

























































Mathematically the Perceptron is

$$y = f\left(\sum_{i=1}^{m} w_i x_i + b\right) = f\left(\sum_{i=0}^{m} w_i x_i\right)$$
We can always treat the bias b as another weight with inputs equal 1
where f is the hard limiter function i.e.

$$y = \begin{cases} 1 & \text{if } \sum_{i=1}^{m} w_i x_i + b > 0 \\ -1 & \text{if } \sum_{i=1}^{m} w_i x_i + b < 0 \end{cases}$$

 Two types of network training:

 Sequential mode (on-line, stochastic, or per-pattern) :

 Weights updated after each pattern is presented (Perceptron is in this class)

 Batch mode (off-line or per-epoch) :

 Weights updated after all patterns are presented

Backward Pass

Recall delta rule , error measure for pattern n is

$$E(t) = \frac{1}{2} \sum_{k=1}^{\infty} (d_k(t) - O_k(t))^2$$

We want to know how to modify weights in order to decrease E where

$$w_{ij}(t+1) - w_{ij}(t) \propto - \frac{\partial E(t)}{\partial w_{ij}(t)}$$

both for hidden units and output units

This can be rewritten as product of two terms using chain rule

Returning to **local error gradients** in BP algorithm we have for output units

$$\Delta_{i}(t) = (d_{i}(t) - O_{i}(t)) f'(Net_{i}(t))$$

= $(d_{i}(t) - O_{i}(t)) kO_{i}(t)(1 - O_{i}(t))$

For hidden units we have

$$\delta_{i}(t) = f'(net_{i}(t)) \sum_{k} \Delta_{k}(t) W_{ki}$$

= $ky_{i}(t)(1 - y_{i}(t)) \sum_{k} \Delta_{k}(t) W_{ki}$

Since degree of weight change is proportional to derivative of activation function, weight changes will be greatest when units receives mid-range functional signal than at extremes

Aim is to minimise an error function over all training patterns by adapting weights in MLP

Recalling the typical error function is the mean squared error as follows

$$\mathsf{E}(\mathsf{t}) = \frac{1}{2} \sum_{k=1}^{p} \left(d_{k}(t) - O_{k}(t) \right)^{2}$$

The idea is to reduce E(t) to global minimum point.

<section-header><list-item><list-item><list-item>

History Background

- Idea of evolutionary computing was introduced in the 1960s by I.
 Rechenberg in his work "*Evolution strategies*" (*Evolutionsstrategie* in original). His idea was then developed by other researchers. Genetic
 Algorithms (GAs) were invented by John Holland and developed by him and his students and colleagues. This lead to Holland's book "*Adaption in Natural and Artificial Systems*" published in 1975.
- In 1992 John Koza has used genetic algorithm to evolve programs to perform certain tasks. He called his method "Genetic Programming" (GP). LISP programs were used, because programs in this language can expressed in the form of a "parse tree", which is the object the GA works on.

A Simple Genetic Algorithm									
Optimization	n task :	find the max	imum of f(x)					
for example	f(x)=x∙:	$\sin(\mathbf{x}) \mathbf{x} \in [0]$,π]						
• genotype: bir	ary stri	ng $s \in [0,1]^5$	e.g. 11010, 0	01011, 10001					
• mapping : ge	notype	phenotype	en=5	1 / (*** **)					
binary intege	er encoc	ling: $x = \pi$	• $\sum_{i=1}^{n} \mathbf{s}_i \cdot 2^{\mathbf{n} - \mathbf{i}}$	$1 / (2^{n}-1)$					
Initial population									
genotype	integ.	phenotype	fitness	prop. fitness					
<u>11010</u>	26	2.6349	1.2787	30%					
<u>01011</u>	11	1.1148	1.0008	24%					
<u>10001</u>	17	1.7228	1.7029	40%					
<u>00101</u>	5	0.5067	0.2459	6%					
				113					

That is, given a set of N vectors \underline{X}_i and a corresponding set of N real numbers, d_i (the targets), find a function F that satisfies the interpolation condition: $F(\underline{X}_i) = d_i \quad \text{for } i = 1, ..., N$ or more exactly find: $F(\overline{X}) = \sum_{i=1}^{N} w^i \phi(||\overline{X} - \overline{X}^j||)$ satisfying: $F(\overline{X}^i) = \sum_{i=1}^{N} w^i \phi(||\overline{X}^i - \overline{X}^j||) = d^i$

Overfitting problem

Bishop(1995) example

Underlying function $f(x)=0.5+0.4sine(2\pi x)$ sampled randomly for 30 points

added Gaussian noise to each data point

30 data points 30 hidden RBF units

fits all data points but creates oscillations due added noise and unconstrained between data points

📣 Network	/Data Manager		
Inputs:	Networks:	Outputs:	
U	network1	out5	
	network2	out10	
Targets:		Errors:	
У		err5	
		ento	
Input Delay 5	itates:	Layer Delay 5	itates:
- Networks a	nd Data		
	Help New Dat	a New Network	
1	mport Export	View Delete	
⊢ ⊢Networks o	nly		
	itializa Rimulata	Train Adapt	1