \sum_{i=1}^c [\det(\mathbf{F}_i)]^{1/2}$$

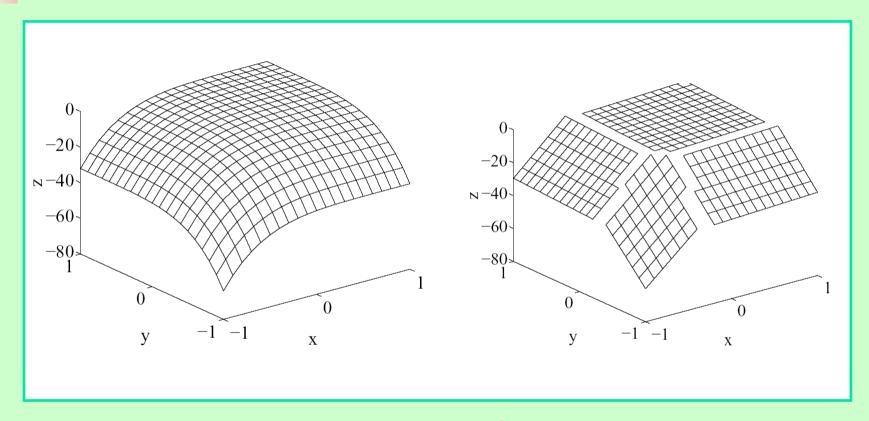
Average within-cluster distance:

Xie Beni index . . .

$$D_w = \frac{1}{c} \sum_{i=1}^{c} \frac{\sum_{k=1}^{N} \mu_{ik}^m D_{ik}^2}{\sum_{k=1}^{N} \mu_{ik}^m}$$



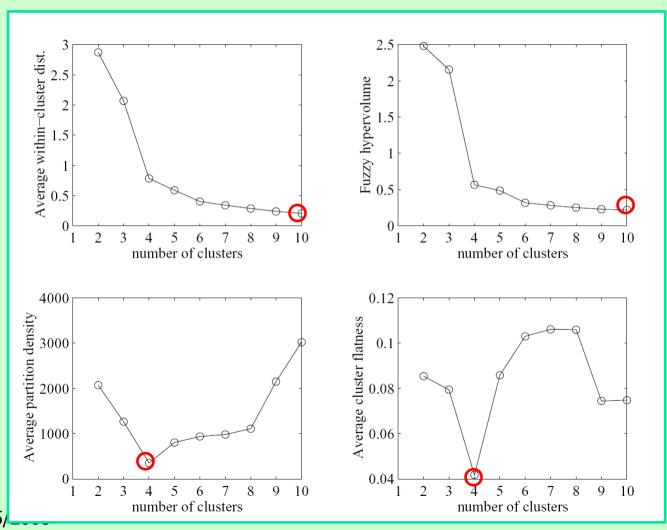
Validity Measures: Example



Data over 4 clusters

02/05/2008 138/170

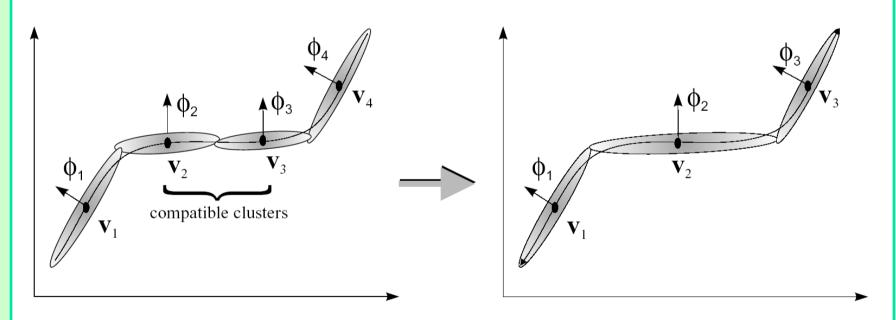
Validity Measures





Number of Clusters

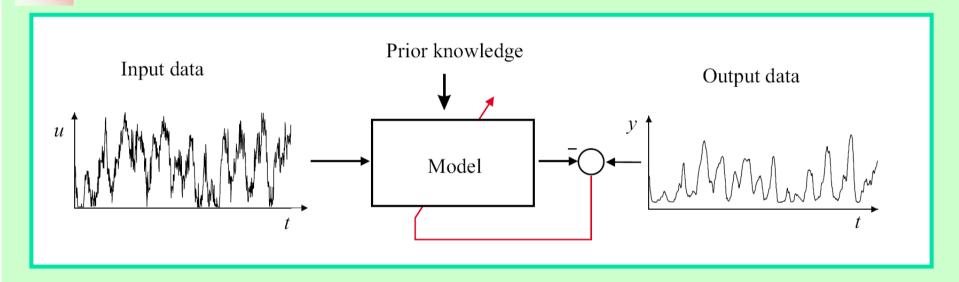
Compatible cluster merging



$$|\Phi_i \cdot \Phi_j| \ge k_1$$
, $k_1 \to 1$ and $||v_i - v_j|| \le k_2$, $k_2 \to 0$

02/05/2008 140/170

Lecture Not Data-Drivens (Black-Boxiv) Simani Modelling

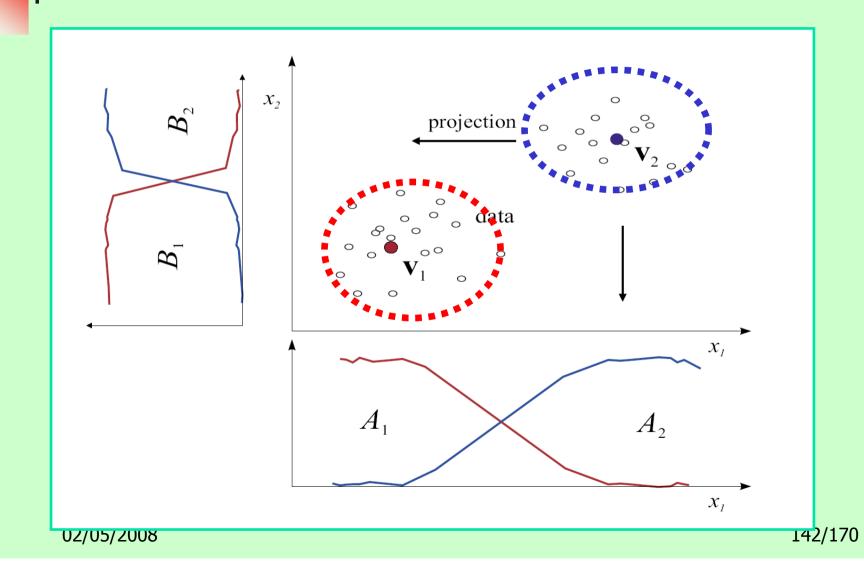


- > Linear model (for linear systems only, limited in use)
- > Neural network (black box, unreliable extrapolation)
- Rule-based model (more transparent, 'grey-box')

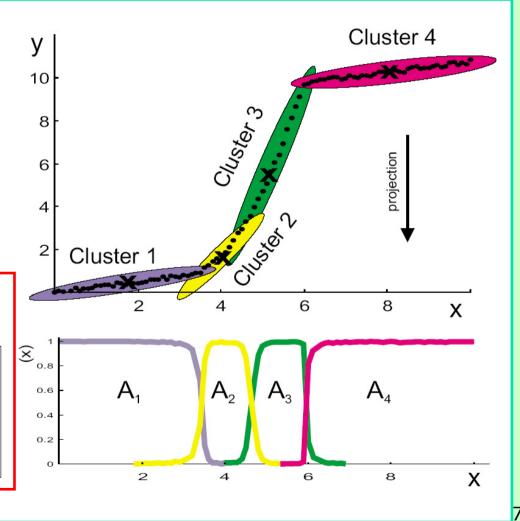
02/05/2008

Fuzzy Clustering

Silvio Simani



Fuzzy Clustering



Takagi-Sugeno model

Rule-based description:

If x is A_1 then y = $a_1x + b_1$ If x is A_2 then y = $a_2x + b_2$

etc...

Example: Non-linear Autoregressive System (NARX)

$$x(k+1) = f(x(k)) + \epsilon(k)$$

$$f(x) = \begin{cases} 2x - 2, & 0.5 < x \\ -2x, & -0.5 \le x < 0.5 \\ 2x + 2, & x \le -0.5 \end{cases}$$

Lecture NoteStructure: Selection and ilvio simani Data Preparation

1. Choose model order p

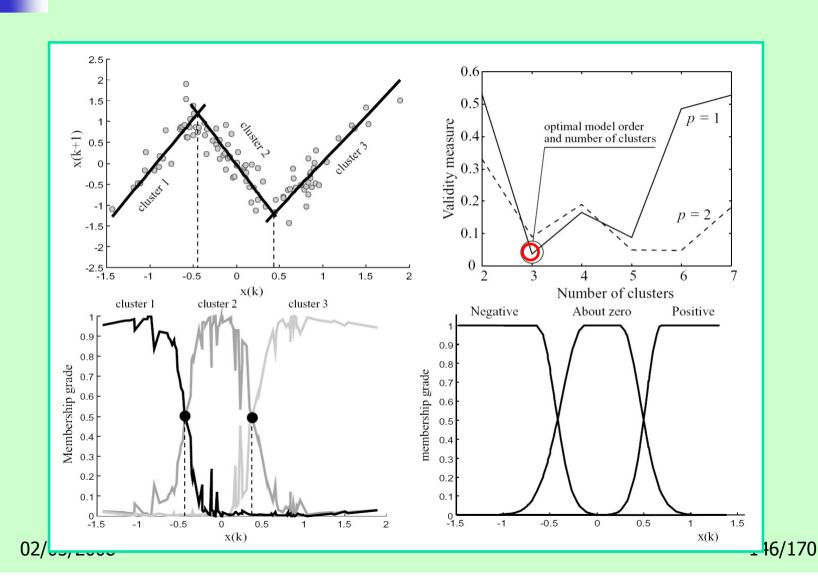
$$x(k+1) = f(\underbrace{x(k), x(k-1), \dots, x(k-p+1)}_{\mathbf{x}(k)})$$

Form pattern matrix Z to be clustered

$$\mathbf{Z}^T = \begin{bmatrix} x(1) & x(2) & \dots & x(p) & x(p+1) \\ x(2) & x(3) & \dots & x(p+1) & x(p+2) \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ x(N-p) & x(N-p+1) & \dots & x(N-1) & x(N) \end{bmatrix}$$

02/05/2008 145/170

Clustering Results



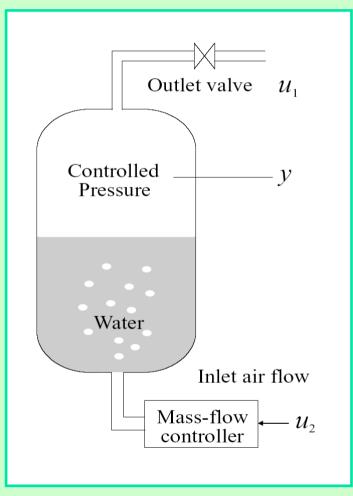


Rules Obtained

- 1) If x(k) is Positive then x(k+1) = 2.0244x(k) 2.0289
- 2) If x(k) is About zero then x(k+1) = -1.8852x(k) + 0.0005
- 3) If x(k) is Negative then x(k+1) = 1.9050x(k) + 1.9399

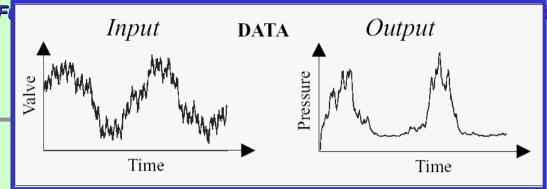
original function: $f(x) = \begin{cases} 2x - 2, & 0.5 < x \\ -2x, & -0.5 \le x < 0.5 \\ 2x + 2, & x \le -0.5 \end{cases}$

Lecture Note I dentification of Pressurement Dynamics



02/05/2008 148/170



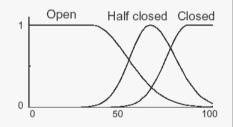




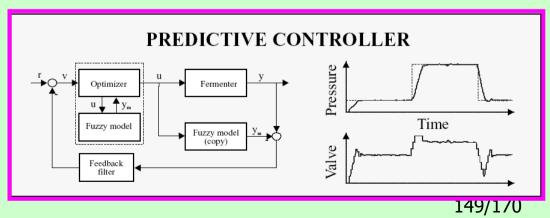
Rules FUZZY MODEL

Membership f.

- 1) If Valve is Open and Pressure is Low then
- 2) If Valve is Closed and Pressure is High then
- 3) ...









Concluding Remarks

> Optimisation approach to clustering

- ✓ effective for metric (e.g., real-valued) data
- ✓ accurate results for small to medium complexity problems
- ✓ for large problems, convergence to local optima, slow

> Many other techniques

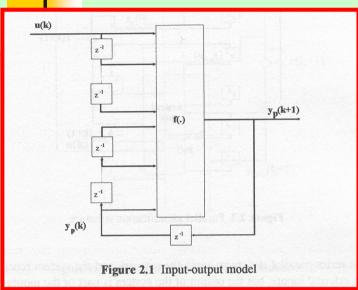
- ✓ agglomerative methods
- ✓ hierarchical splitting methods
- ✓ graph-theoretic methods
- > Variety of applications

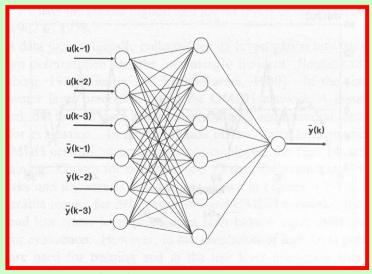


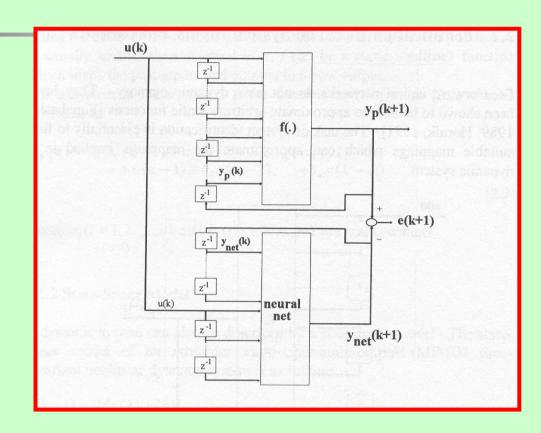
Application Examples

Neural Networks for Non-linear Identification, Prediction and Control

Nonlinear System Identification







Target function:

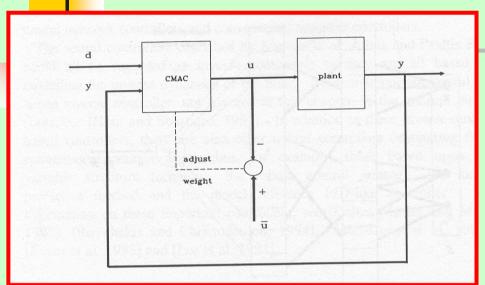
Target function: $y_p(k+1) = f(.)$ Identified function: $y_{NET}(k+1) = F(.)$

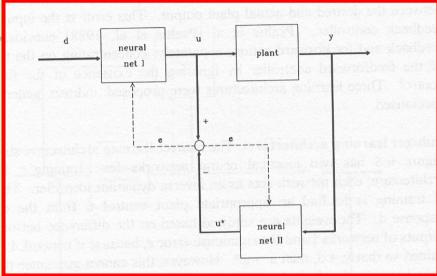
Estimation error: e(k+1)

02/05/2008

152/170

Lect Nonthear's System Neural Control"





d: reference/desired response

y: system output/desired output

u: system input/controller output

ū: desired controller input

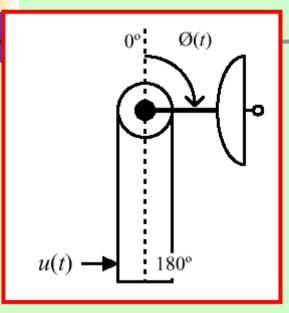
u*: NN output

e: controller/network error

The goal of training is to find an appropriate plant control u from the desired response d. The weights are adjusted based on the difference between the outputs of the networks I & II to minimise e. If network I is trained so that y = d, then $u = u^*$. Networks act as inverse dynamics identifiers.

Lecture Notes on Neural Networks and Fuzzy Systems

Nonlinear System Identification



<u>02| 03| 2000</u>

$$\frac{d}{dt} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} x_2 \\ 9.81 \sin x_1 - 2x_2 + u \end{bmatrix}$$

$$x_1 = \emptyset$$

$$x_2 = \frac{d\emptyset}{dt}$$

```
deg2rad = pi/180;
angle = [-20:40:200]*deg2rad;
ve1 = [-90:36:90]*deg2rad;
force = -30:6:30:
```

```
ang1e2 = [-20:10:200]*deg2rad;
Pm = [combvec(angle, vel, force);
  [angle2; zeros(2,length(angle2))]];
```

Neural network input generation Pm



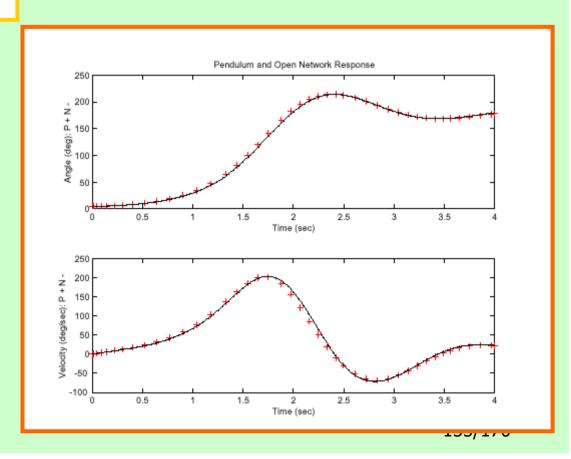
Nonlinear System Identification

```
S1 = 8;
[S2,Q] = size(Tm);
mnet = newff(minmax(Pm),[S1 S2],{'tansig' 'purelin'},'trainlm');
```

```
mnet.trainParam.goa1 = (0.0037^2);
mnet = train(mnet,Pm,Tm);
```

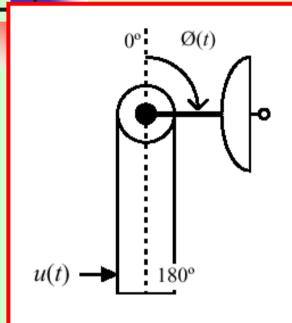
Neural network target
Tm

Neural network response (angle & velocity)





Model Reference Control



$$\frac{d}{dt} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} x_2 \\ 9.81 \sin x_1 - 2x_2 + u \end{bmatrix}$$

$$x_1 = \emptyset$$

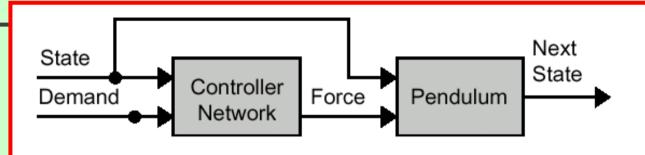
$$x_2 = \frac{d\emptyset}{dt}$$

Antenna arm nonlinear model

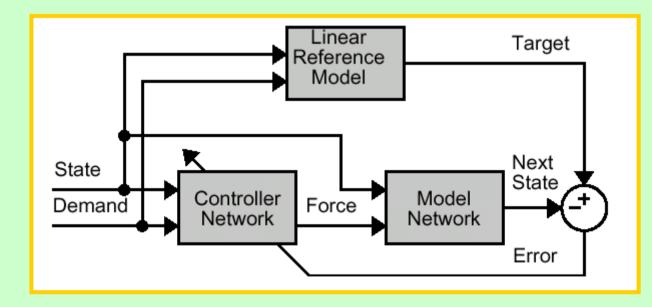
Linear reference model

$$\frac{d}{dt} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} x_2 \\ -9x_1 - 6x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 9r \end{bmatrix}$$

Model Reference Control

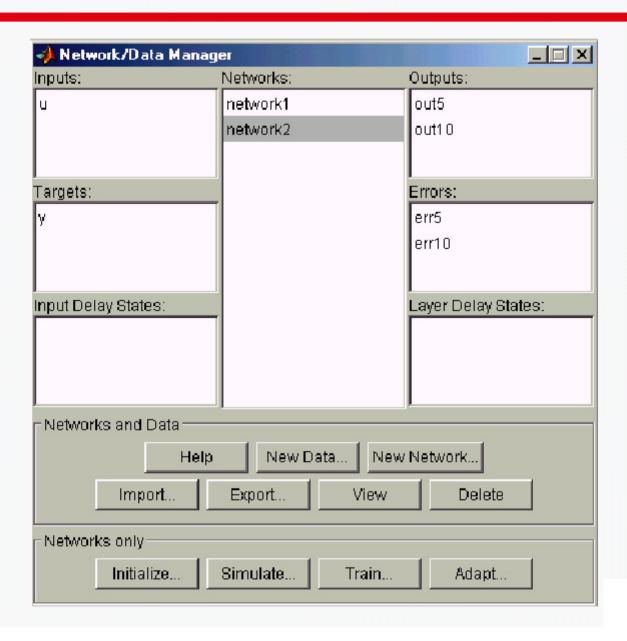


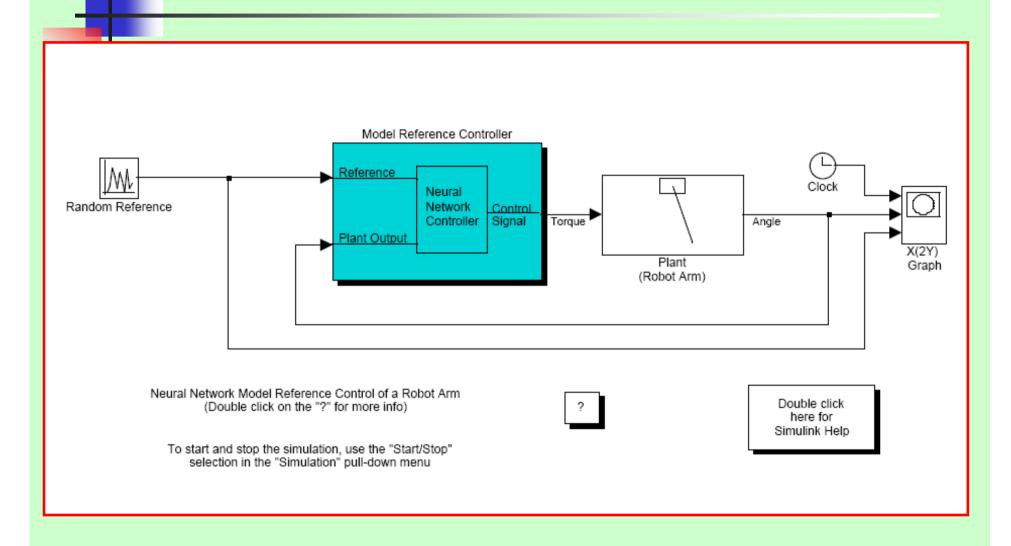
Neural controller + nonlinear system diagram



Neural controller, reference model, neural model 02/05/2008

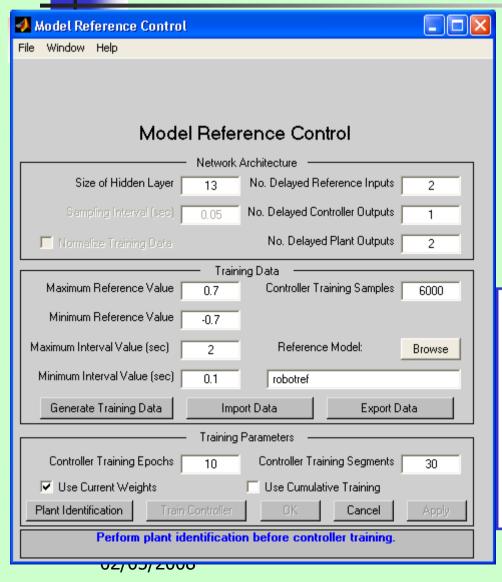
Matlab NNtool GUI (Graphical User Interface)

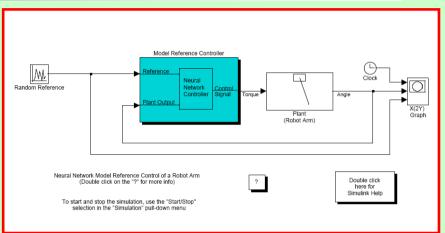


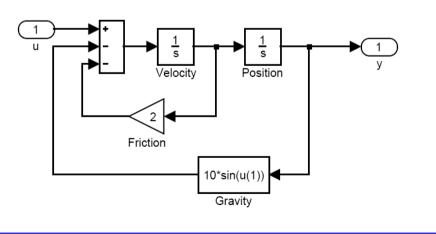


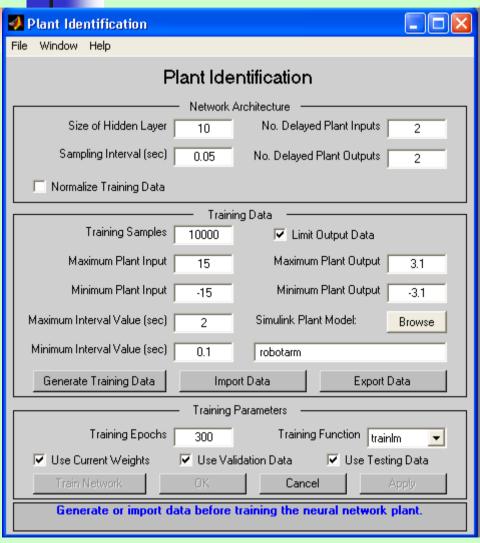
02/05/2008 159/170

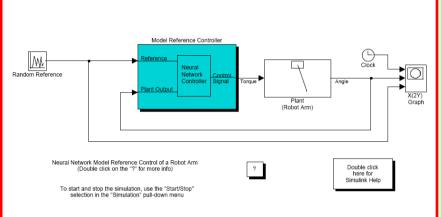












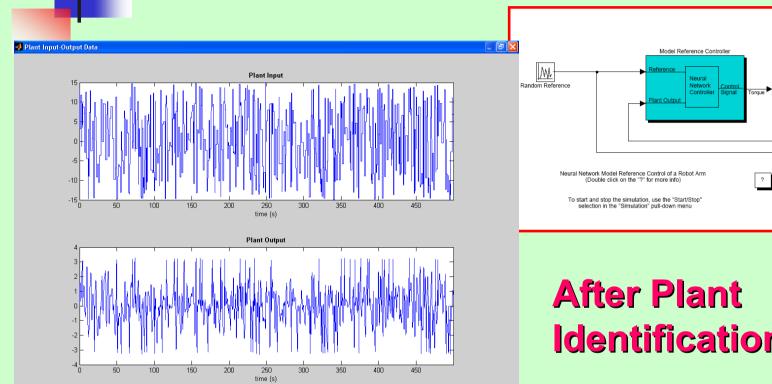
Plant Identification:

Data generation from the Reference Model for Neural Network training

02/05/2008 161/170

Accept Data Reject Data Please Accept or Reject Data to con

Control of a Robot Arm Example

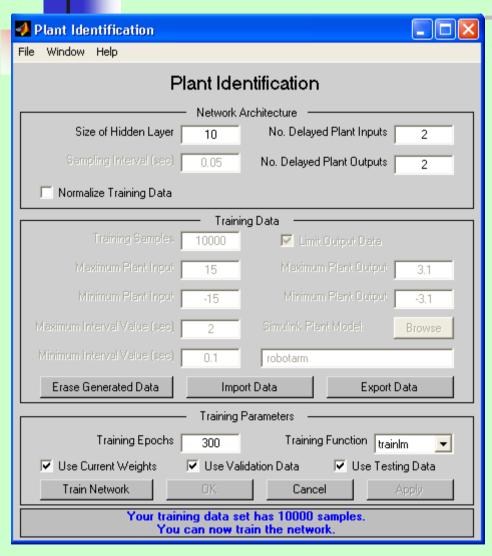


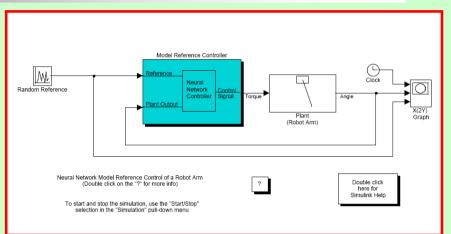
Identification:

Neural Network training

162/170 02/05/2008



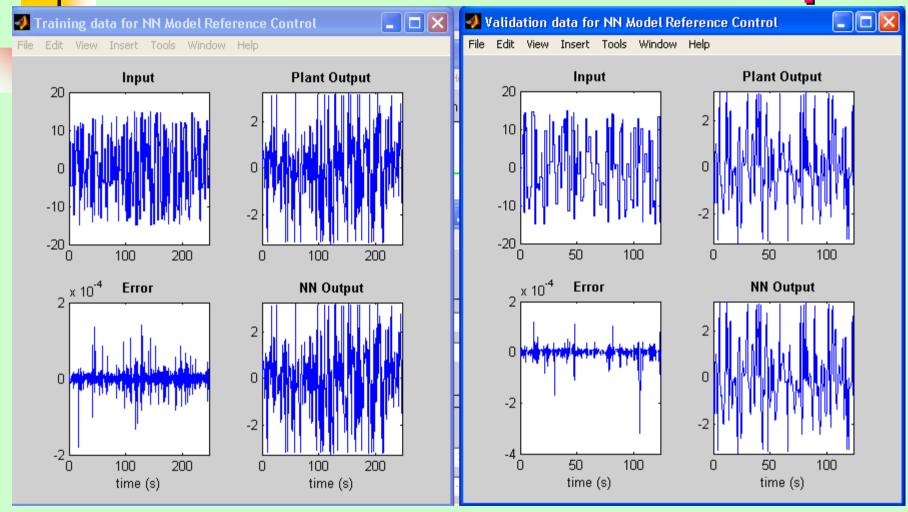




After Plant Identification:

Neural Network training

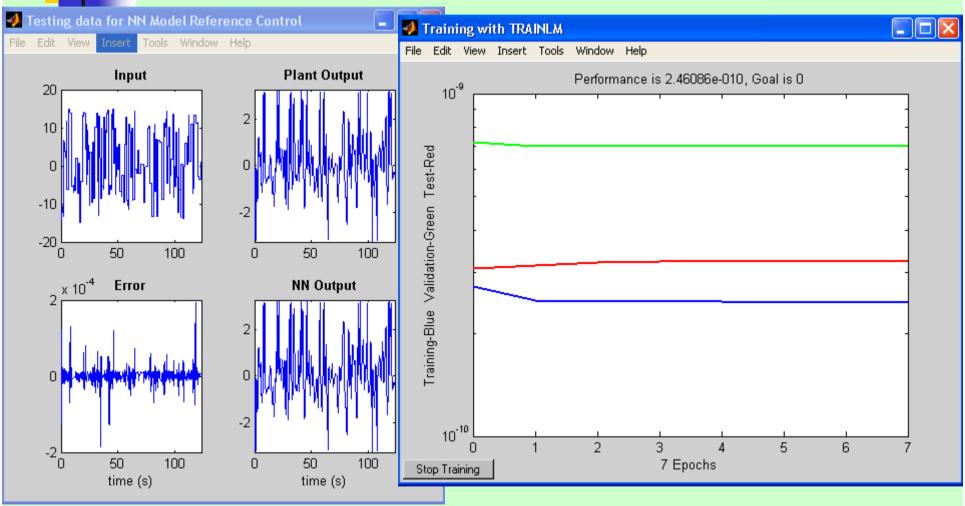
02/05/2008 163/170



Training and Validation Data

02/05/2008 164/170





Testing Data and Training Results

02/05/2008

165/170

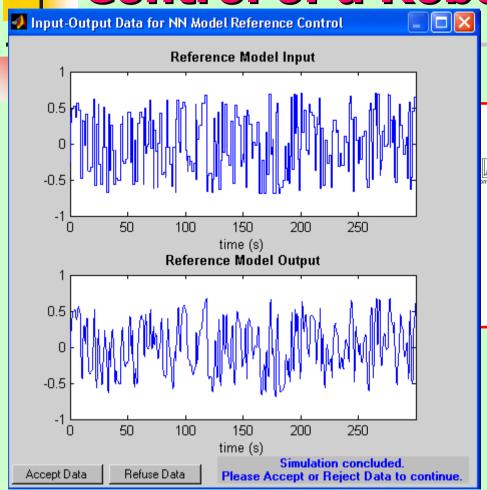
Model Reference Contro	ol			<		
File Window Help						
Model Reference Control						
Network Architecture —						
Size of Hidden Layer	13	No. Delayed Reference Inputs 2				
Sampling Interval (sec)	0.05	0.05 No. Delayed Controller Outputs 1				
Normalize Training Data		No. Delayed Plant Outputs 2				
Training Data —						
Maximum Reference Value	0.7	Controller T	Fraining Samples 6000	ı		
Minimum Reference Value	-0.7	Defines how many data points will be generat				
Maximum Interval Value (sec)	2	Reference Model: Browse				
Minimum Interval Value (sec)	0.1	robotref				
Generate Training Data	Imp	ort Data	Export Data			
Training Parameters —						
Controller Training Epochs	10	Controller Tr	aining Segments 30			
✓ Use Current Weights	Use Cumulative Training					
Plant Identification Tra	in Controller	OK.	Cancel Apply			
Generate or import data before training the neural network controller.						

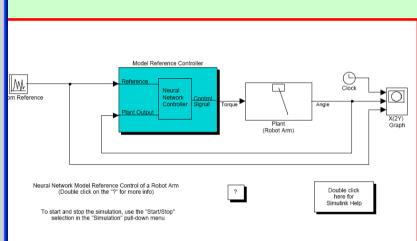
Random Reference	Reference Controller Reference Neural Network Controller Signal Torque Plant Output Plant (Robot Arm)	Angle X(2Y) Graph
Neural Network Model Reference Control of a Robot Arm (Double click on the "?" for more info) To start and stop the simulation, use the "Start/Stop" selection in the "Simulation" pull-down menu		

Plant identification with a NN

Data Generation for NN Controller Identification

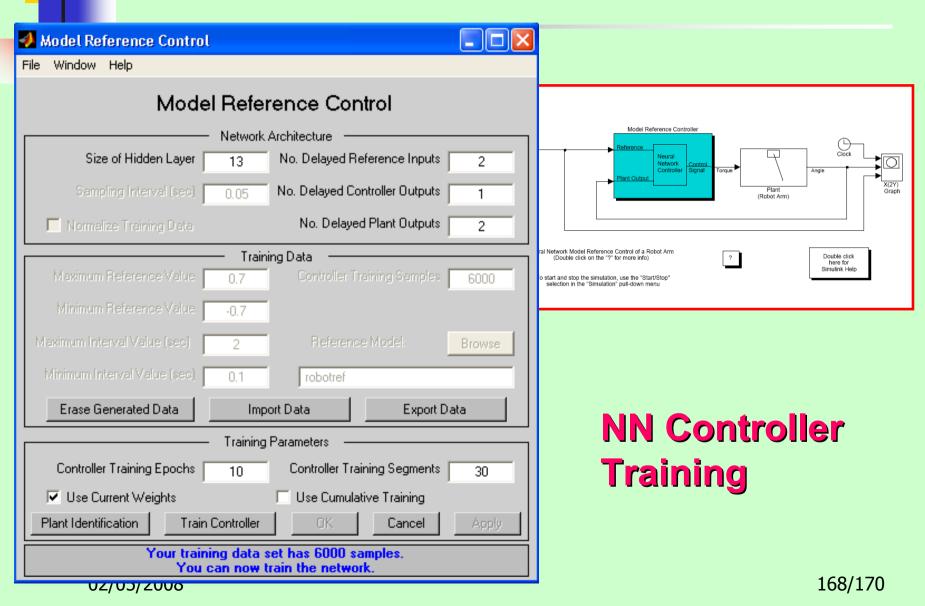
02/05/2008 166/170



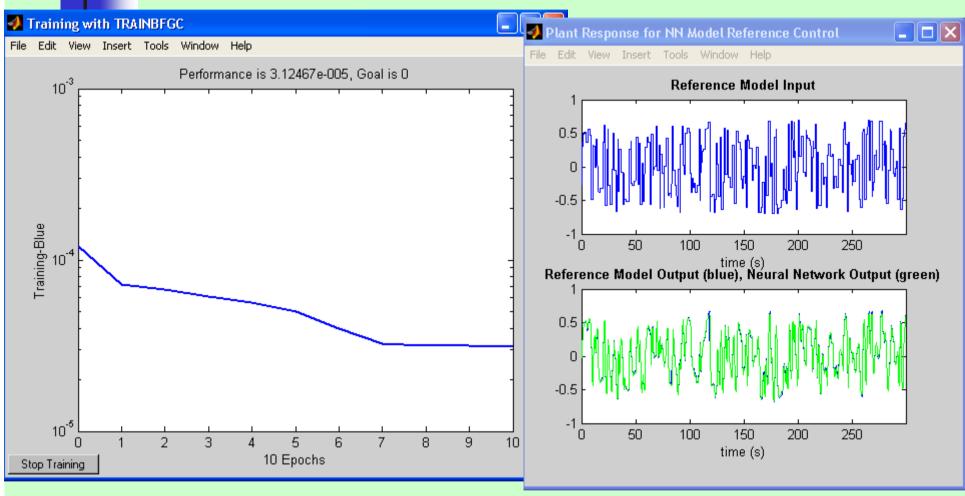


Accept the Data Generated for NN Controller Identification

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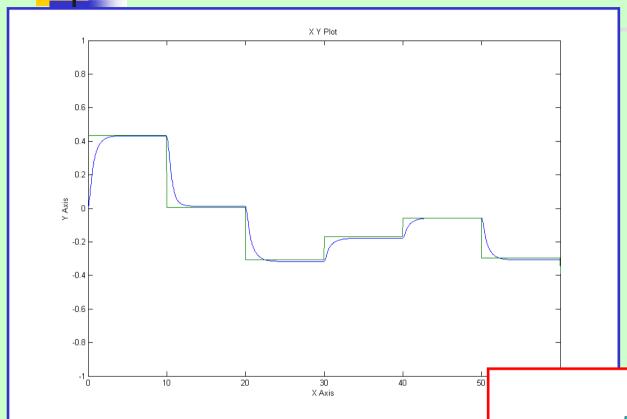






NN Controller Training and Results 02/05/2008





Reference and Tracked Output Signals

Simulation Final Results

02/05/2008

